

# Magnetostàtica

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# La força de Lorentz

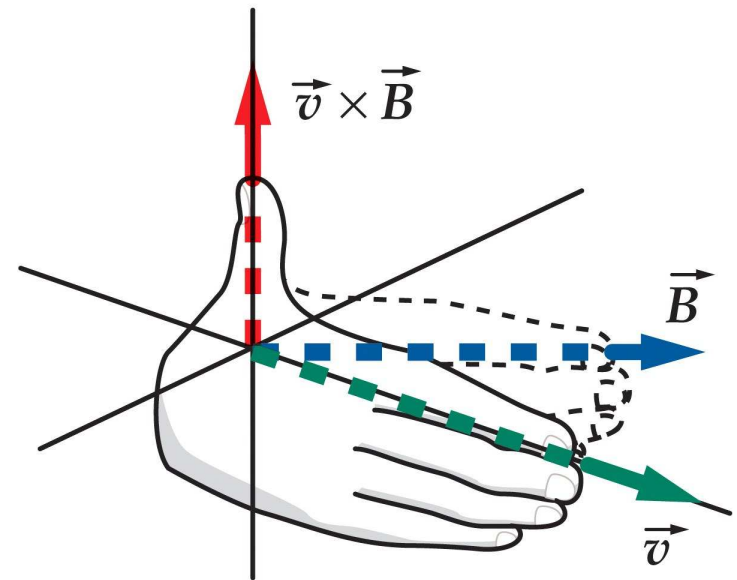
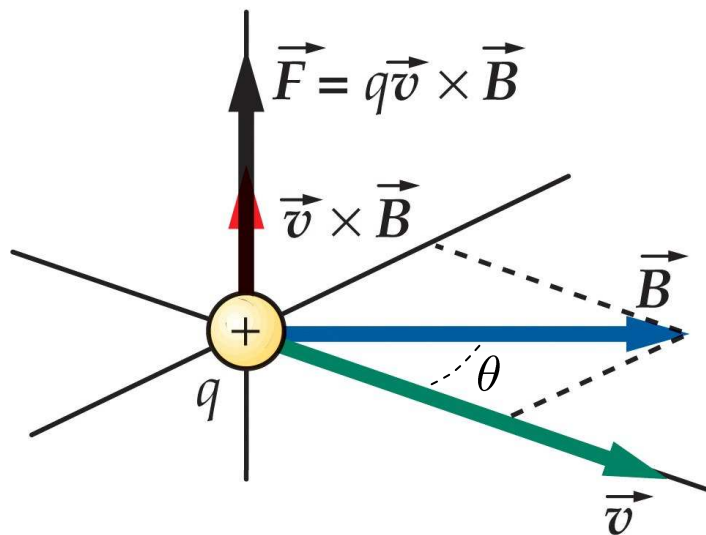
Camp magnètic  $\vec{B}(\vec{r})$

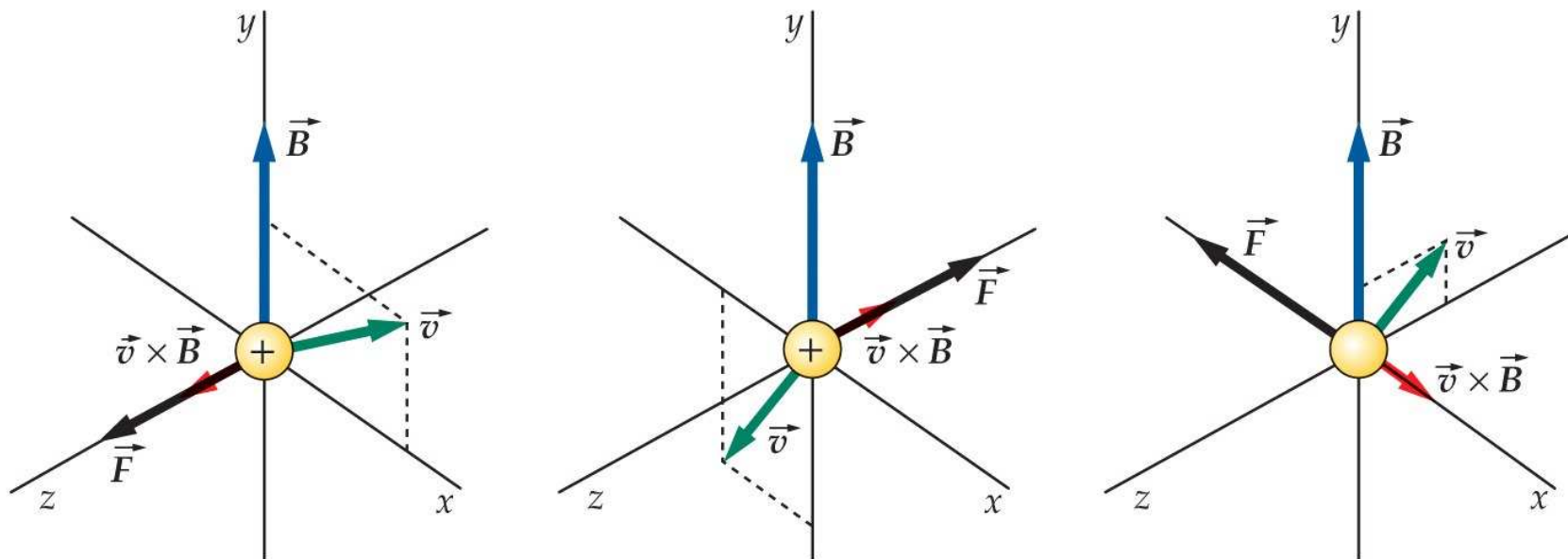
Una càrrega en moviment dins un camp magnètic experimenta una força

$$\vec{F} = q \vec{v} \times \vec{B}$$

$$\vec{F} = q (\vec{E} + \vec{v} \times \vec{B})$$

$$F = qvB \sin \theta$$





## Unitat

$$[B] = \frac{[F]}{[qv]} = \frac{\text{N}}{\text{C m}} = \text{T} \quad \text{tesla}$$

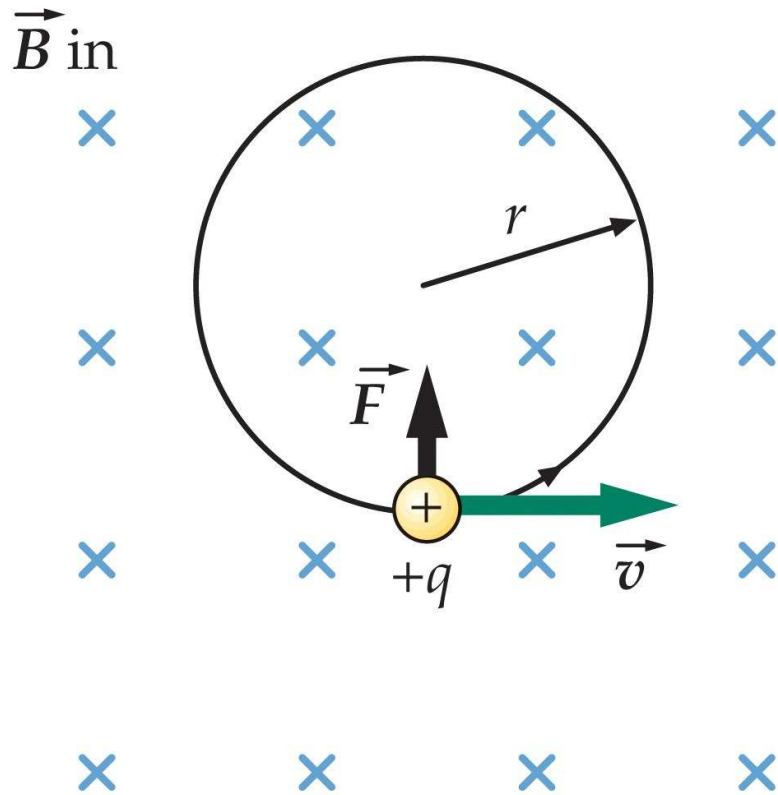
A vegades

weber  $\text{Wb} = \text{T m}^2$  (flux de camp magnètic)

$\text{T} = 10^4 \text{G}$  gauss

camp de laboratori  $B \lesssim 1\text{T}$

## Moviment d'una càrrega puntual



Moviment circular uniforme  
acceleració centrípeta

$$\vec{F}_{\text{cent}} = q \vec{v} \times \vec{B}$$

$$m \frac{v^2}{r} = qvB$$

$$r = \frac{mv}{qB}$$

velocitat angular constant

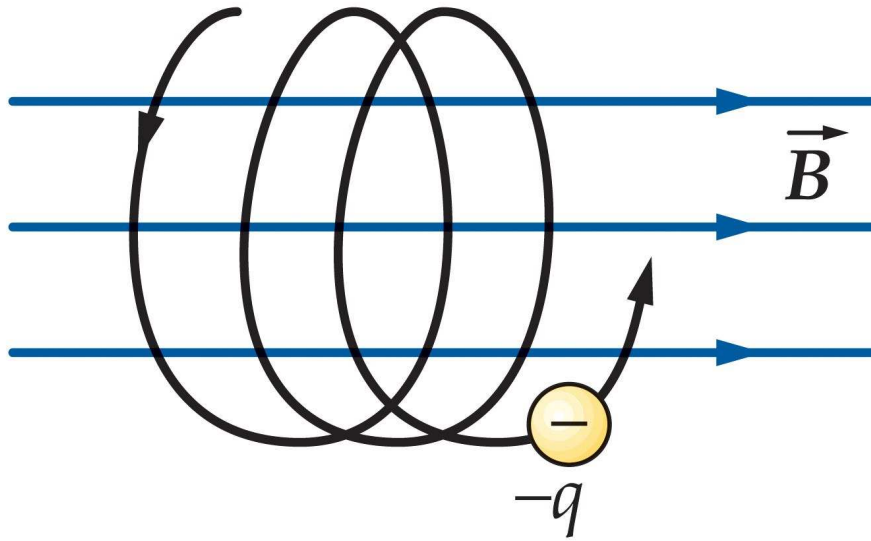
$$\omega \equiv \frac{v}{r} = \frac{qB}{m}$$

freqüència i període

$$\omega = 2\pi f = \frac{2\pi}{T}$$

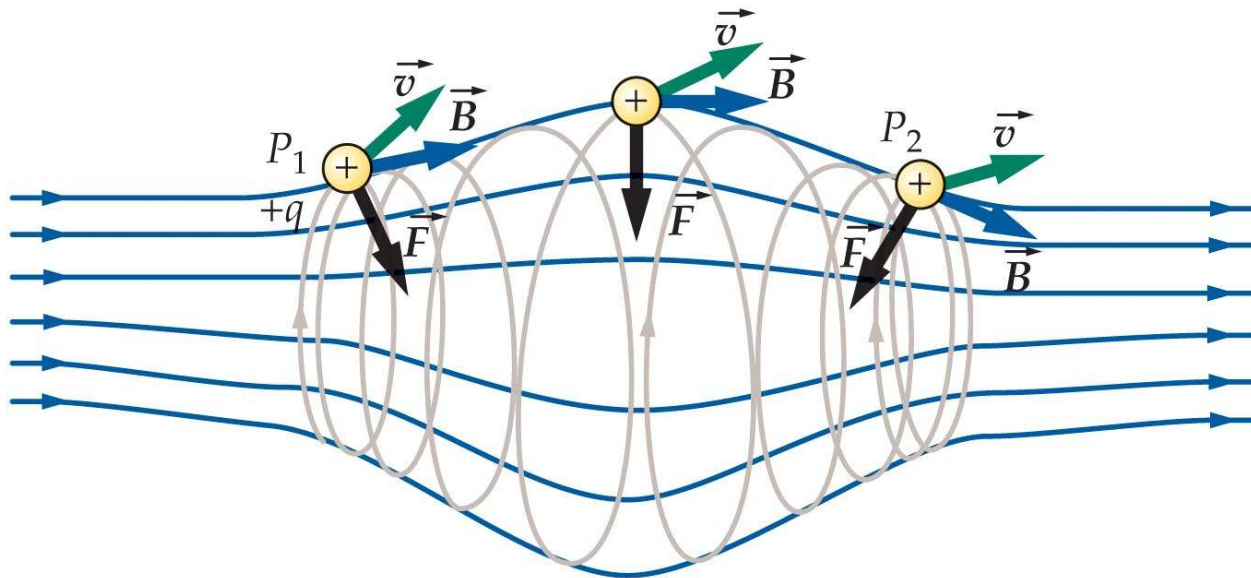
Freqüència  $f$  i freqüència angular  $\omega$

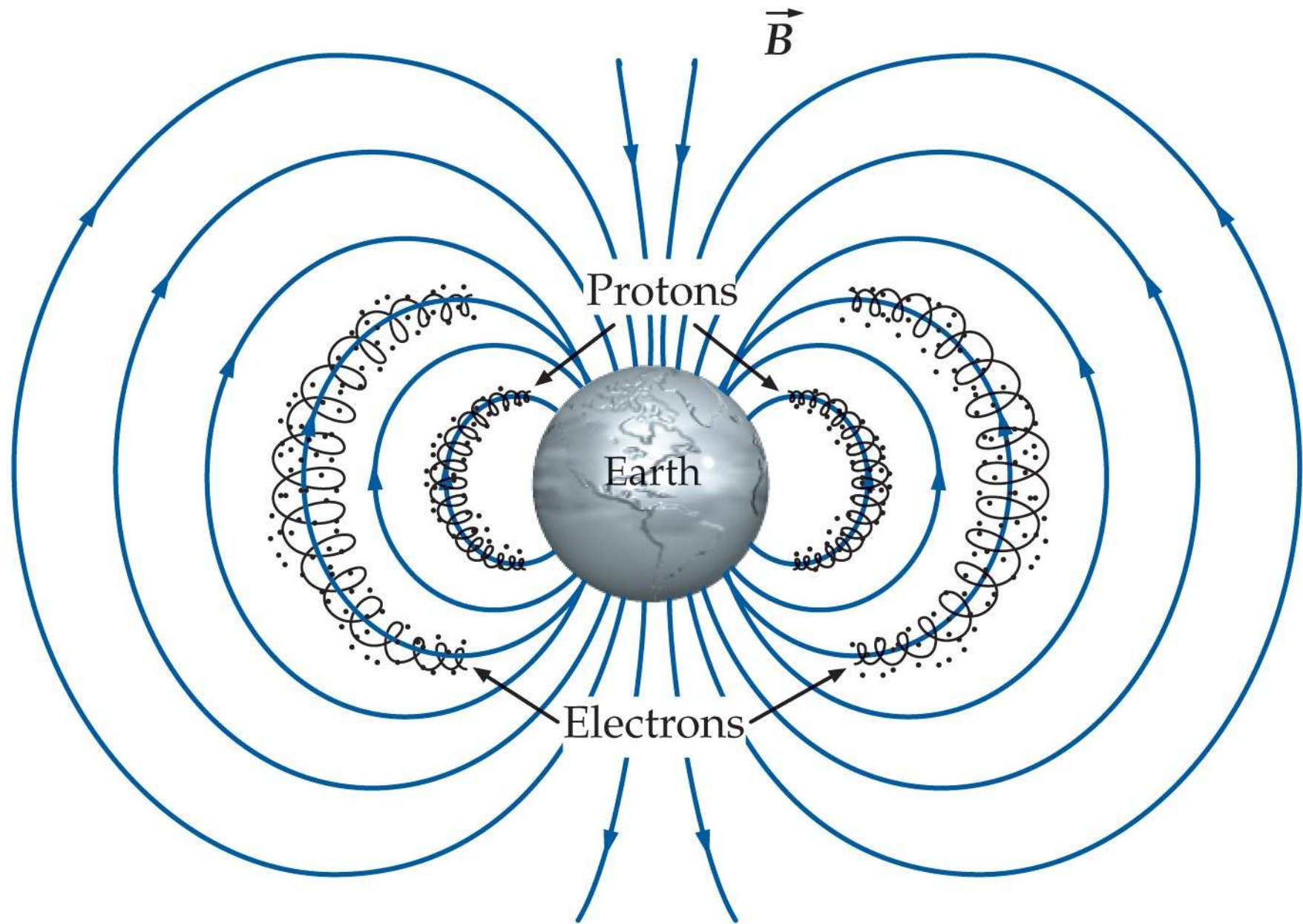
$$\omega_c = \frac{qB}{m} \quad \text{freqüència de ciclotró}$$



$$\vec{v} = v_{\parallel} \hat{u}_{\parallel} + v_{\perp} \hat{u}_{\perp}$$

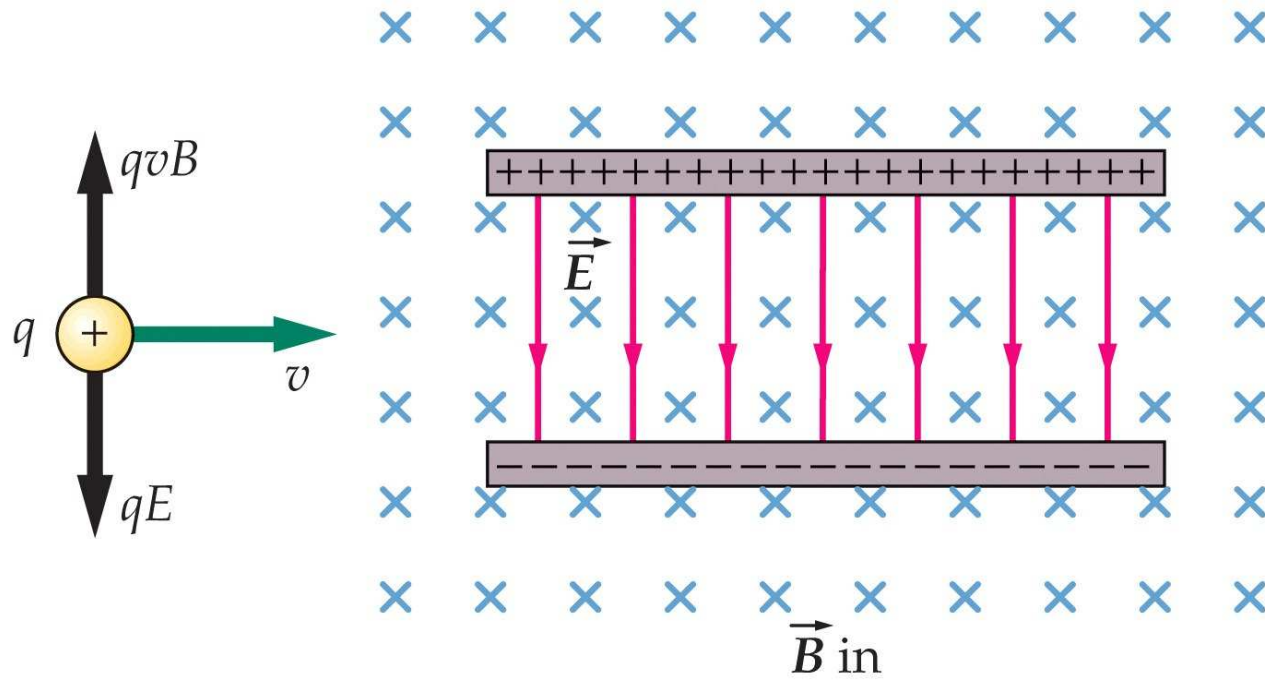
$$r = \frac{mv_{\perp}}{qB}$$



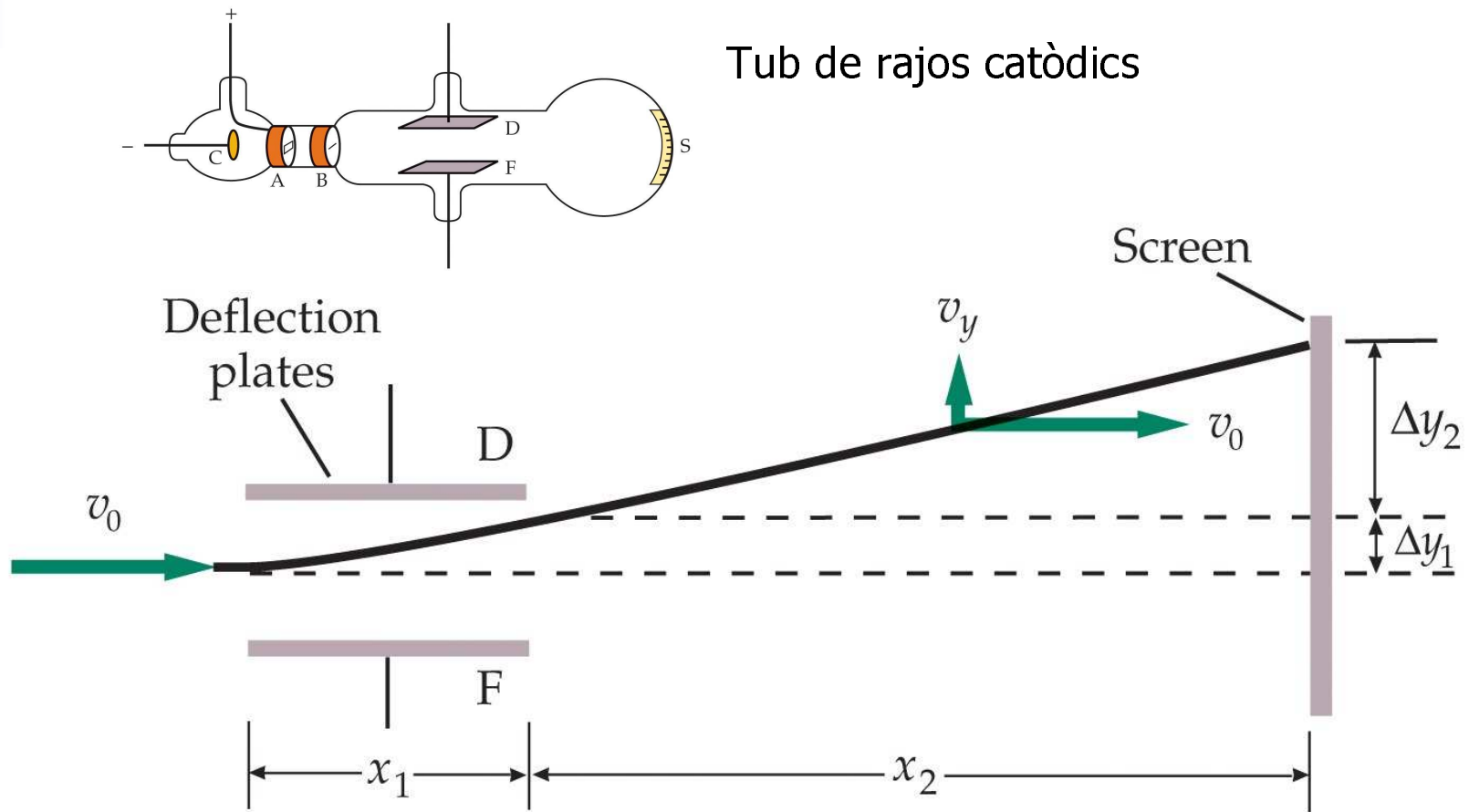




$$\vec{F} = q(\vec{E} + \vec{v} \times \vec{B})$$



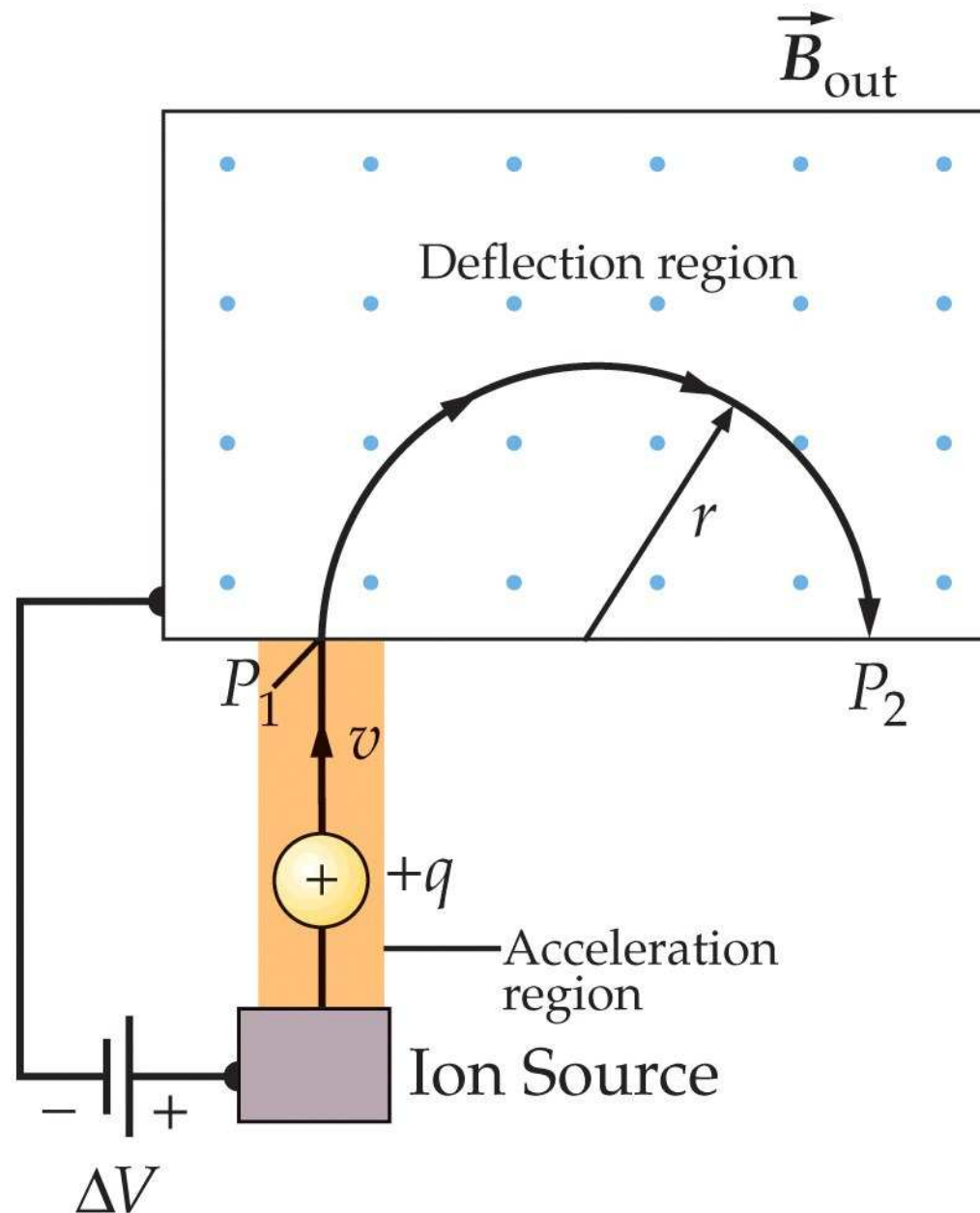
# L'experiment de Thomson



$$\left. \begin{aligned} \Delta y_1 &= \frac{1}{2} \left( \frac{qE}{m} \right) \left( \frac{x_1}{v_0} \right)^2 \\ \text{Sense deflexió } \frac{qE}{m} &= qv_0 B \end{aligned} \right\} \quad \frac{q}{m} \approx 1.76 \times 10^{11} \frac{\text{C}}{\text{kg}}$$



# Espectròmetre de masses

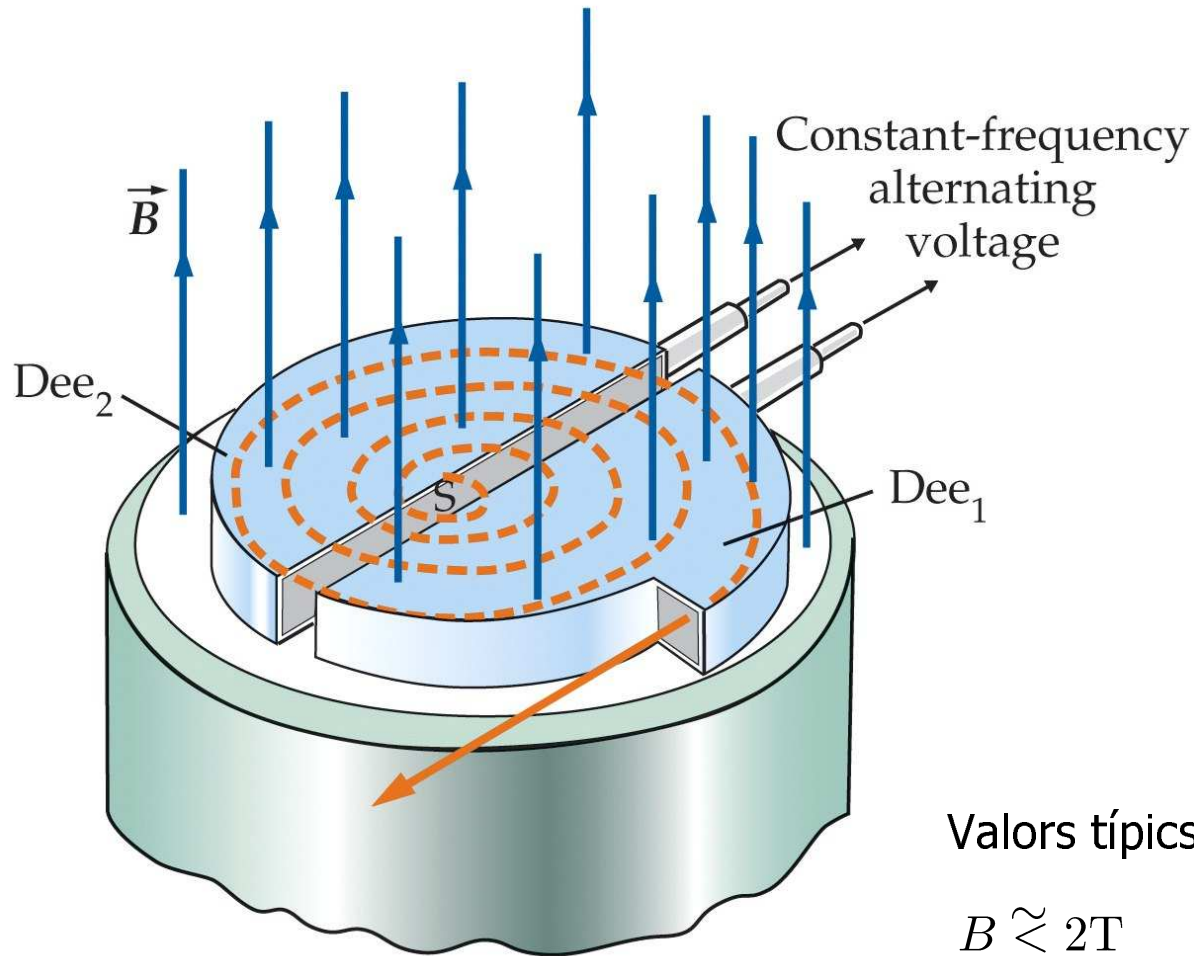


$$\frac{1}{2}mv^2 = q|\Delta V|$$

$$v^2 = \frac{r^2 q^2 B^2}{m^2}$$

$$\frac{m}{q} = \frac{B^2 r^2}{2|\Delta V|}$$

# El ciclotrón



$$V = V_0 \cos \omega_p t$$

$$\omega_p = \omega_c \quad (\omega_p = n\omega_c)$$

$$v_{\max} = \omega_c R_{\max} = \frac{qB}{m} R_{\max}$$

$$E_{\max} = \frac{1}{2} m v_{\max}^2$$

$$= \frac{1}{2} \frac{q^2 B^2}{m} R_{\max}^2$$

Valors típics

$$B \approx 2T$$

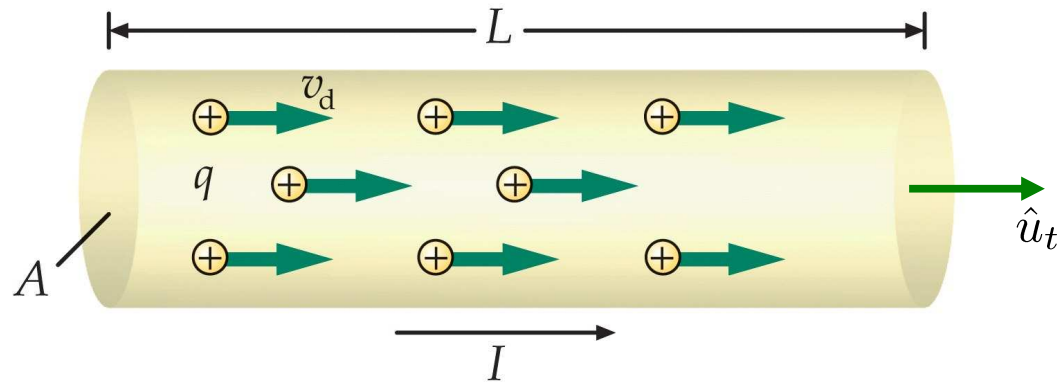
$$R \approx 30cm$$

protons

$$E_{\max} \approx 2MeV$$

$$(1MeV = 10^6 eV = 10^6 \cdot 1.6 \cdot 10^{-19} J)$$

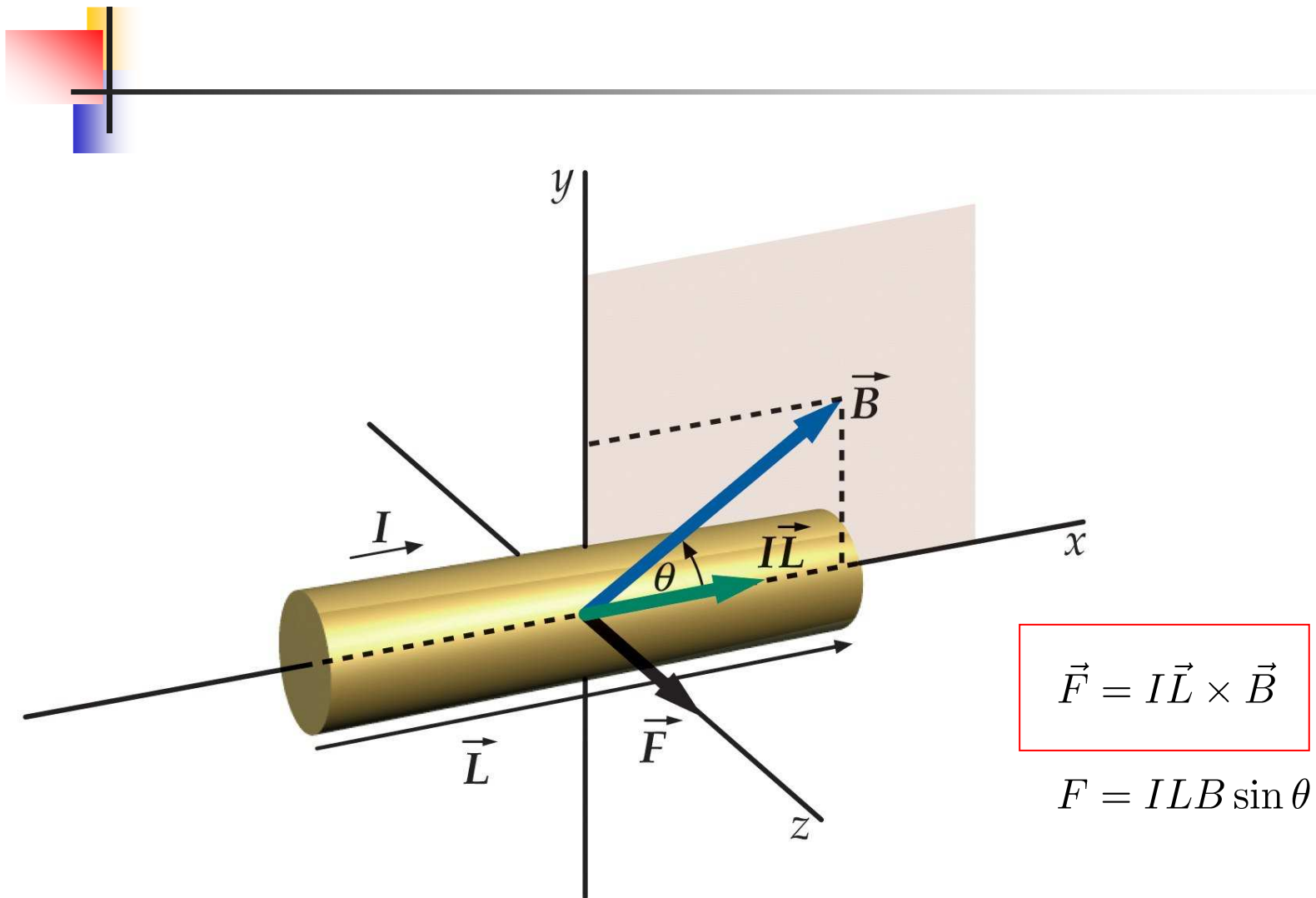
## Força magnética sobre un corrent

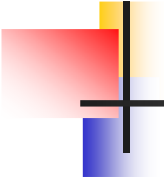


$$\Delta \vec{F} = (n \Delta V) q \vec{v}_d \times \vec{B}$$

$$\Delta \vec{F} = \vec{j} \times \vec{B} \Delta V$$

$$\frac{\Delta \vec{F}}{\Delta L} = \vec{j} \times \vec{B} A = I \hat{u}_t \times \vec{B}$$

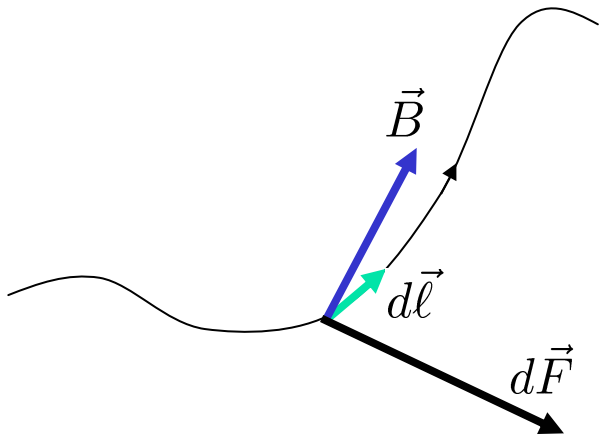



$$d\vec{F} = I d\vec{\ell} \times \vec{B}$$

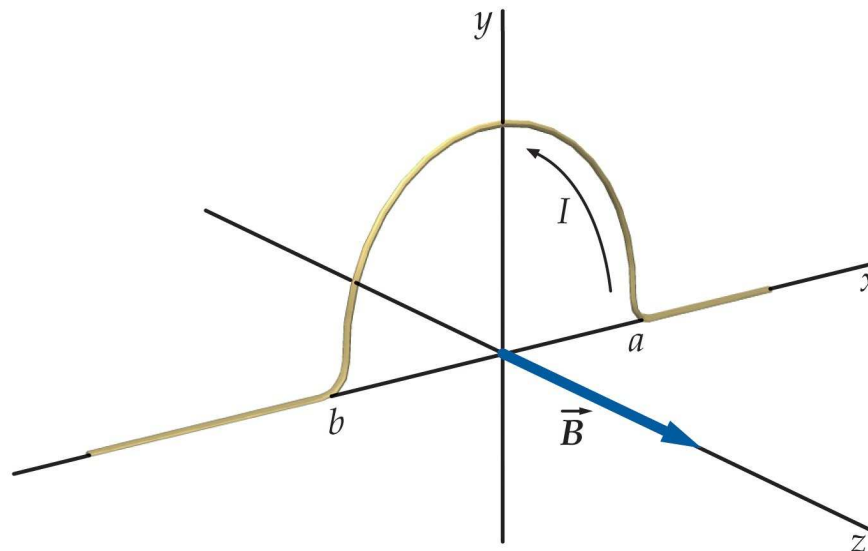
26-5

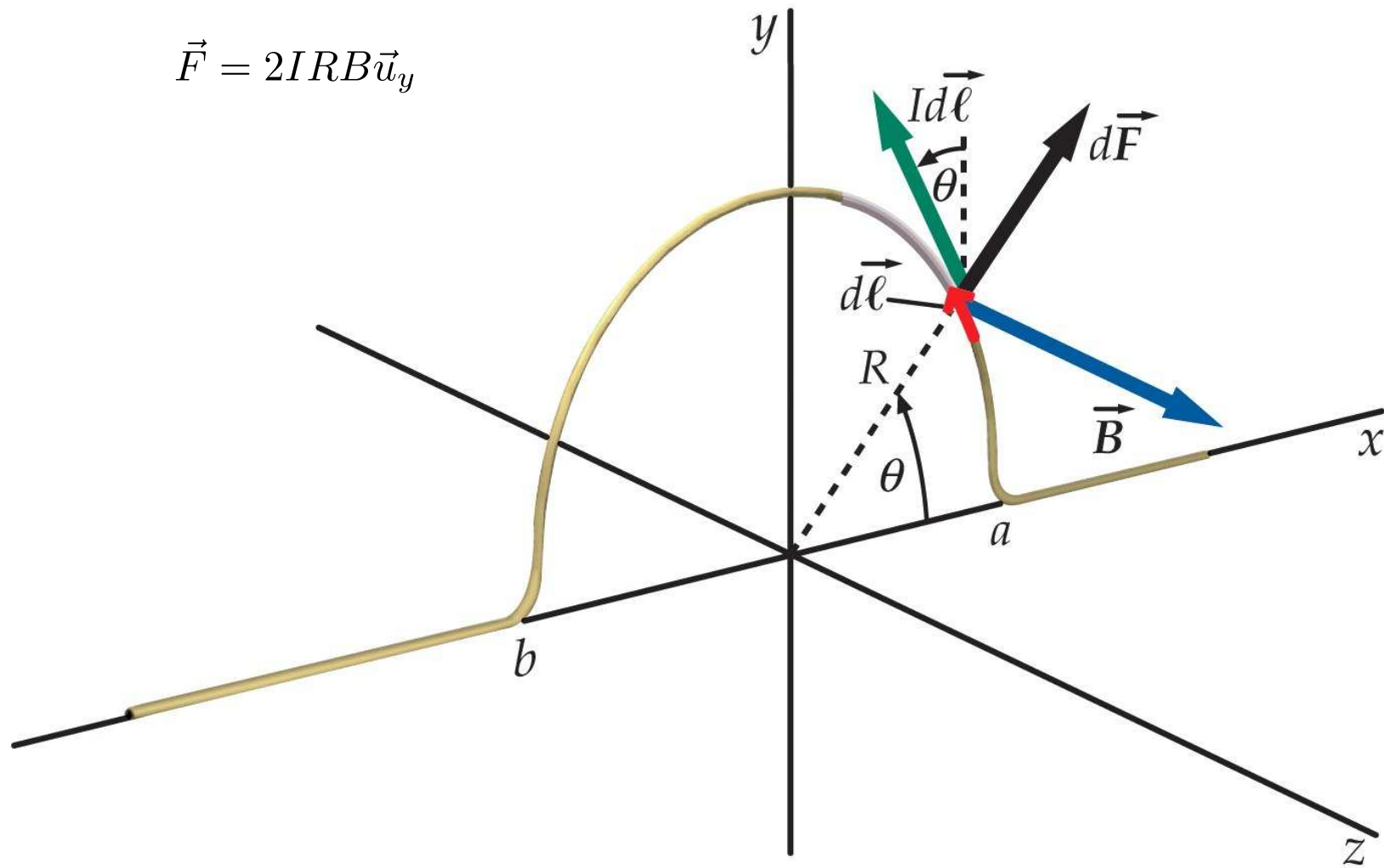
MAGNETIC FORCE ON A CURRENT ELEMENT

$$\vec{F} = \int d\vec{F} = I \int d\vec{\ell} \times \vec{B}$$

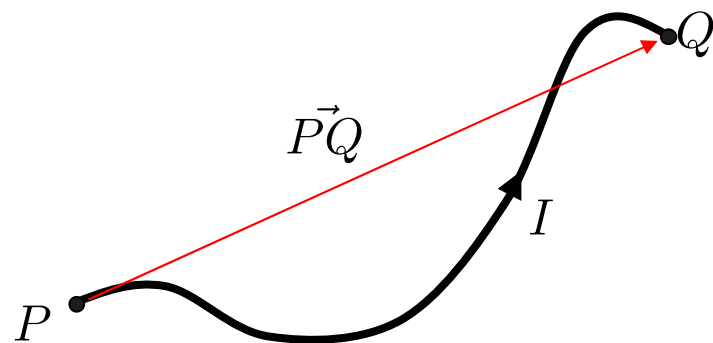


**Example:**





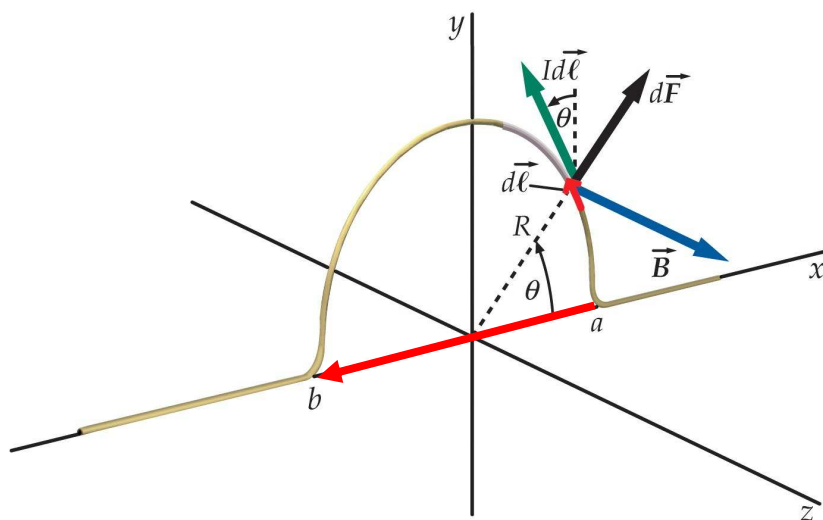
## Camp uniforme i fil arbitrari



$$\vec{F} = \int d\vec{F} = I \int d\vec{\ell} \times \vec{B}$$

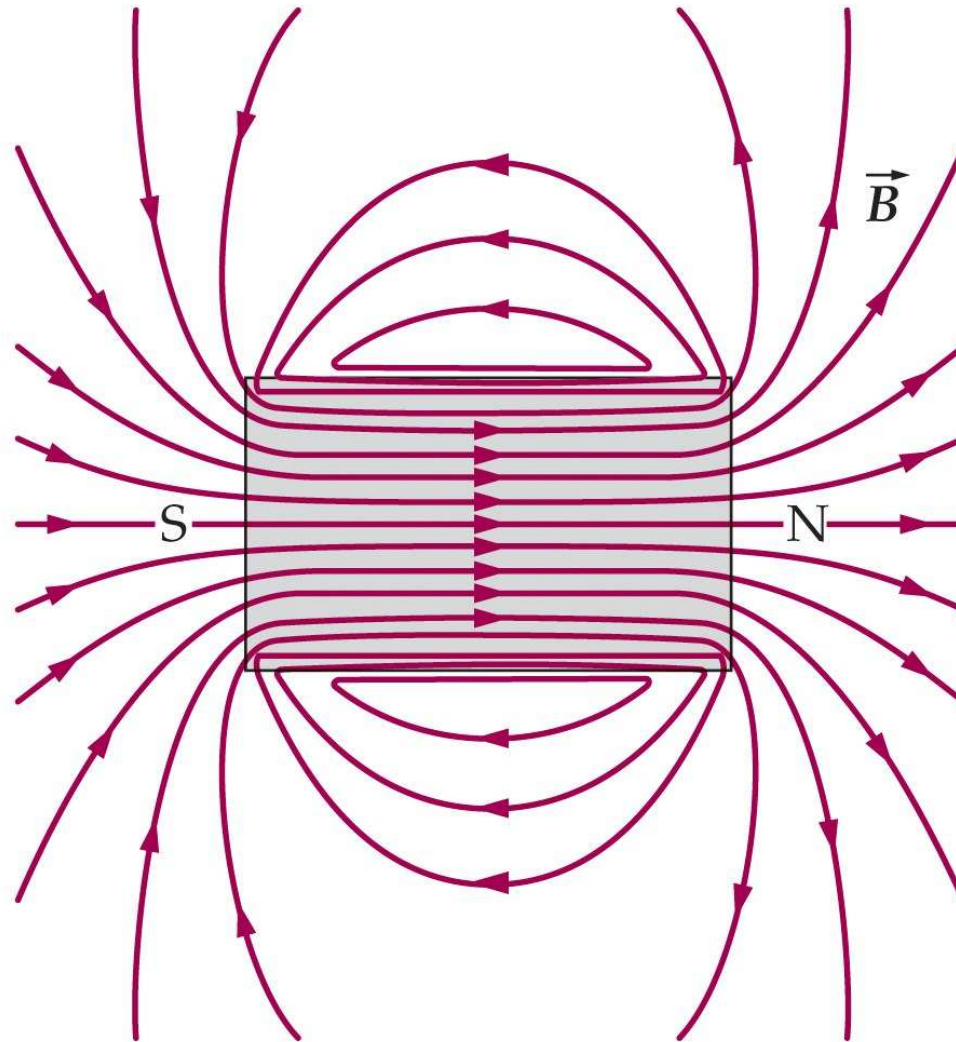
$$\int_P^Q d\vec{\ell} = \vec{PQ}$$

$$\vec{F} = I \vec{PQ} \times \vec{B}$$

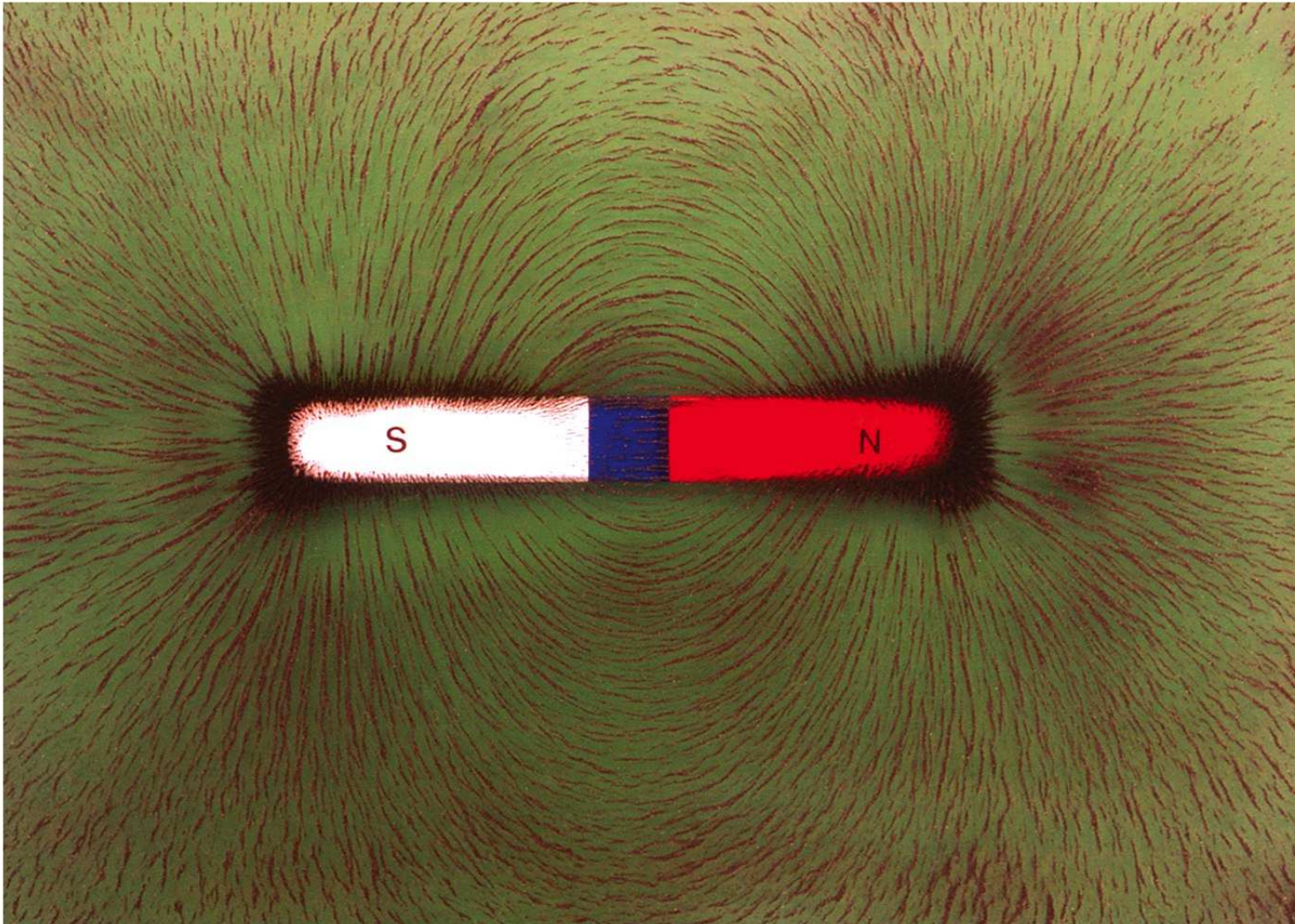


$$\vec{F} = 2IRB\vec{u}_y$$

## Les línies de camp magnètic



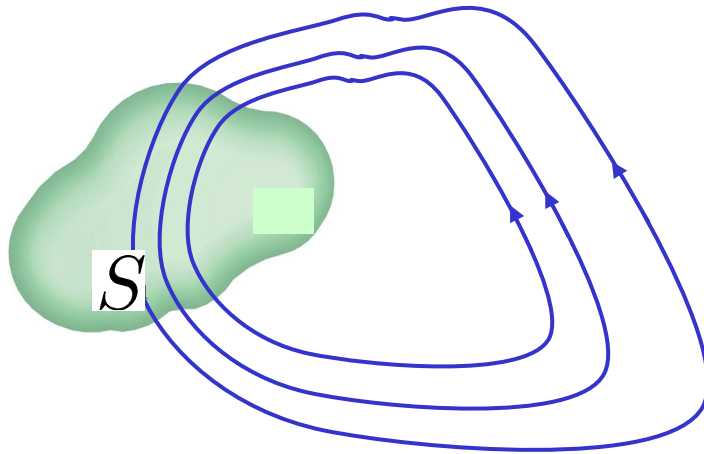




# Primera llei de la magnetostàtica

El flux de camp magnètic per una superfície tancada és zero

$$\oint_S \vec{B} \cdot d\vec{s} = 0$$



Les línies de camp magnètic són tancades  
No hi ha "càrregues magnètiques"

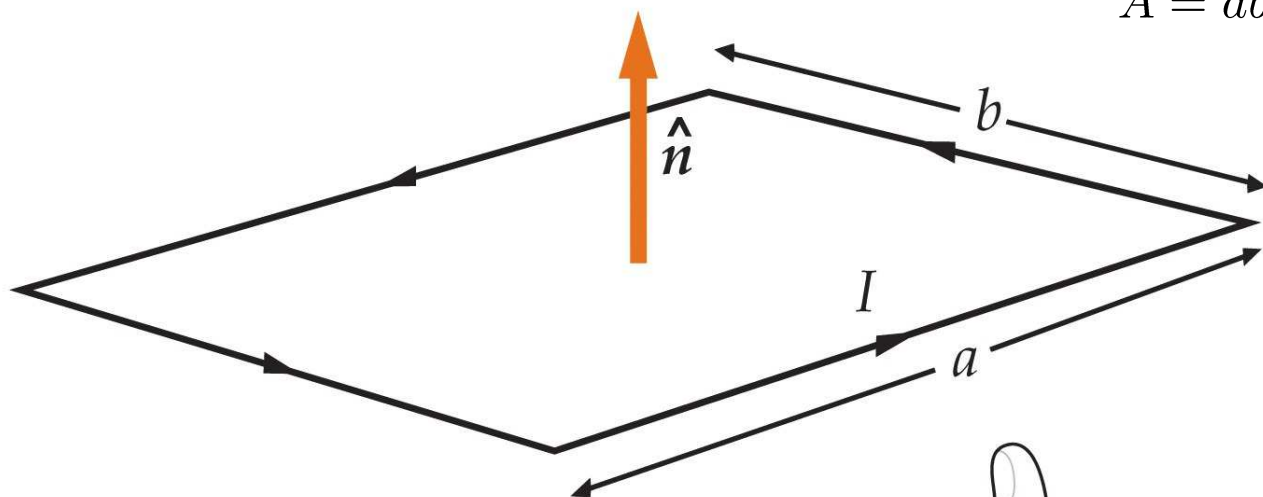
# Moments de força sobre espires de corrent i imants

## Moment dipolar magnètic (*moment magnètic*)

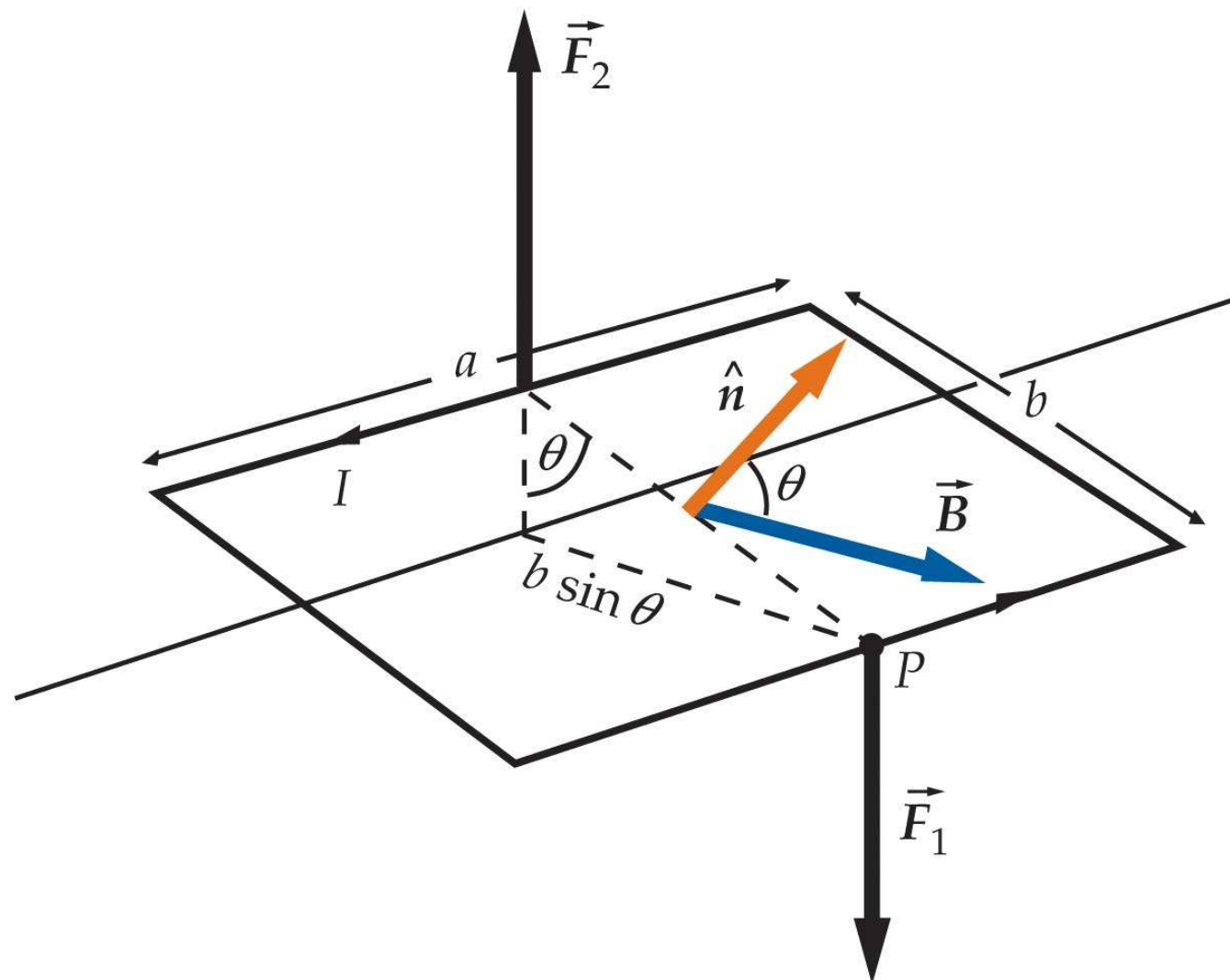
D'una espira de corrent

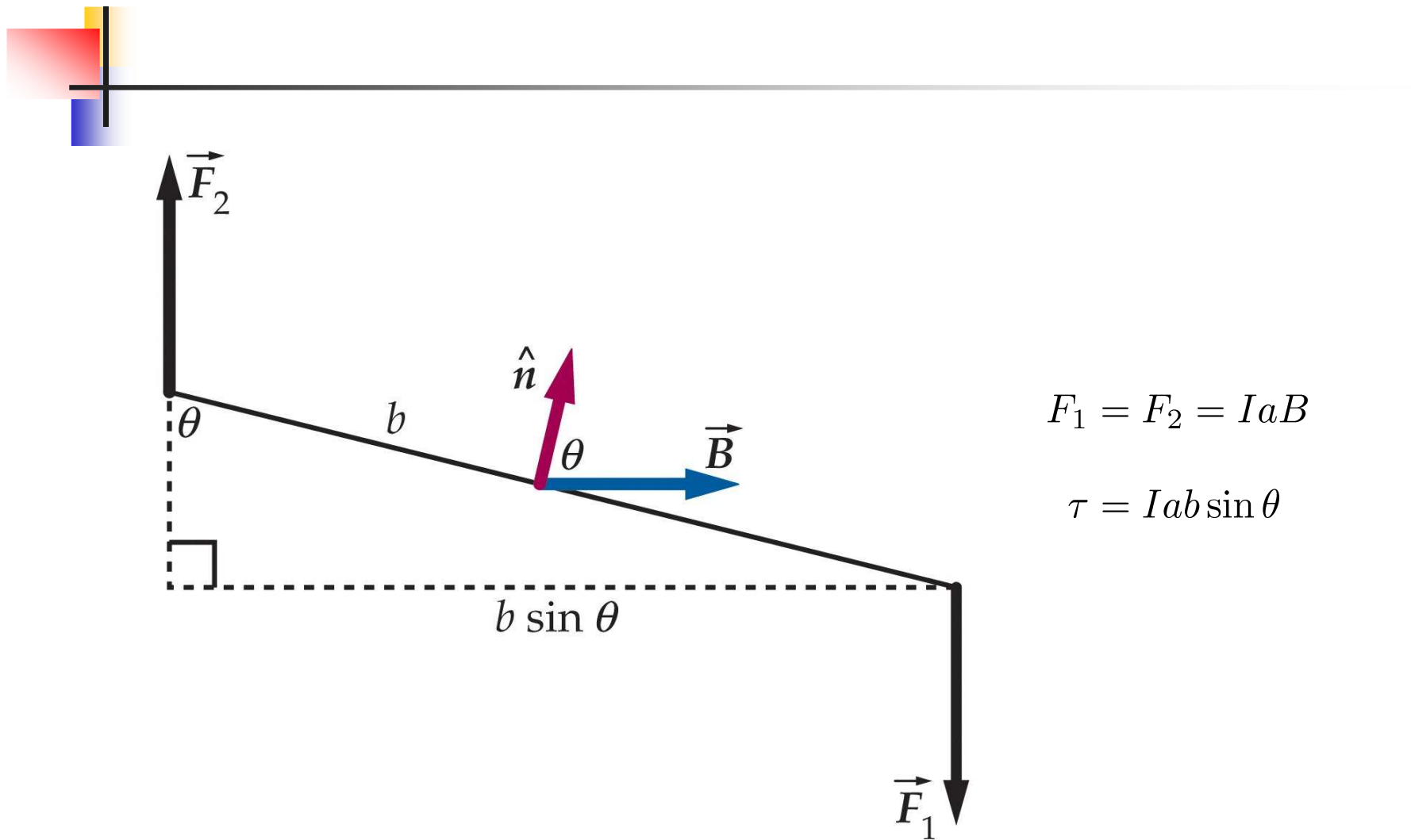
$$\vec{\mu} = I A \hat{n}$$

$$A = ab$$



## Espira dins un camp magnètic



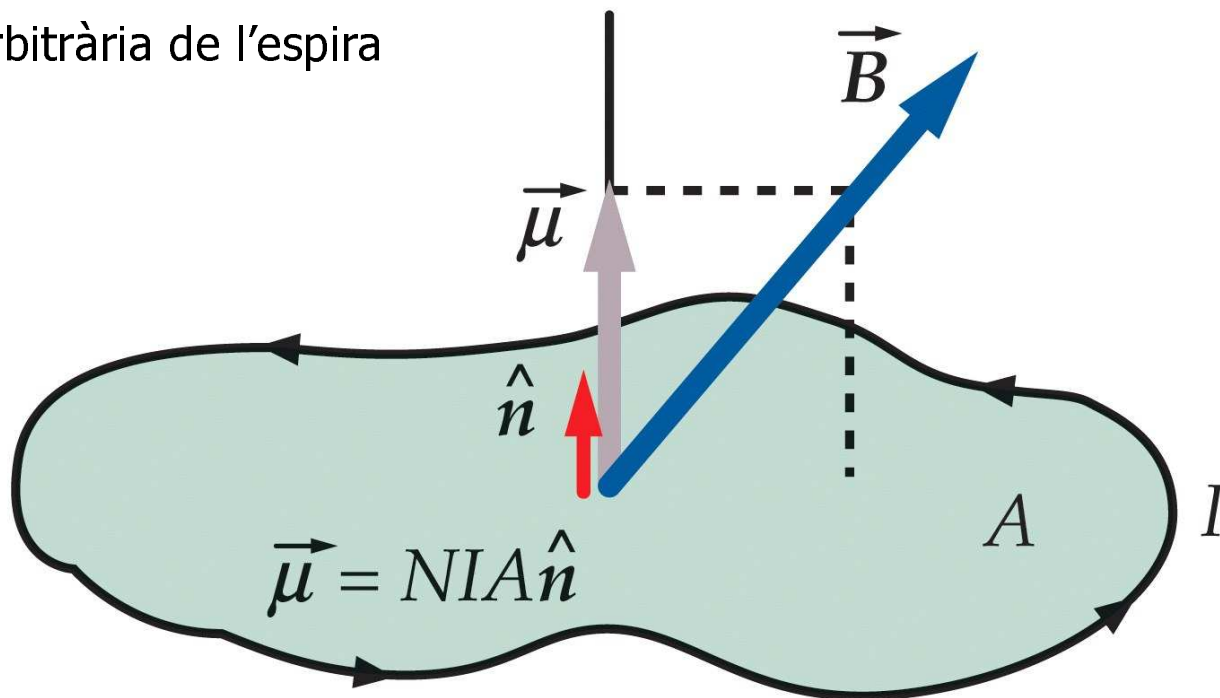


$$\vec{\tau} = \vec{\mu} \times \vec{B}$$

26-15



Forma arbitrària de l'espira

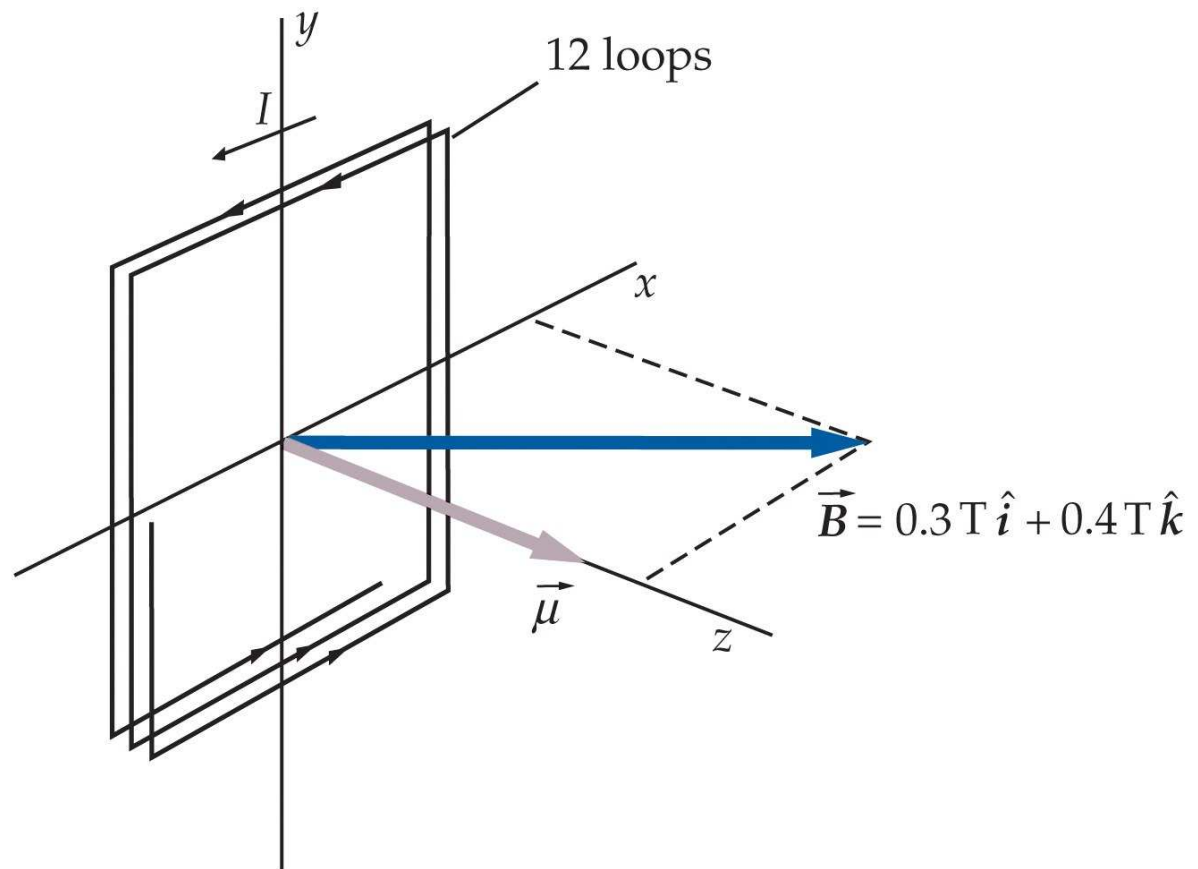


**Energia potencial d'una espira dins un camp magnètic**

$$U = -\mu B \cos \theta = -\vec{\mu} \cdot \vec{B}$$

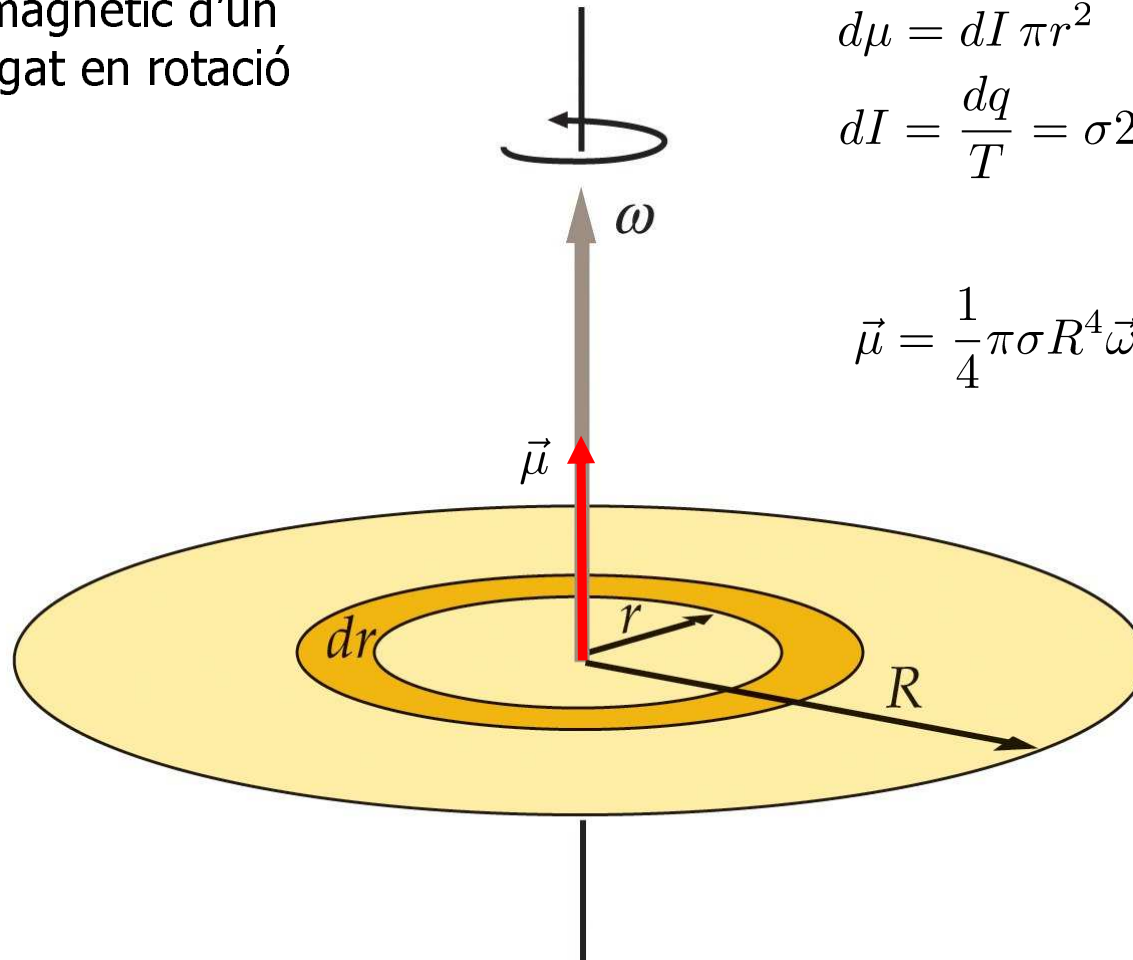
## Exemples

Moment de força sobre una bobina





Moment magnètic d'un  
disc carregat en rotació



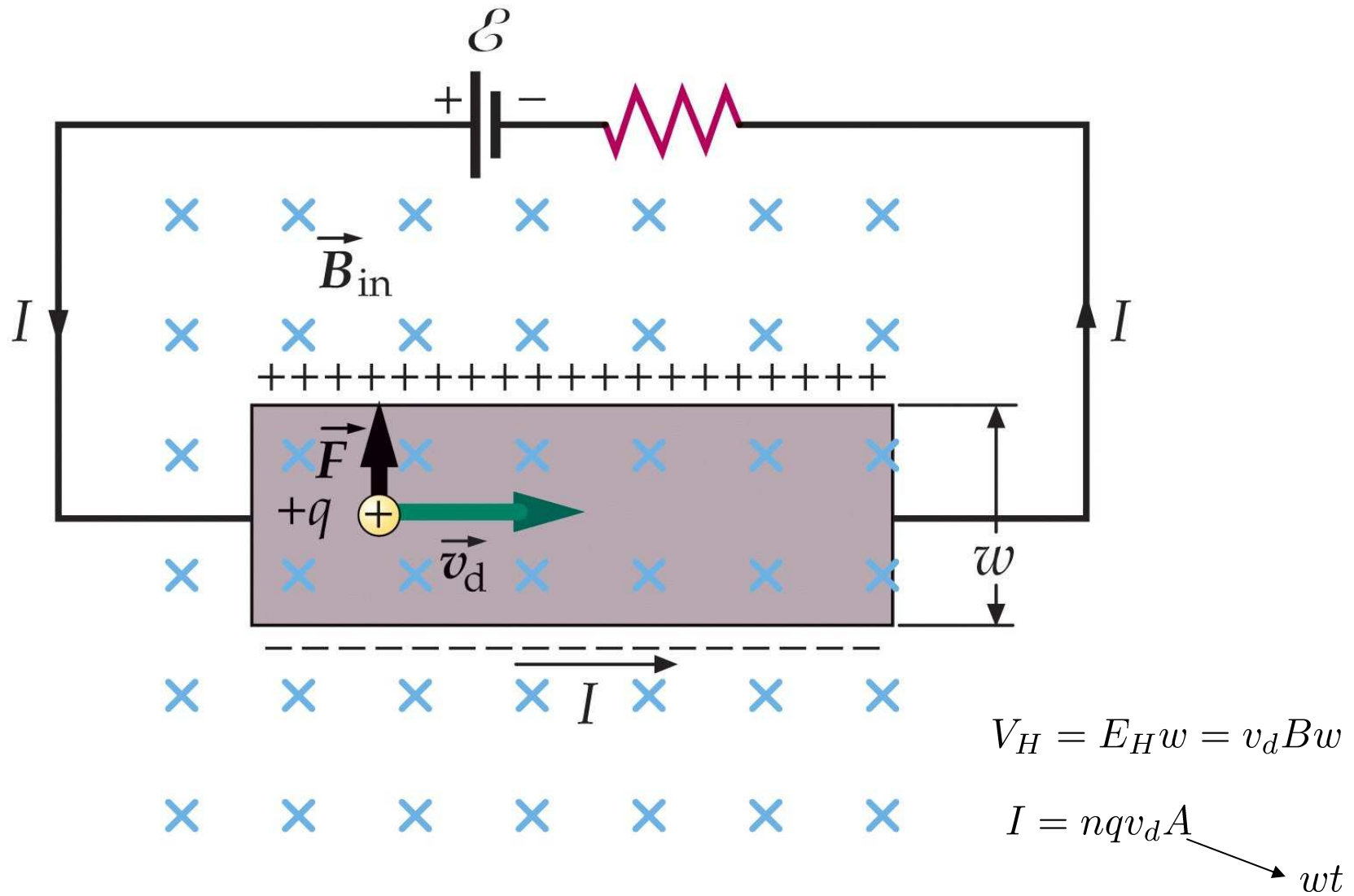
$$d\mu = dI \pi r^2$$

$$dI = \frac{dq}{T} = \sigma 2\pi r dr \frac{\omega}{2\pi} = \sigma \omega r dr$$

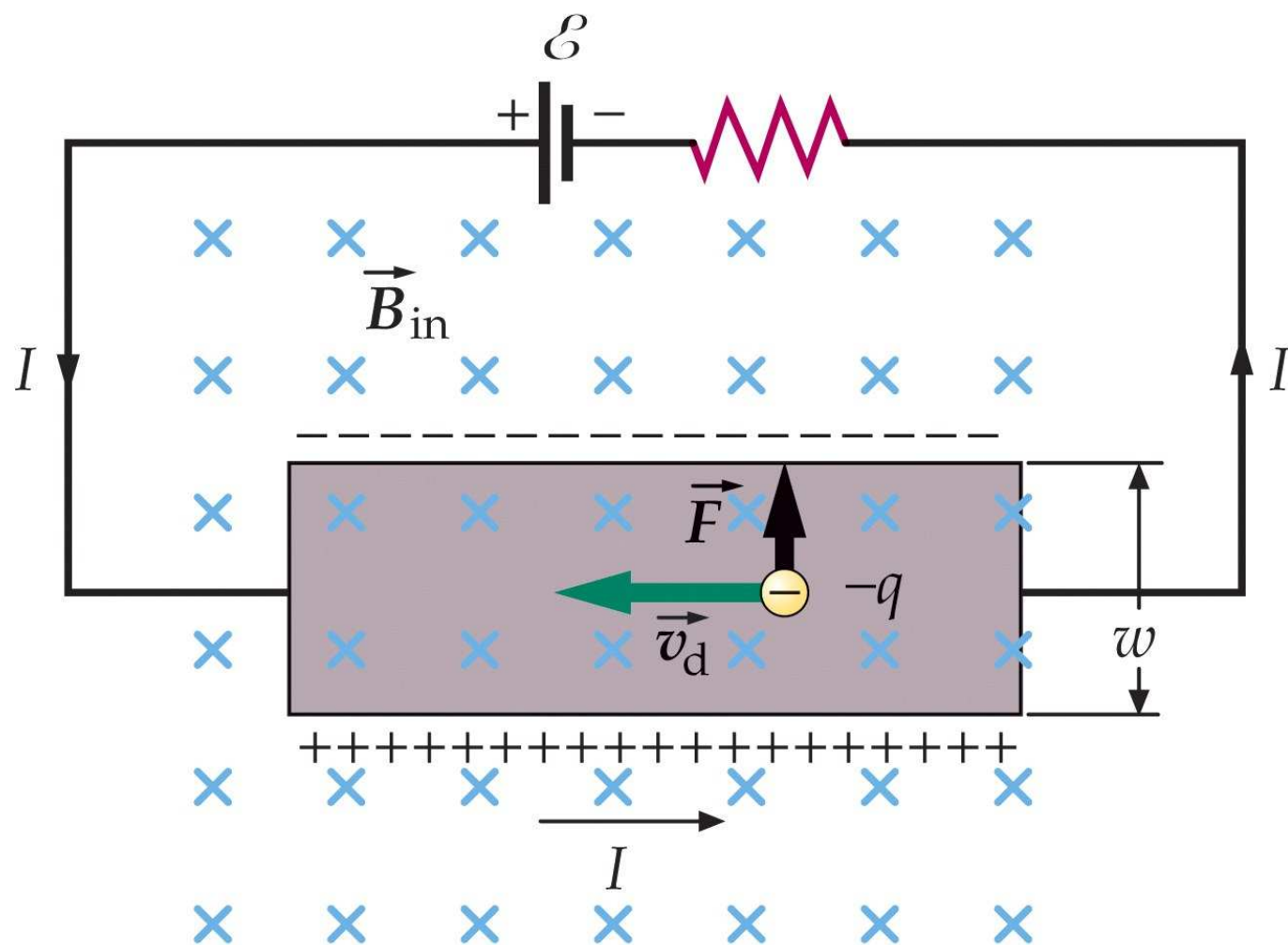
$$\vec{\mu} = \frac{1}{4} \pi \sigma R^4 \vec{\omega}$$



# L'efecte Hall



$$V_H = \frac{I}{nqt} B \quad \text{mesura de B}$$

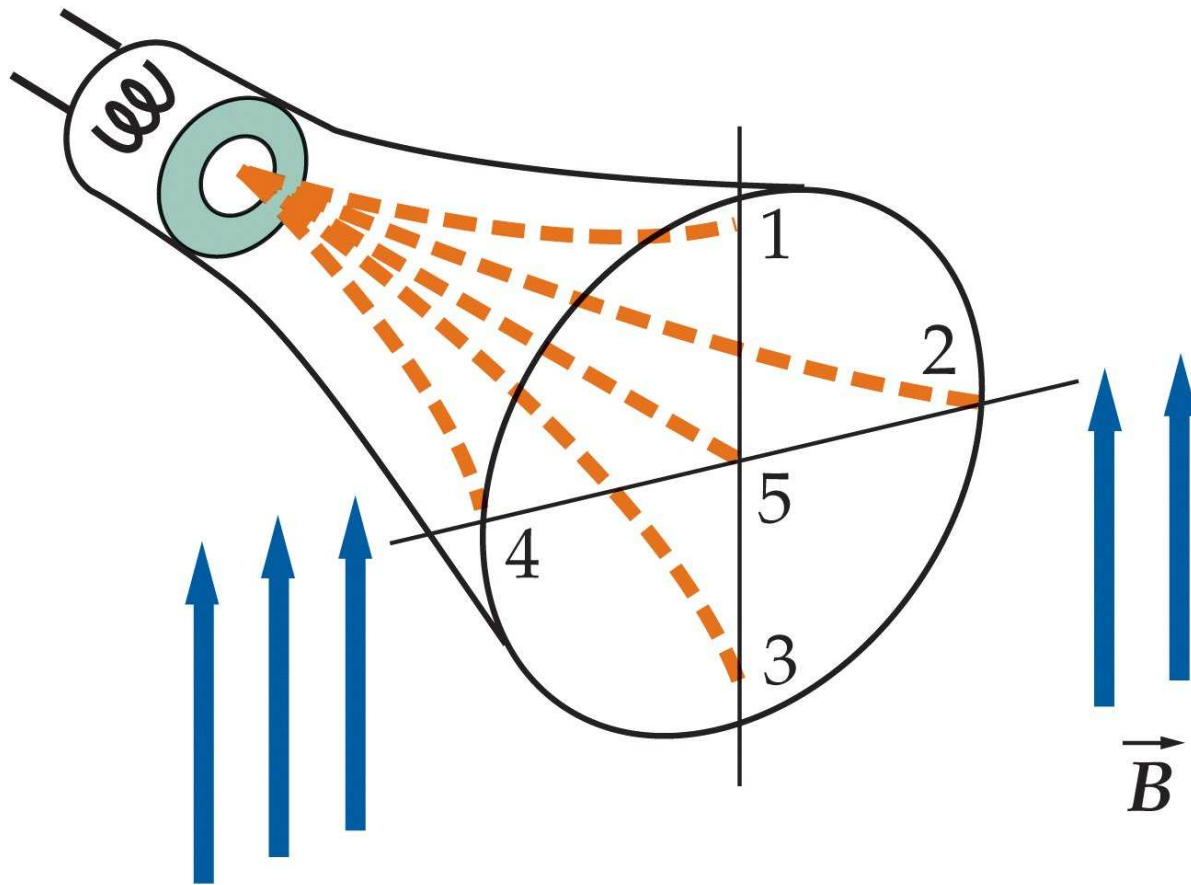




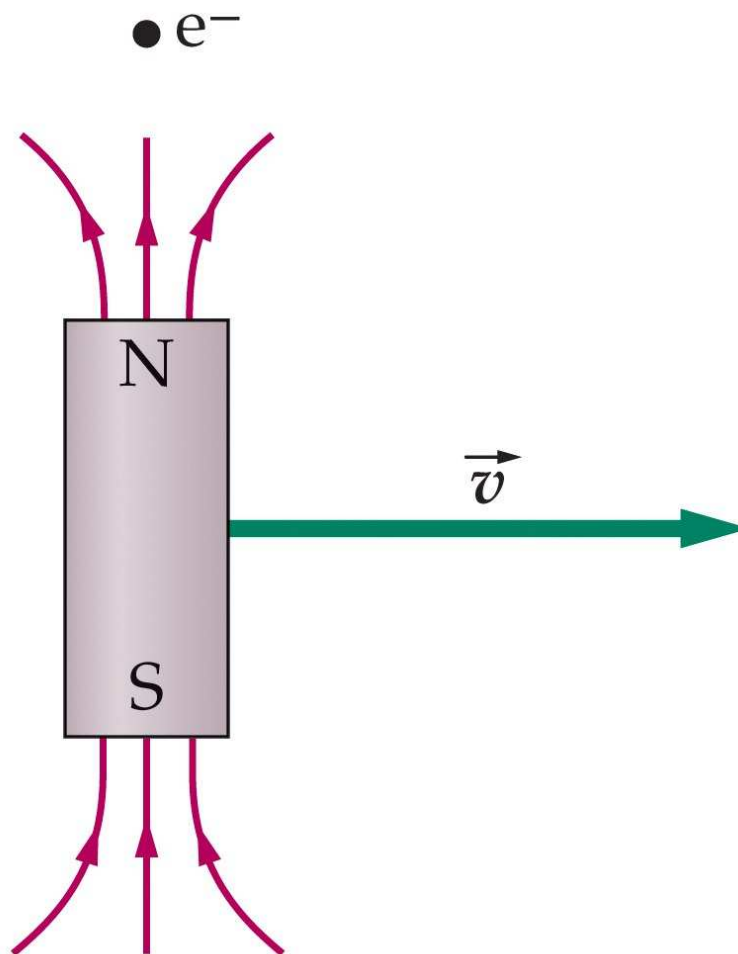
# Problems

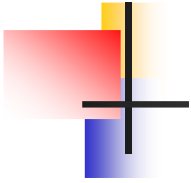
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26.1

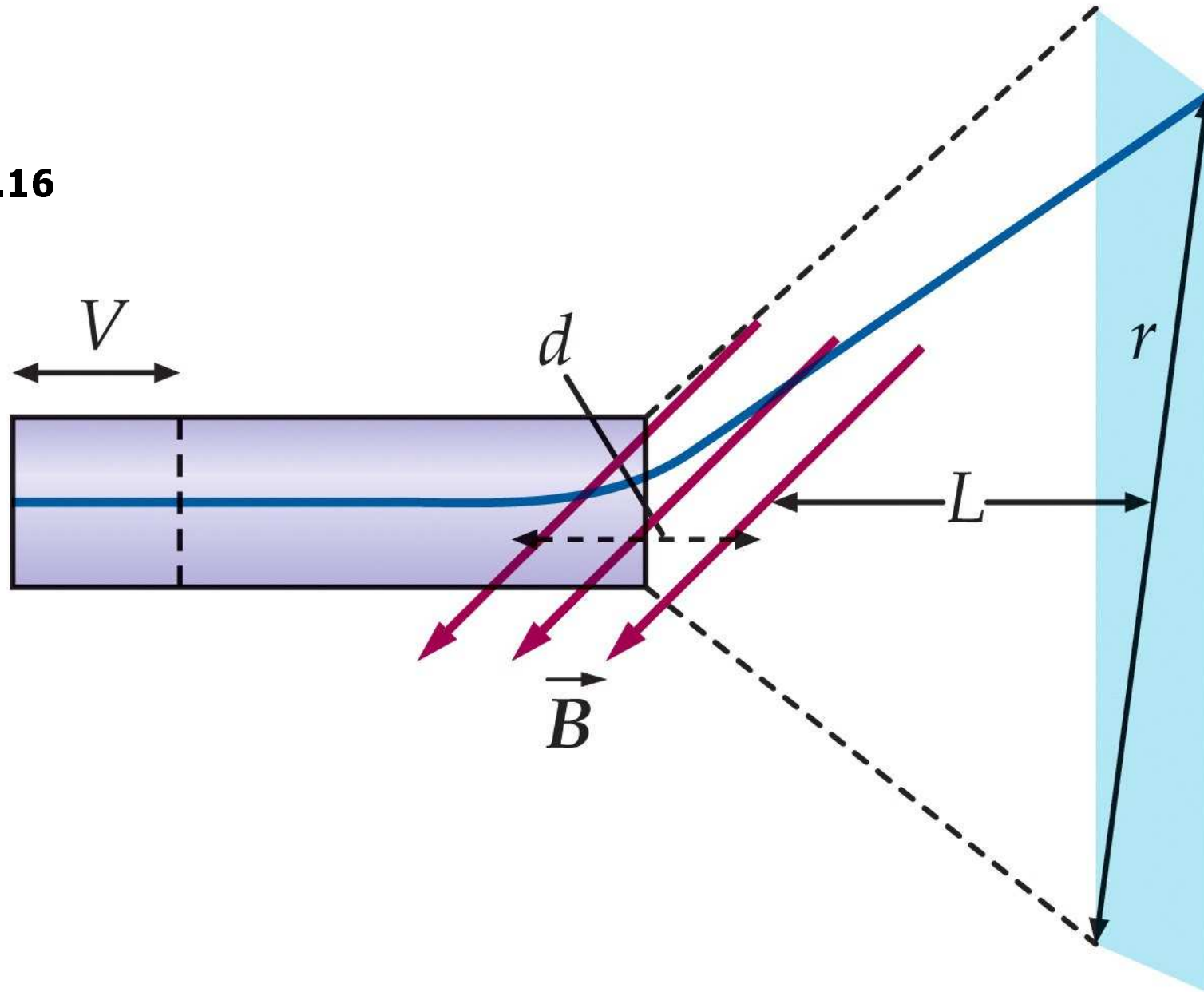


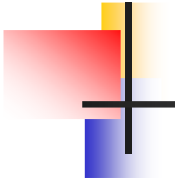
26.13



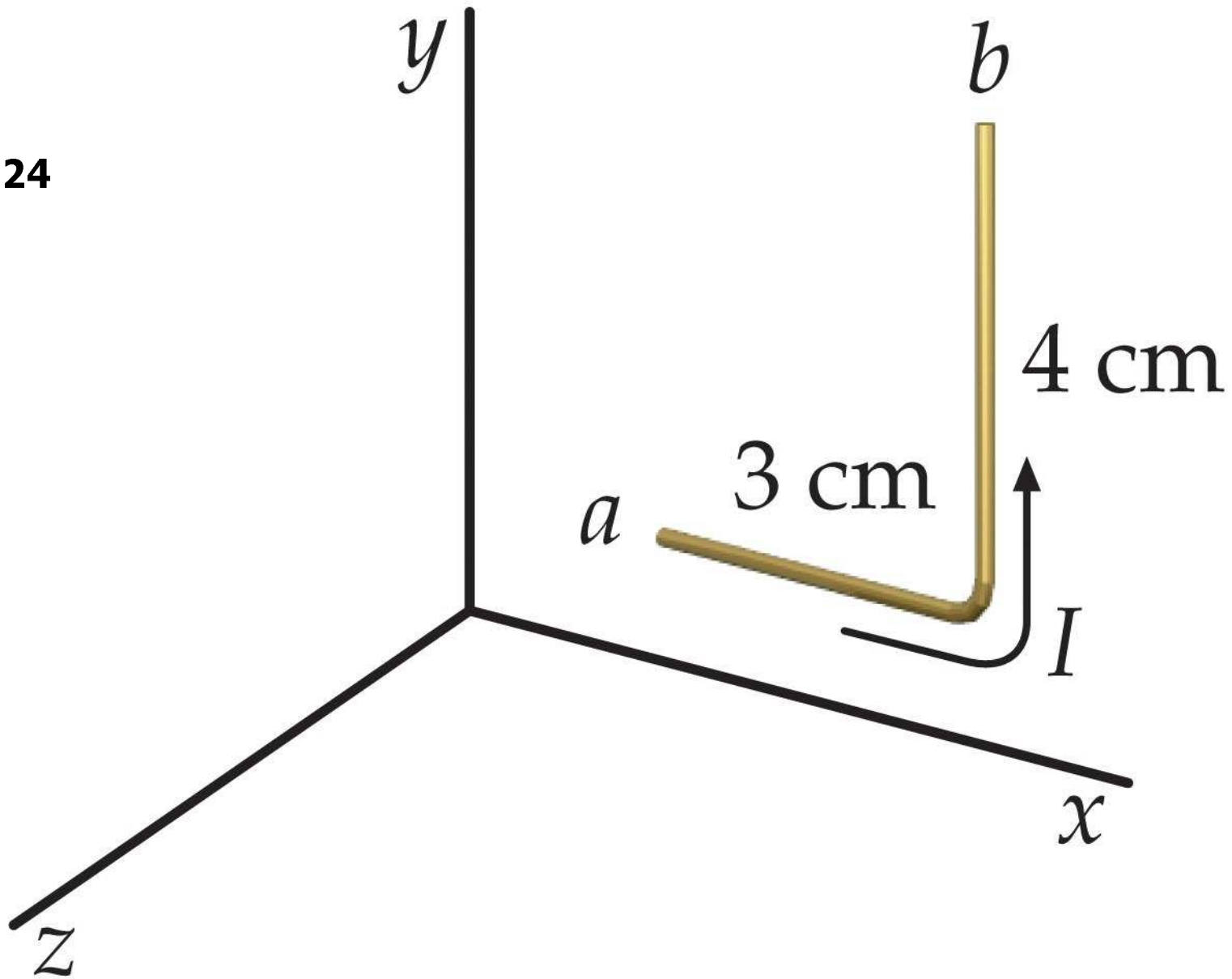


26.16

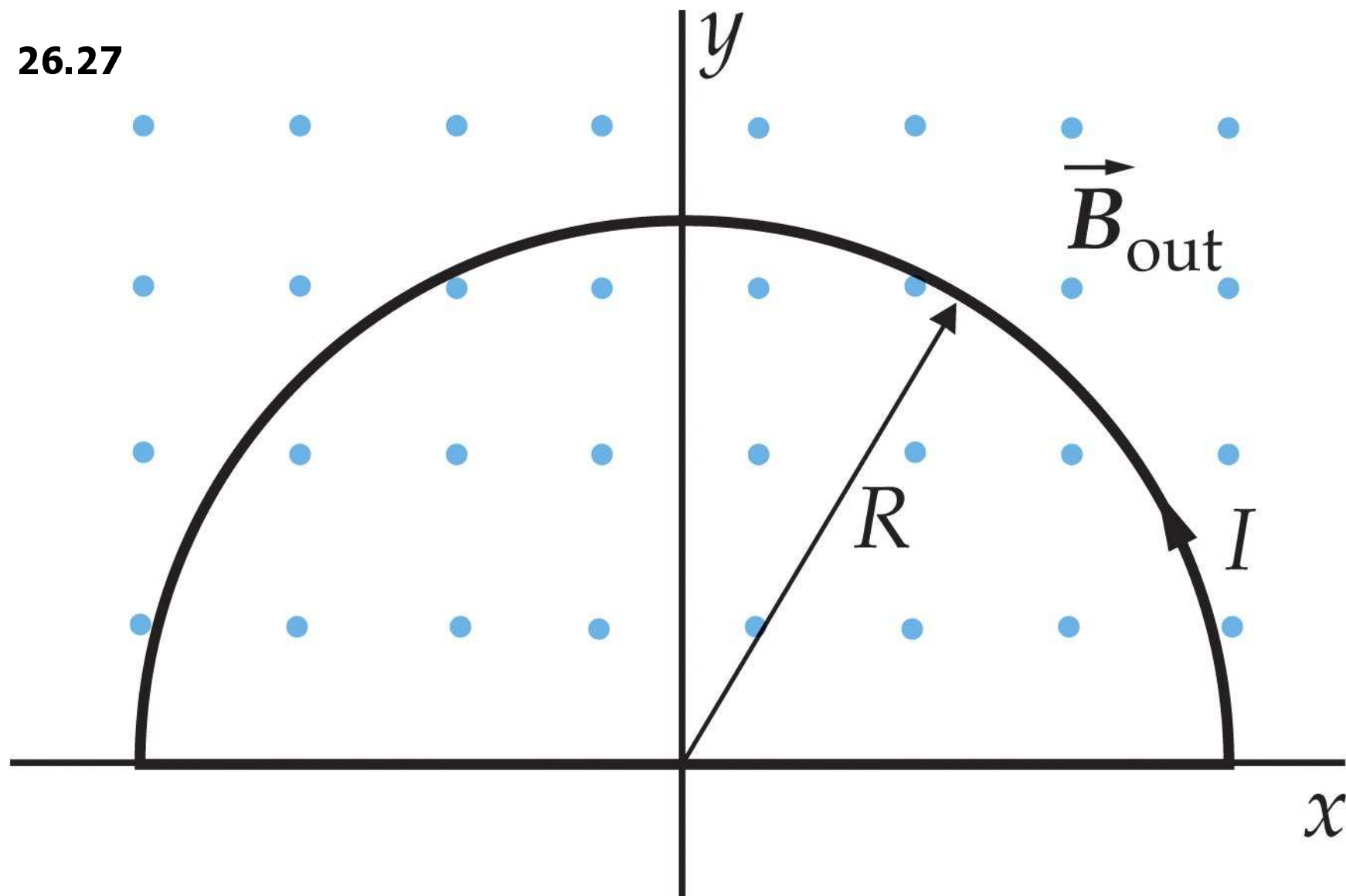




26.24



26.27

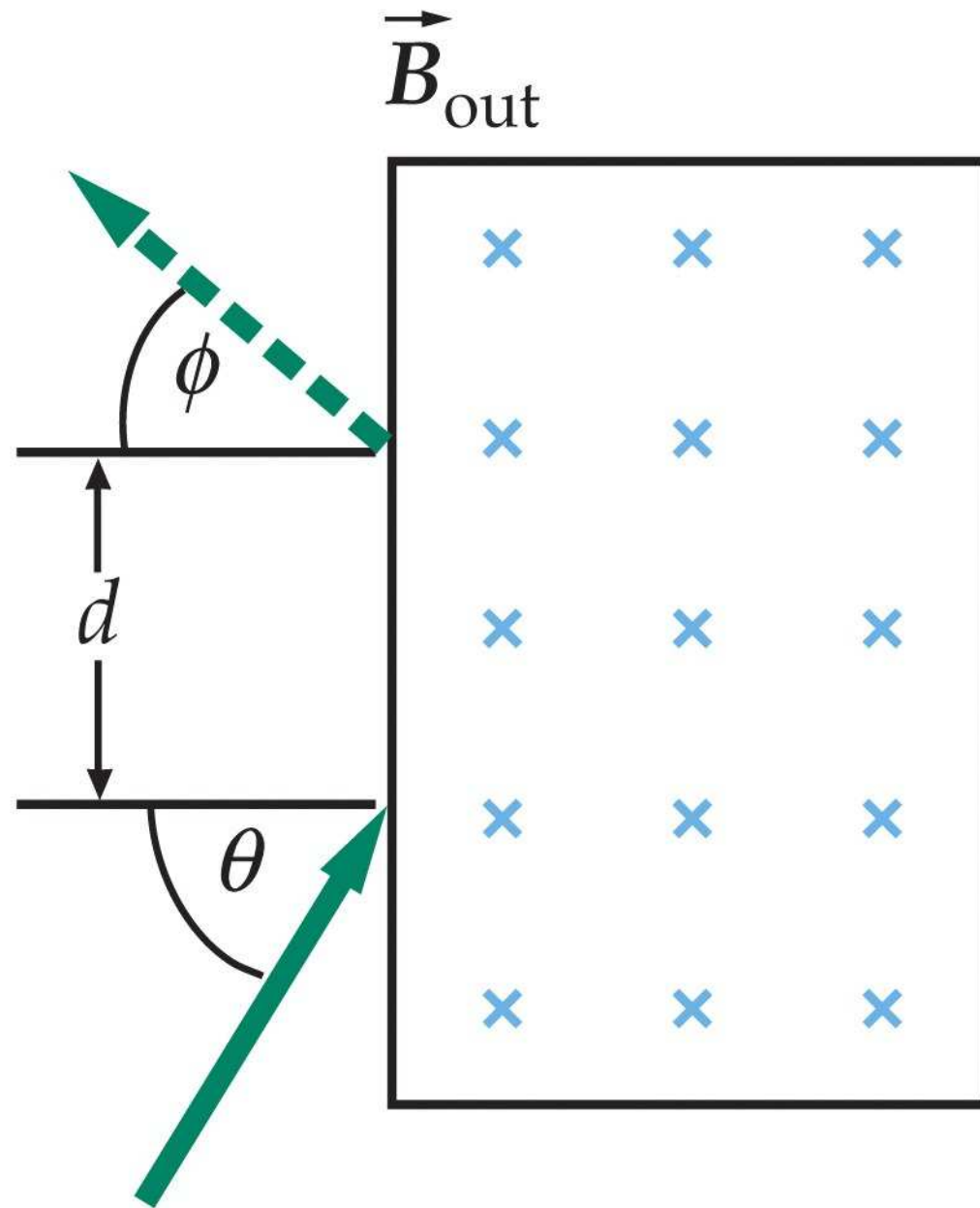






26.38

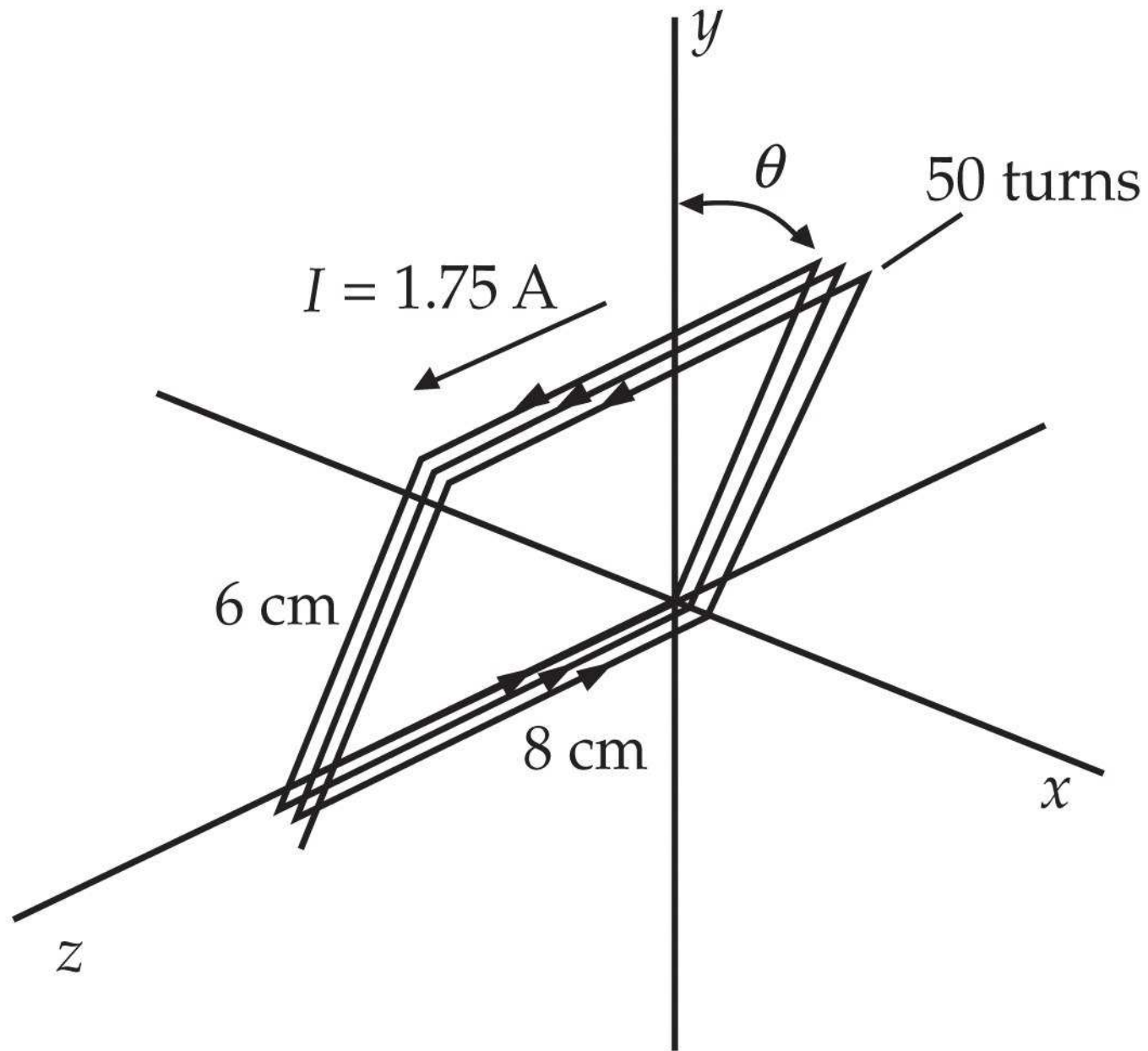
26.39





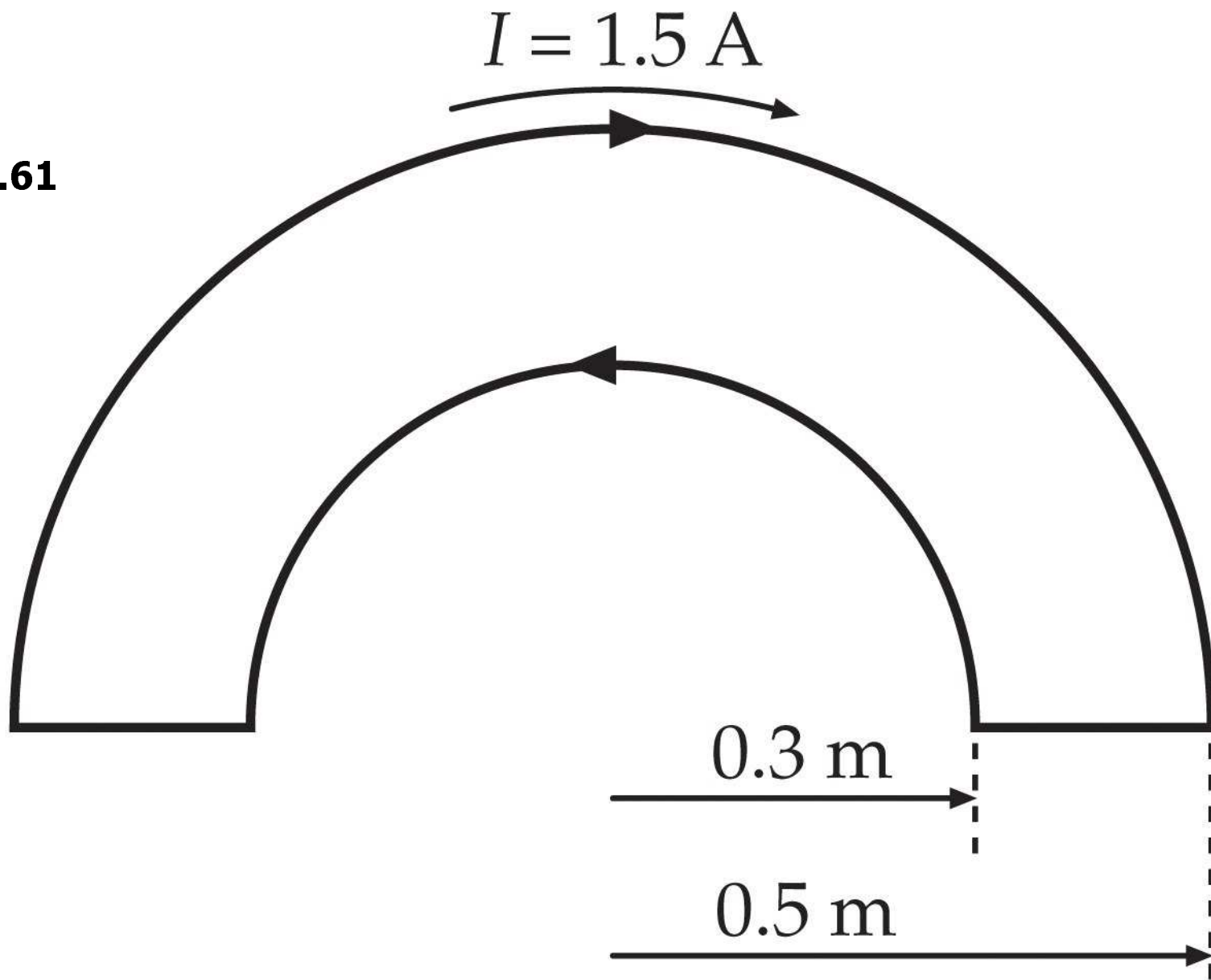
**26.58**

**26.59**

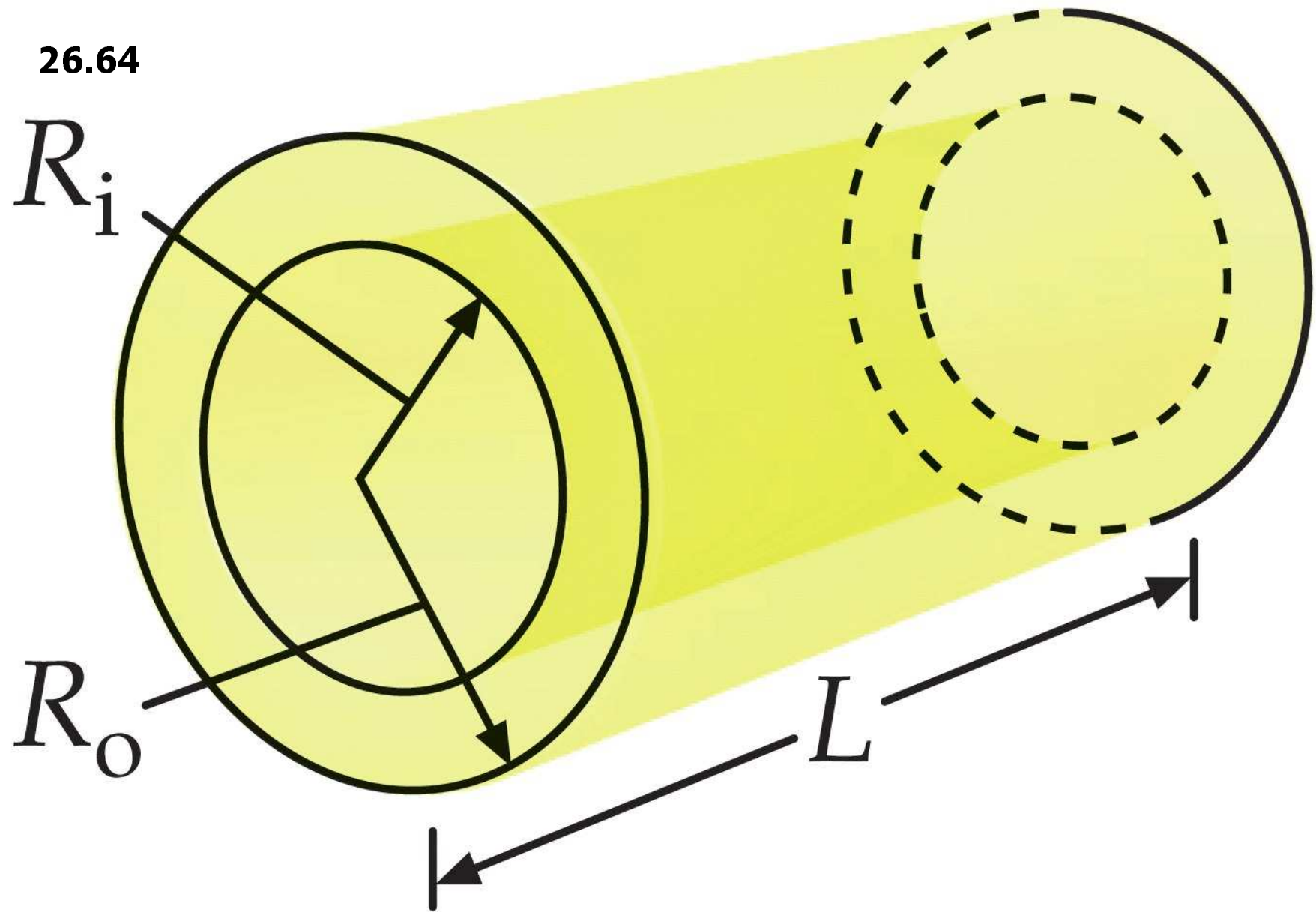




26.61

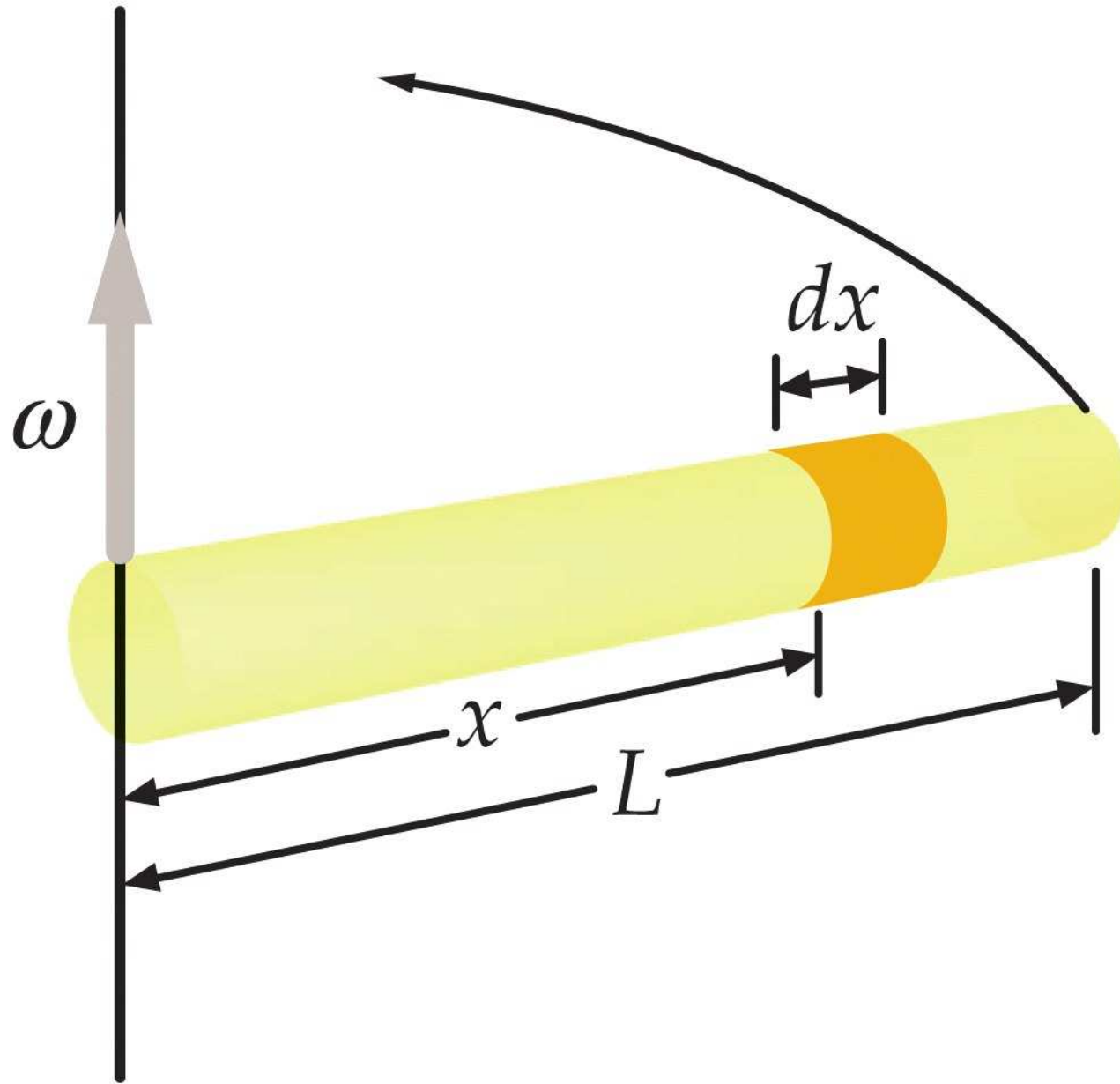


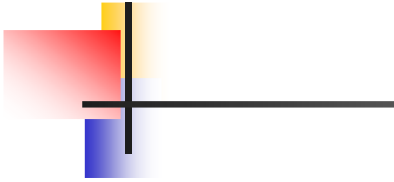
26.64



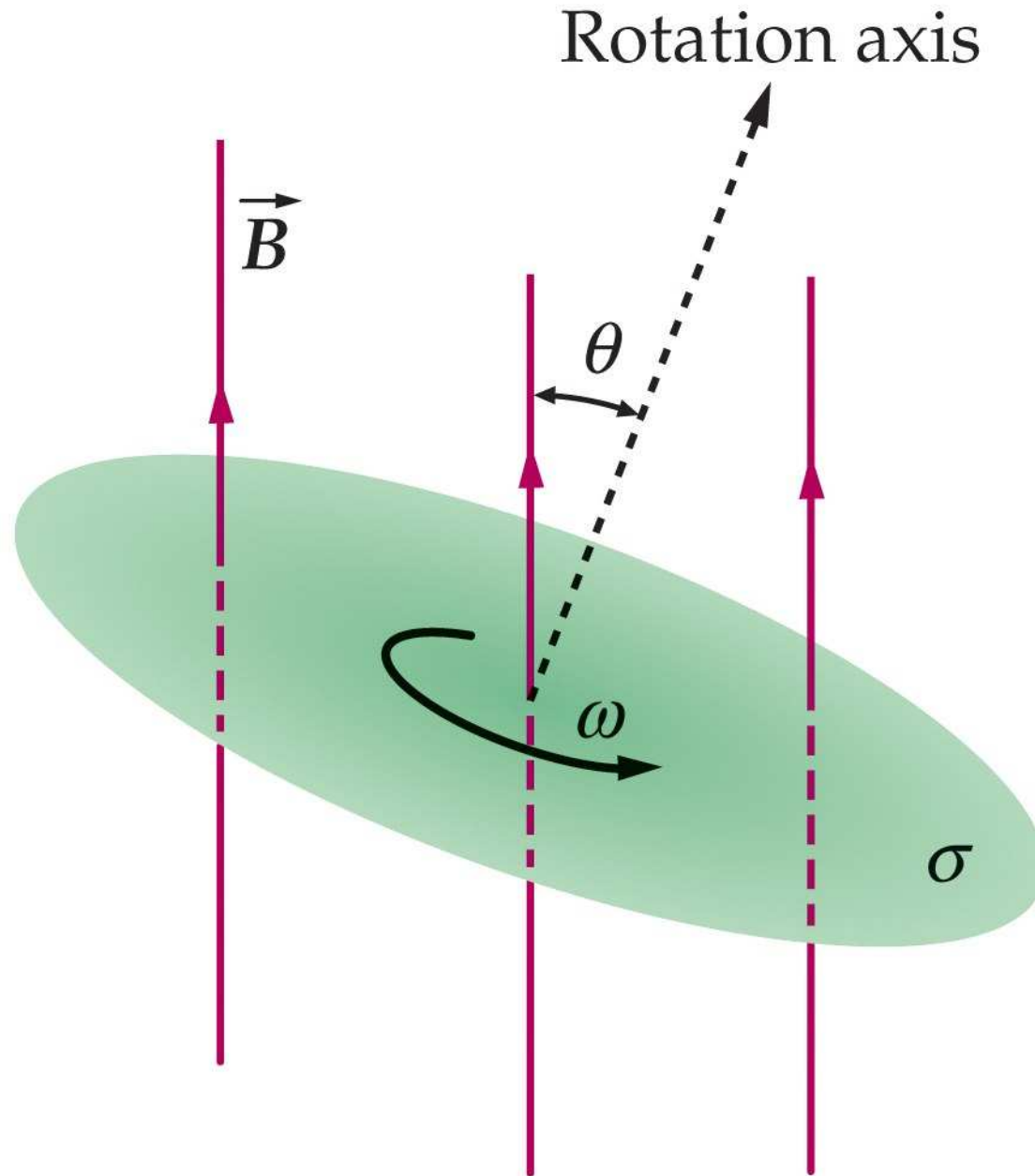


26.65



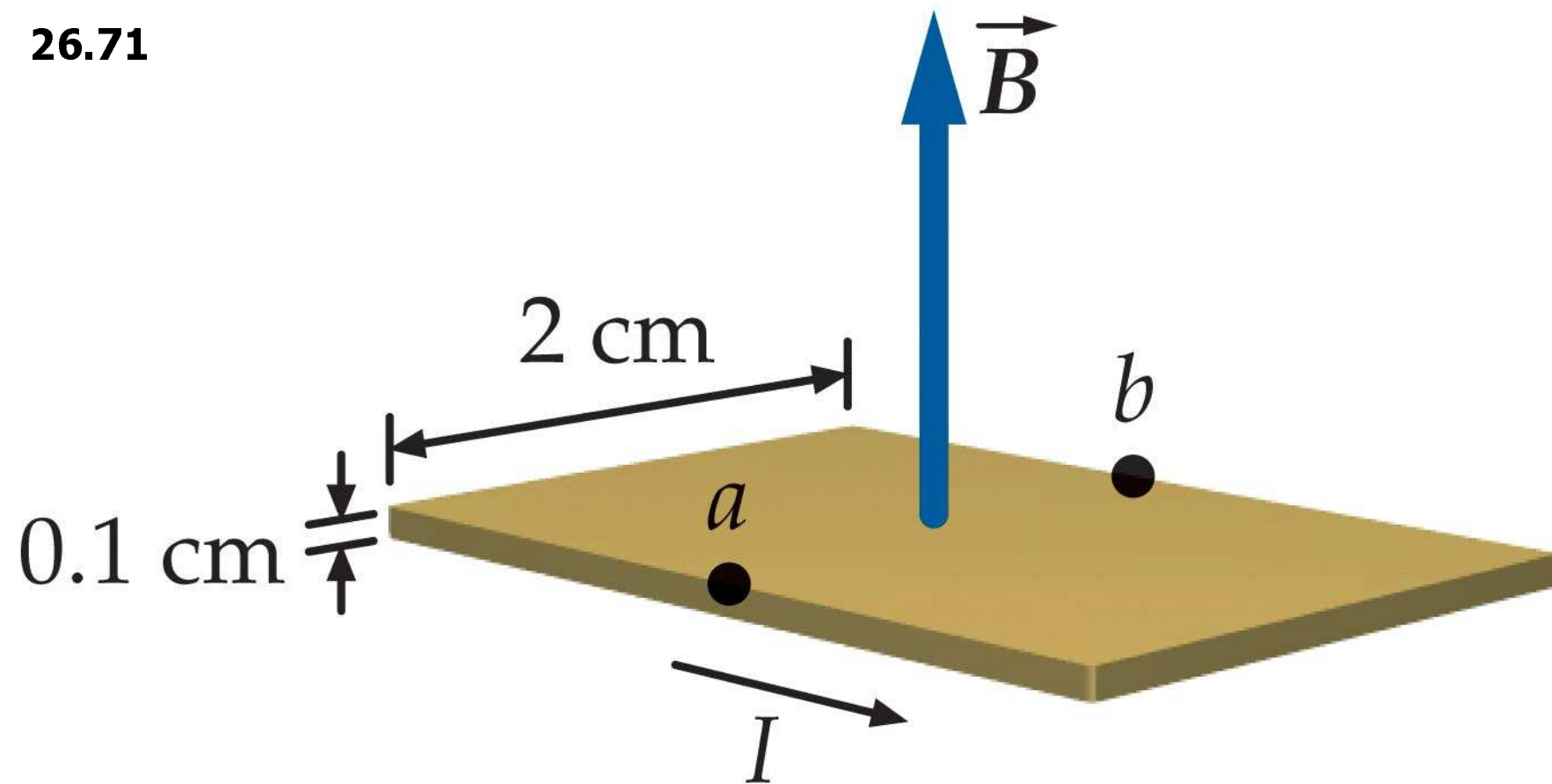


26.69

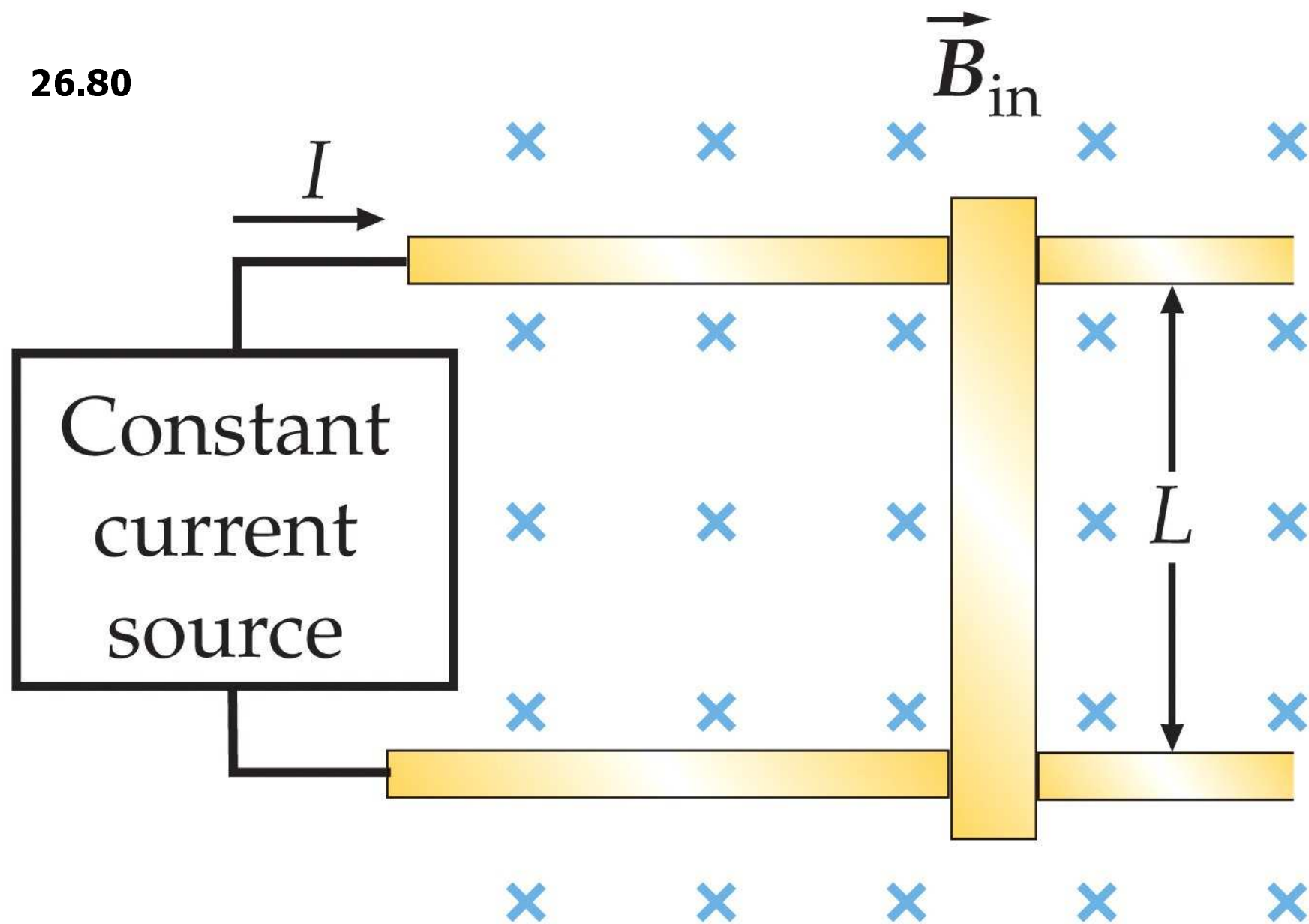


26.70

26.71



26.80







26.84

