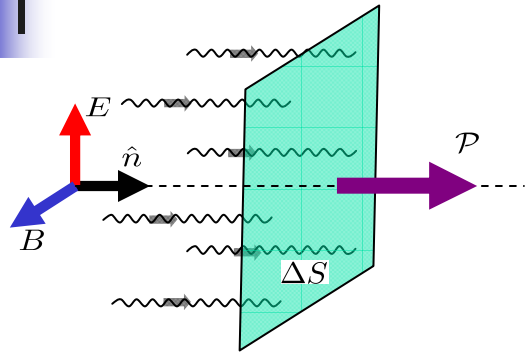


# Propietats de la llum

---

# Dualitat ona partícula



$$\mathcal{I}_m = \frac{1}{2} \epsilon_0 c E_{\max}^2 = uc$$

$$\frac{\vec{p}}{\Delta V} = \frac{u}{c} \hat{n}$$

## Constant de Planck

$$h = 6.626 \times 10^{-34} \text{ Js}$$

$$= 4.136 \times 10^{-15} \text{ eVs}$$

$$\hbar = \frac{h}{2\pi}$$

$$hc = 1240 \text{ eVnm}$$

## fotons

Partícules discretes d'energia

Moment lineal (De Broglie)

Relacio de dispersió

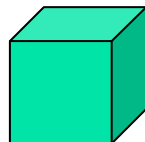
$$E = h\nu = \hbar\omega$$

$$p = \frac{h}{\lambda}$$

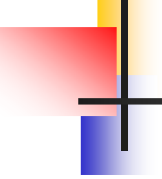
$$E = pc$$

$$\nu = \frac{c}{\lambda}$$

Nombre de fotons a  $\Delta V$



$$\mathcal{N} = \frac{U}{\hbar\omega} = \frac{u}{\hbar\omega} \Delta V$$



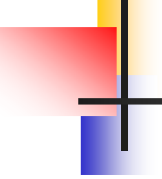
## Einstein:

La intensitat (flux d'energia) i el moment de l'ona EM són el resultat de la transmissió de fotons individuals

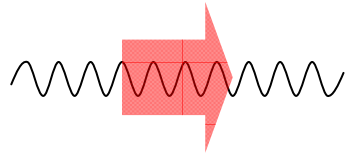
frequència  $f \equiv \nu$


$$E = hf = \frac{hc}{\lambda} \quad 31-1$$

EINSTEIN'S EQUATION FOR PHOTON ENERGY



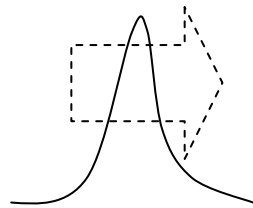
## Ona harmònica monocromàtica



Fotons d'una sola classe

$$E, p, \nu, \lambda, \omega, k$$

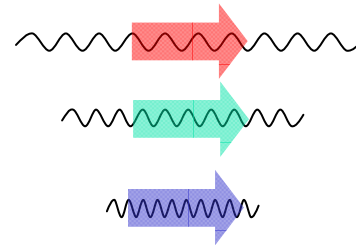
## Pols de radiació



“Paquet d’ones”

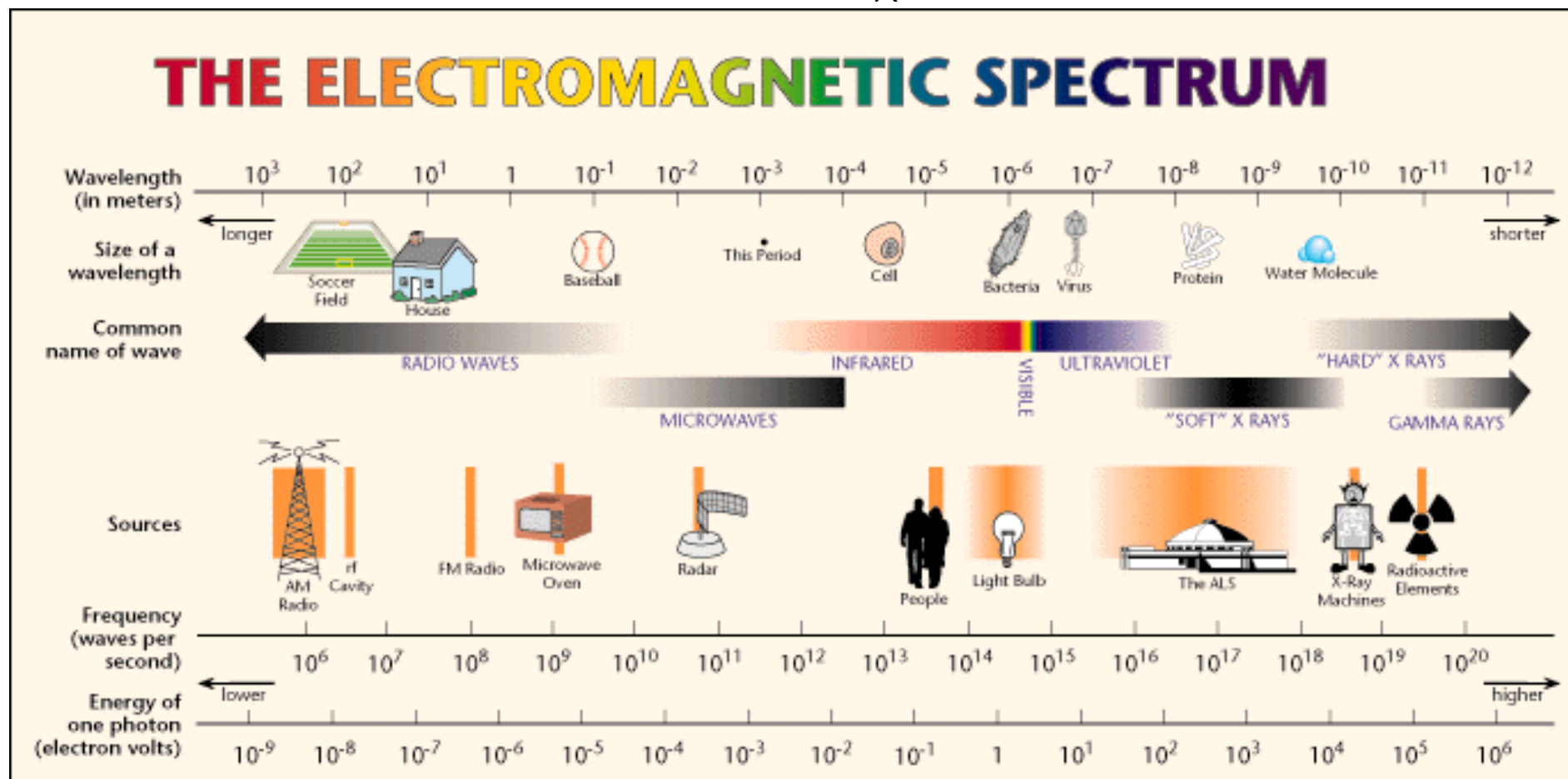
Fotons de diverses classes

Distribució d’energies, moments, freqüències ...



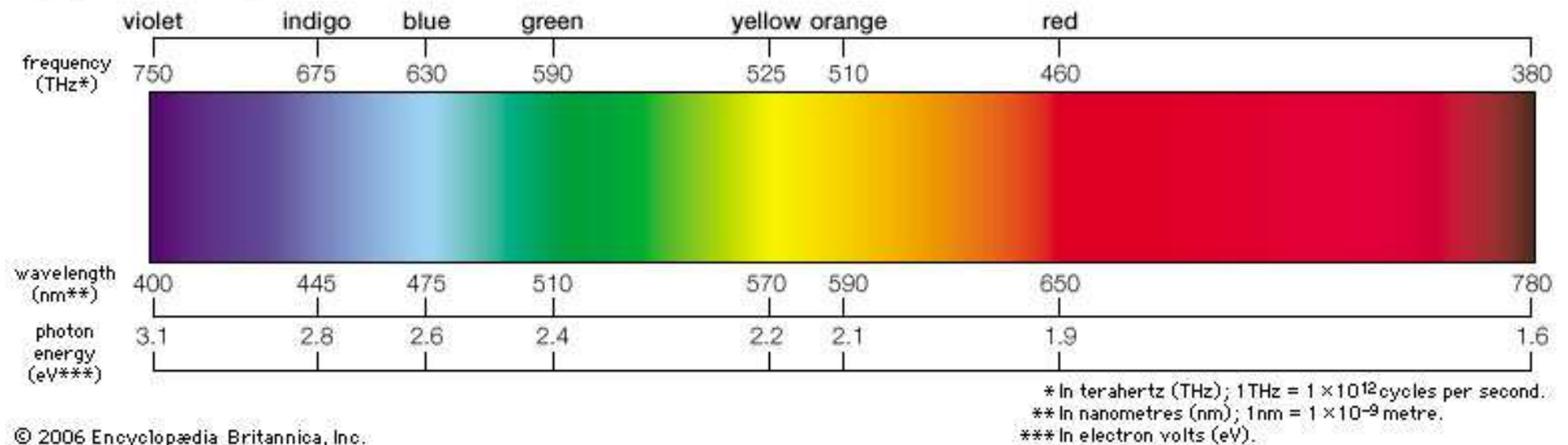
## Els fotons de l'espectre EM

$$E = h\nu = h\frac{c}{\lambda}$$

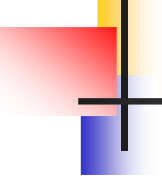




## Light, the visible spectrum

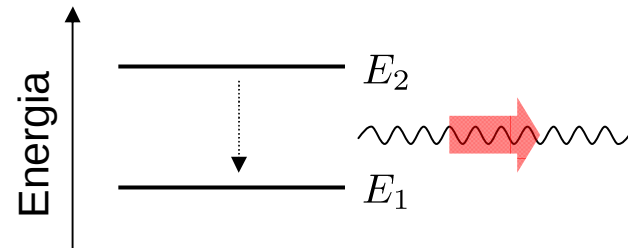


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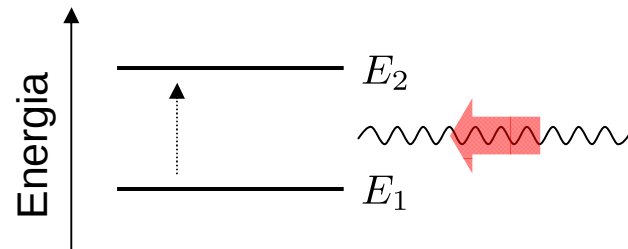
**Espectres** (imatge de Bohr):  
transicions entre estats discrets  
radiació EM emesa o absorbida

**emissió**



$$h\nu_{21} = E_2 - E_1$$

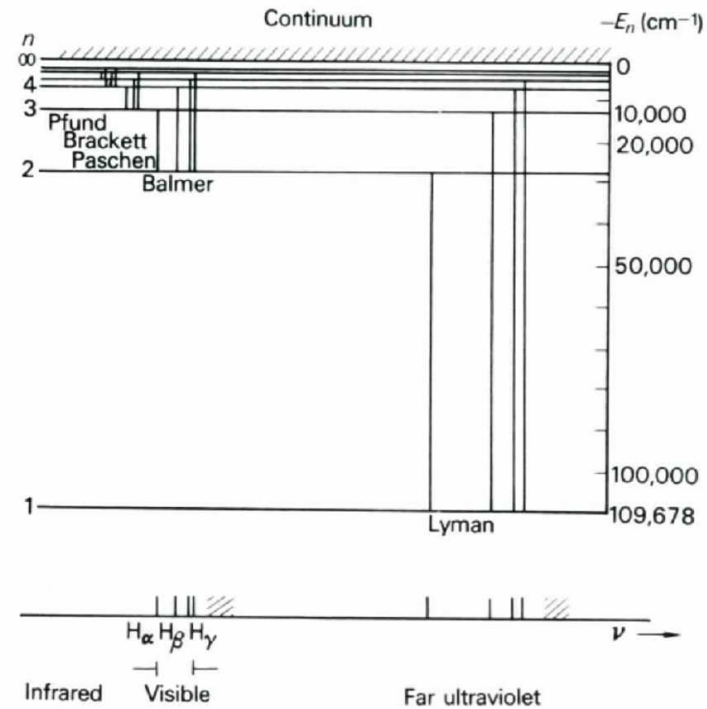
**absorció**



$$\lambda_{21} = \frac{c}{\nu_{21}}$$

# L'espectre de l'hydrogène

## 2.6. The hydrogen energy spectrum

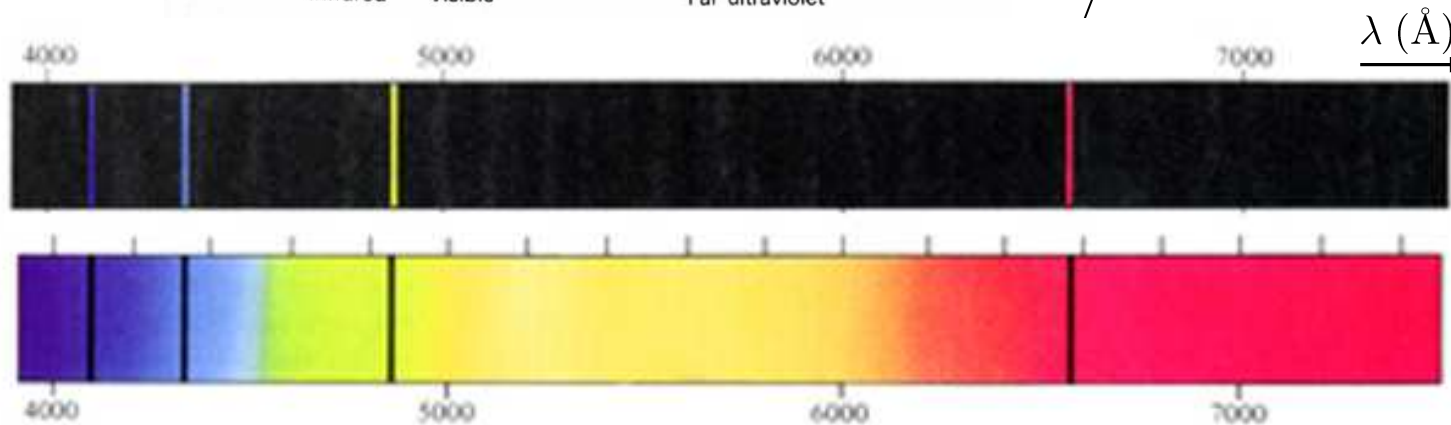


$$E_n = -\frac{13.6}{n^2} \text{ eV}$$

**H $\alpha$**

$$\Delta E = \left( \frac{1}{4} - \frac{1}{9} \right) 13.6 \text{ eV} = 1.88 \text{ eV}$$

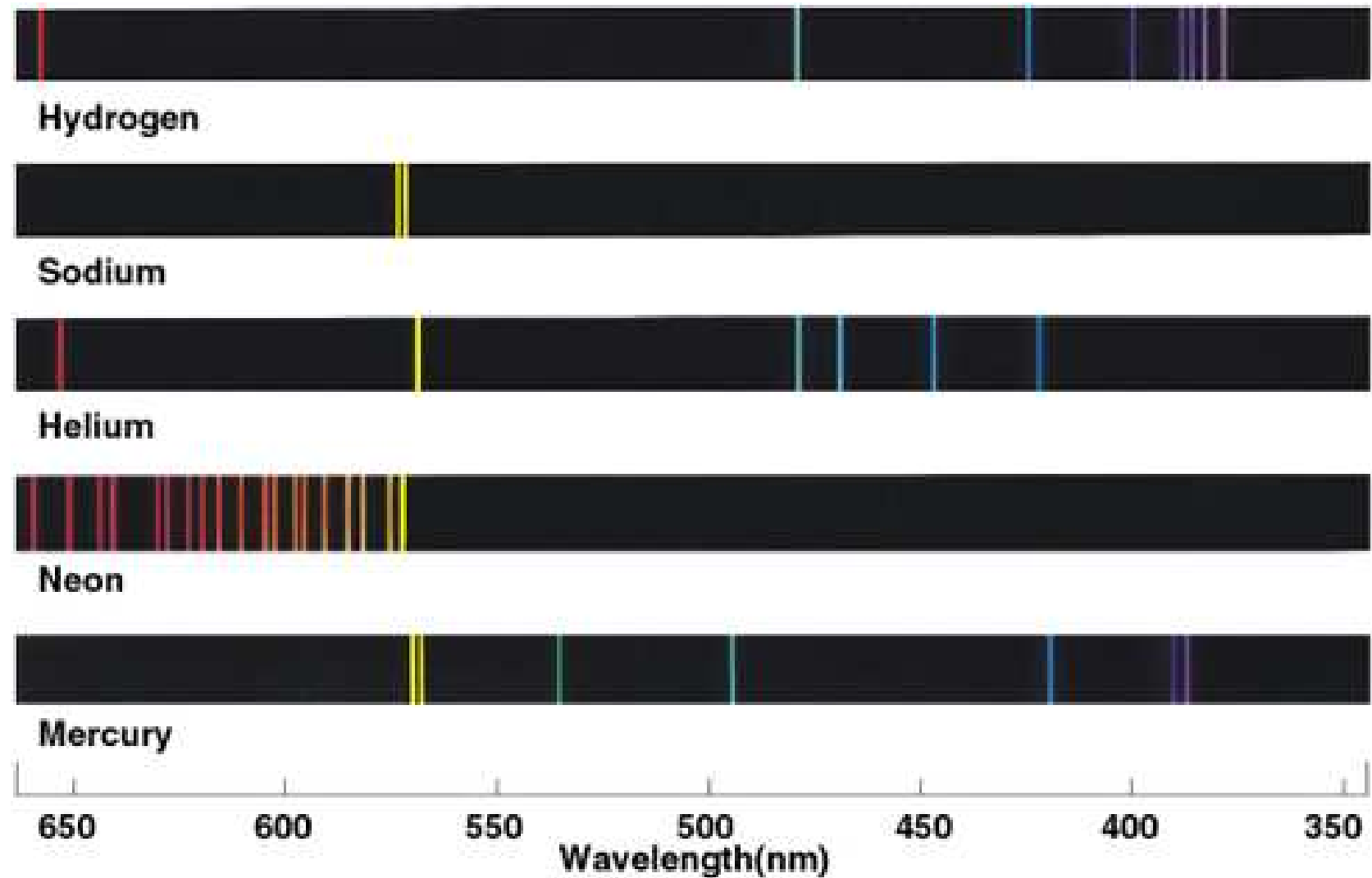
$$\lambda = \frac{hc}{\Delta E} = \frac{1240 \text{ eV nm}}{1.88 \text{ eV}} = 659.6 \text{ nm}$$



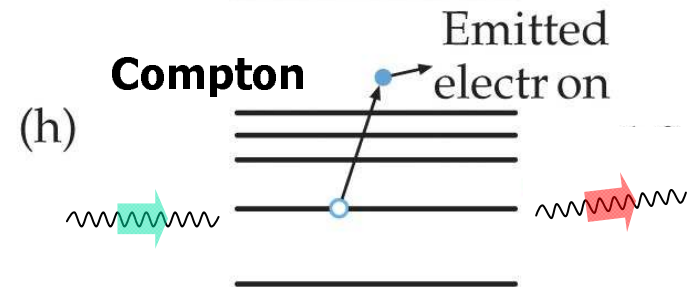
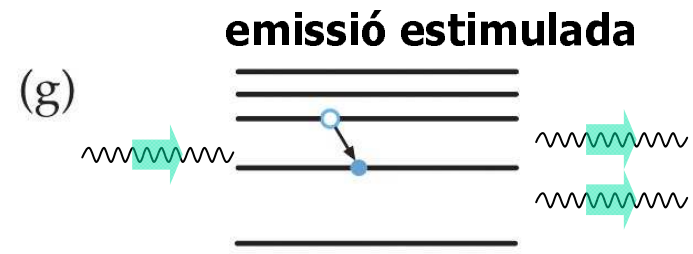
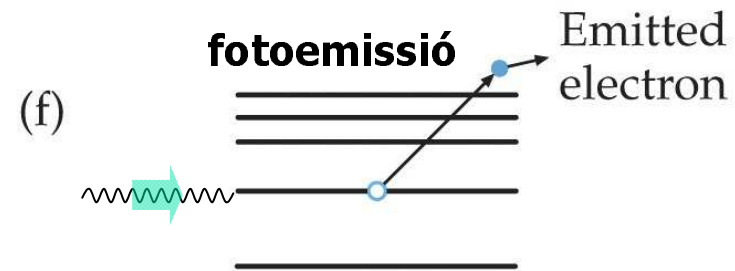
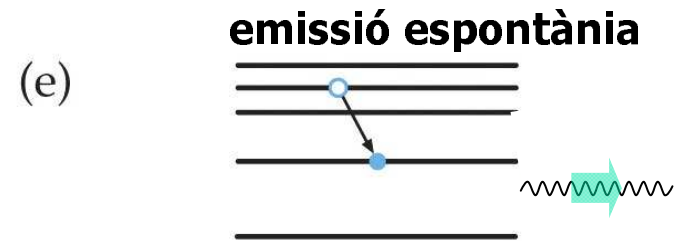
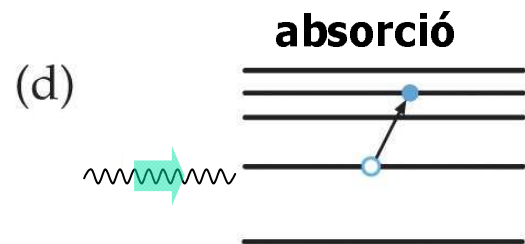
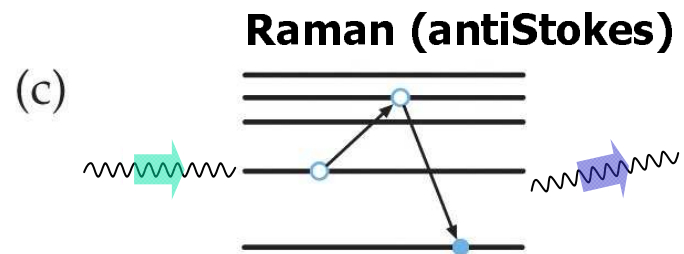
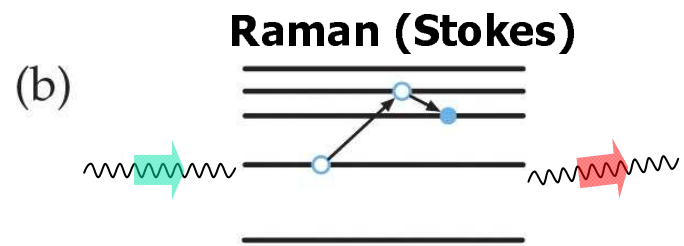
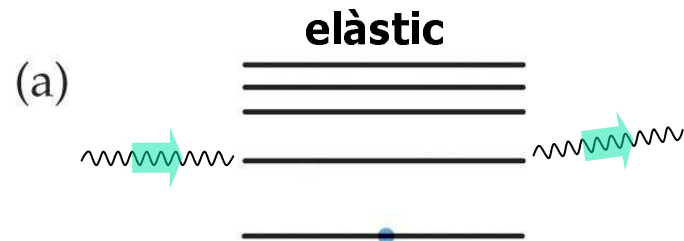
The Hydrogen Spectrum  
Above: Emission  
Below: Absorption



## Altres àtoms

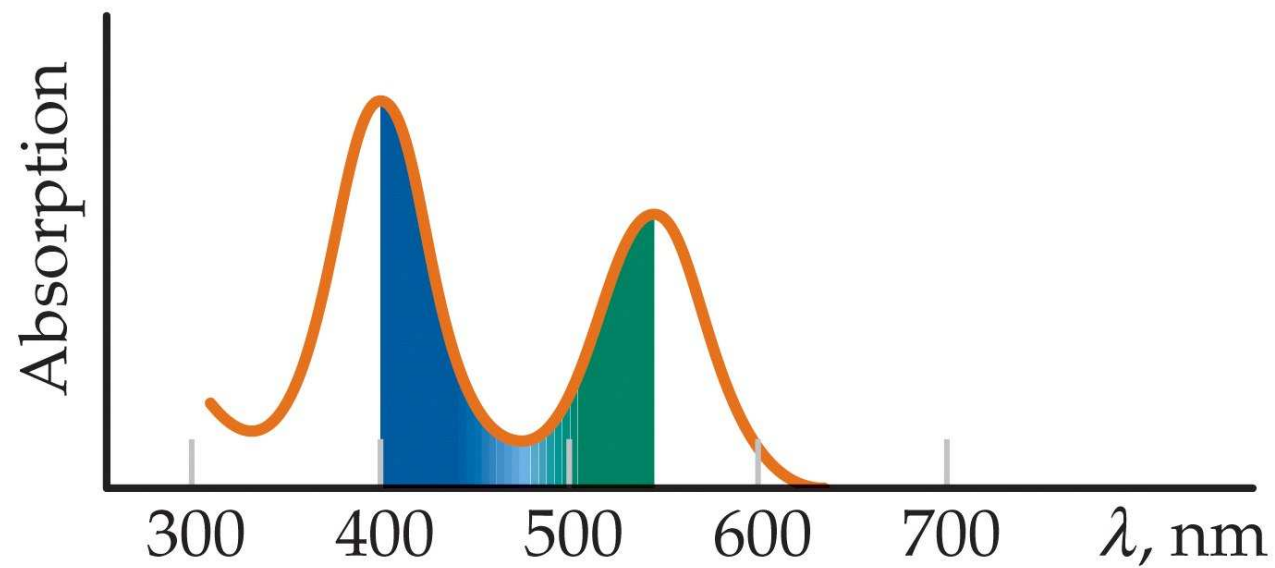
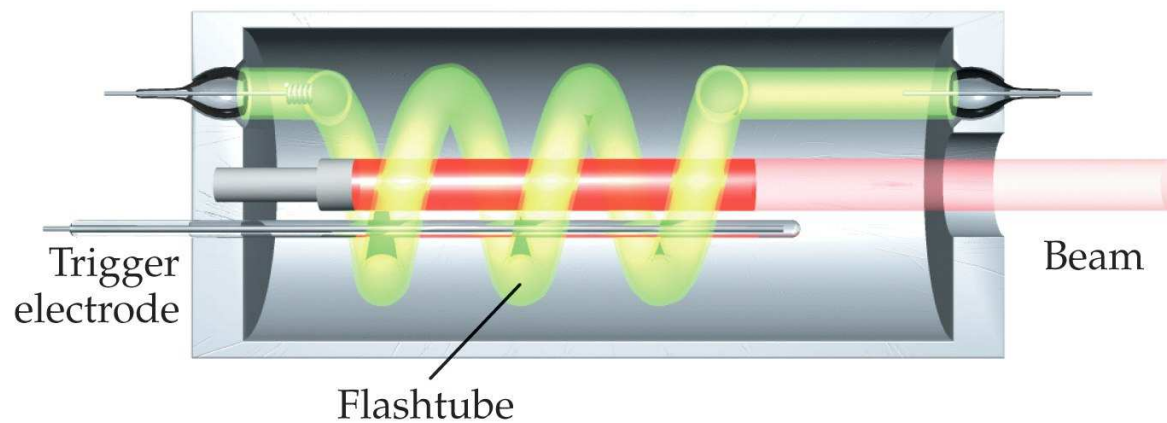
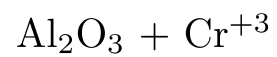


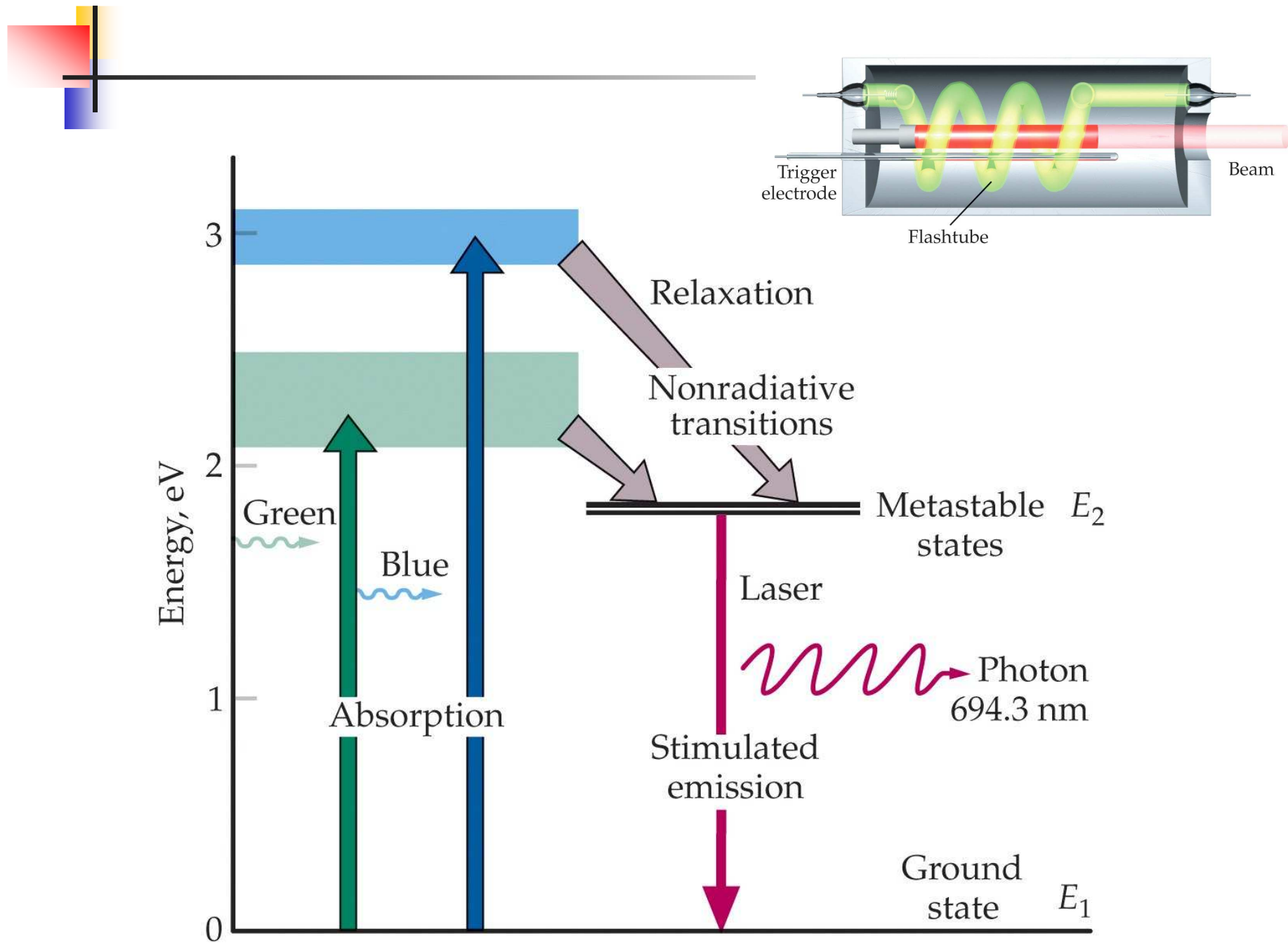
## Processos amb fotons

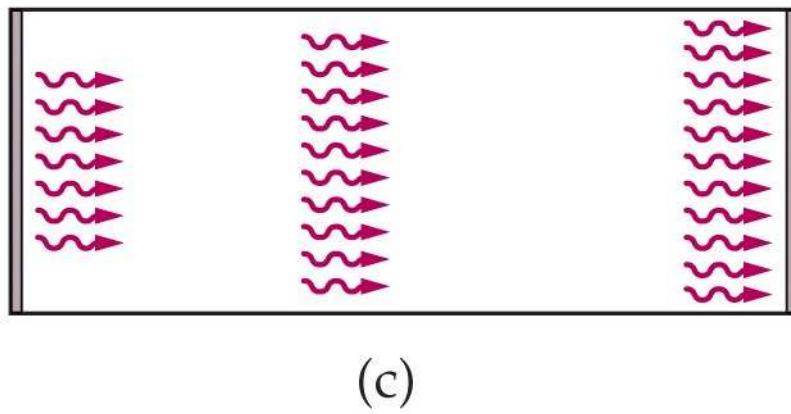
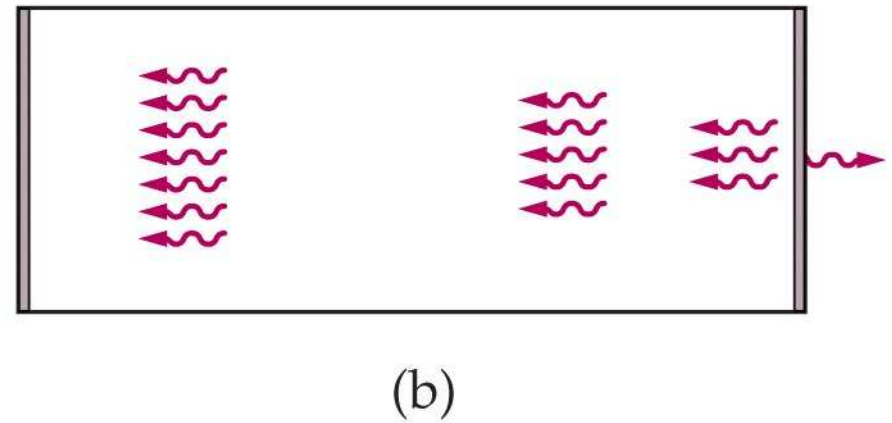
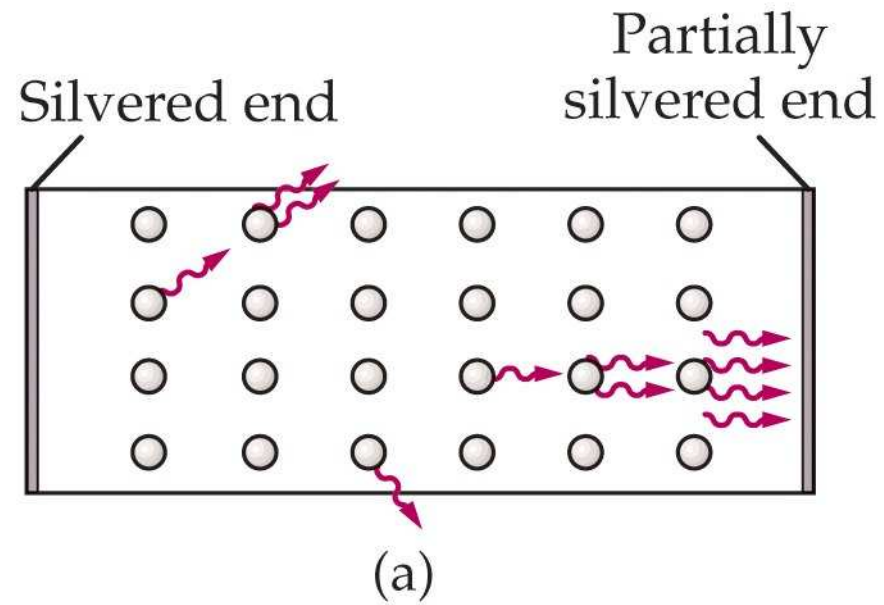
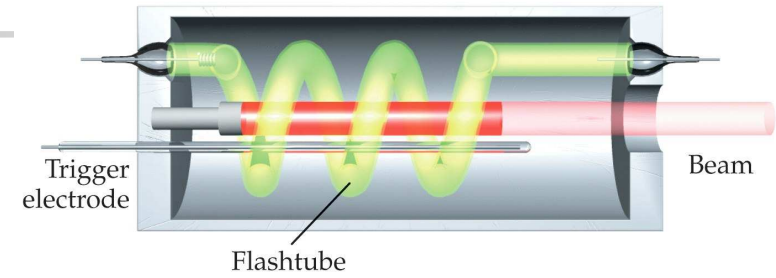


# Lasers

## Rubí



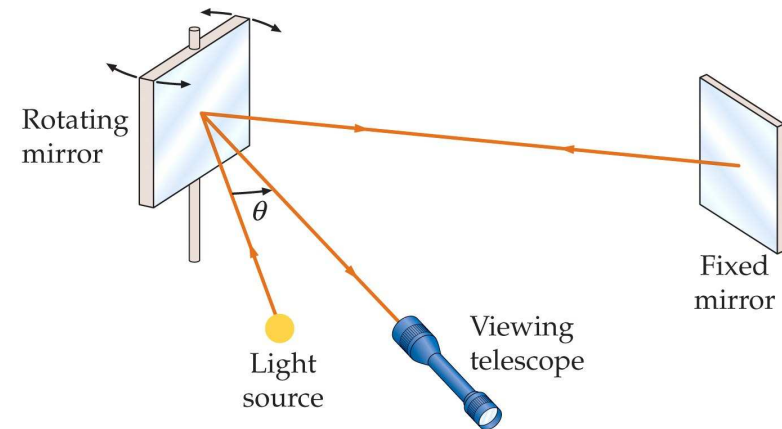
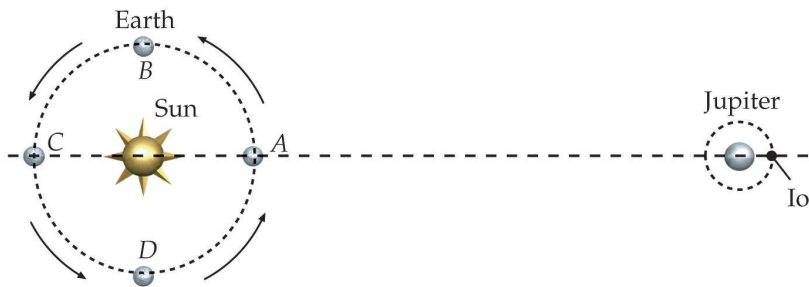


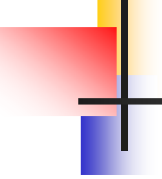


## La velocitat de la llum

$$c = 299,792,458 \text{ m/s} \approx 3 \times 10^8 \text{ m/s} \quad 31-5$$

### DEFINITION—SPEED OF LIGHT





## Índex de refracció

A un medi material  $v < c$

*Índex de refracció* del medi

$$n = \frac{c}{v} \quad n > 1$$

### Constants relatives

$$\epsilon = \epsilon_r \epsilon_0$$

$$\mu = \mu_r \mu_0$$

$$v = \frac{1}{\sqrt{\epsilon\mu}} = \frac{c}{\sqrt{\epsilon_r\mu_r}}$$

Estàtica

$$\epsilon_r = \kappa$$

Constant dielèctrica

# Propagació de la llum: Òptica

## Òptica geomètrica

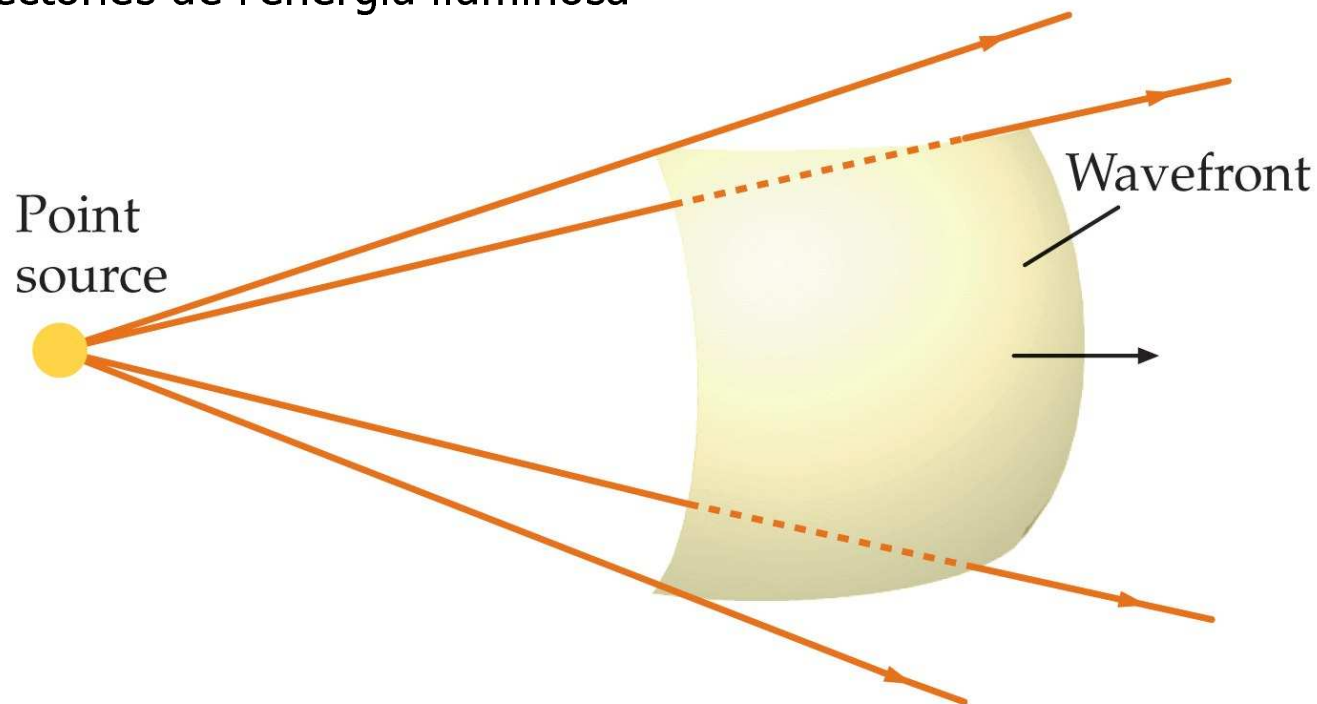
Llum visible

Les dimensions d'interès són molt més grans que la longitud d'ona de l'ona EM

$$\lambda \approx 500 \text{ nm} = 5 \times 10^{-7} \text{ m}$$

## El raig lluminós i el front d'ona

Trajectòries de l'energia lluminosa

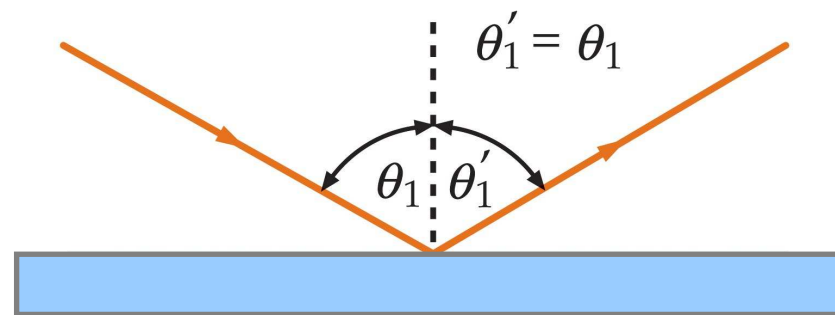


## Lleis de l'òptica geomètrica

- Dins un medi homogeni i isòtrop un raig de llum es propaga seguint una trajectòria recta

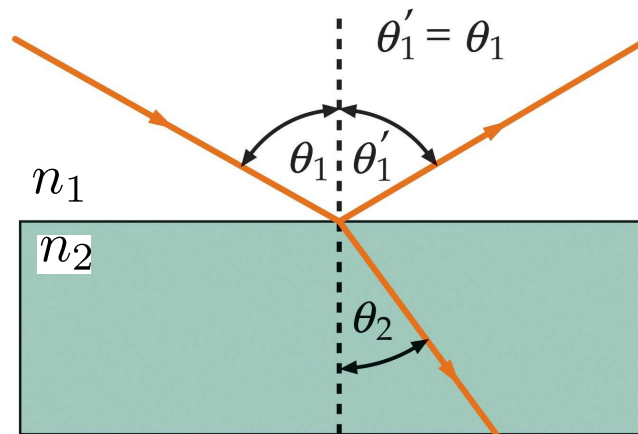
### reflexió

- Un raig "rebota" d'un mirall de manera que l'angle amb la normal del raig incident i el reflectit és el mateix



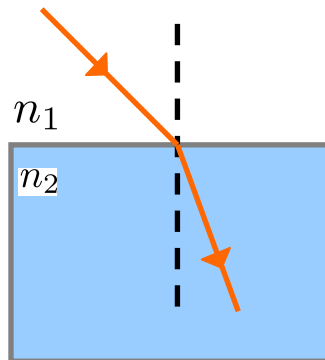
## refracció (Llei de Snell)

- Quan un raig passa d'un medi a un altre, canvia de trajectòria, essent la relació entre angle incident i refractat la donada per la llei de Snell

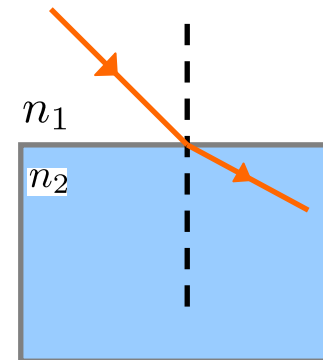


$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

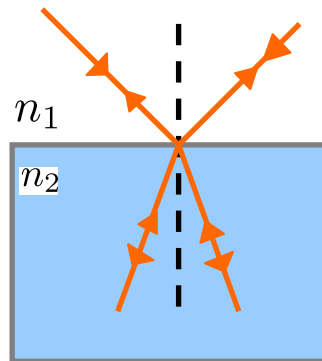
Si  $n_2 > n_1$  ( $v_2 < v_1$ )



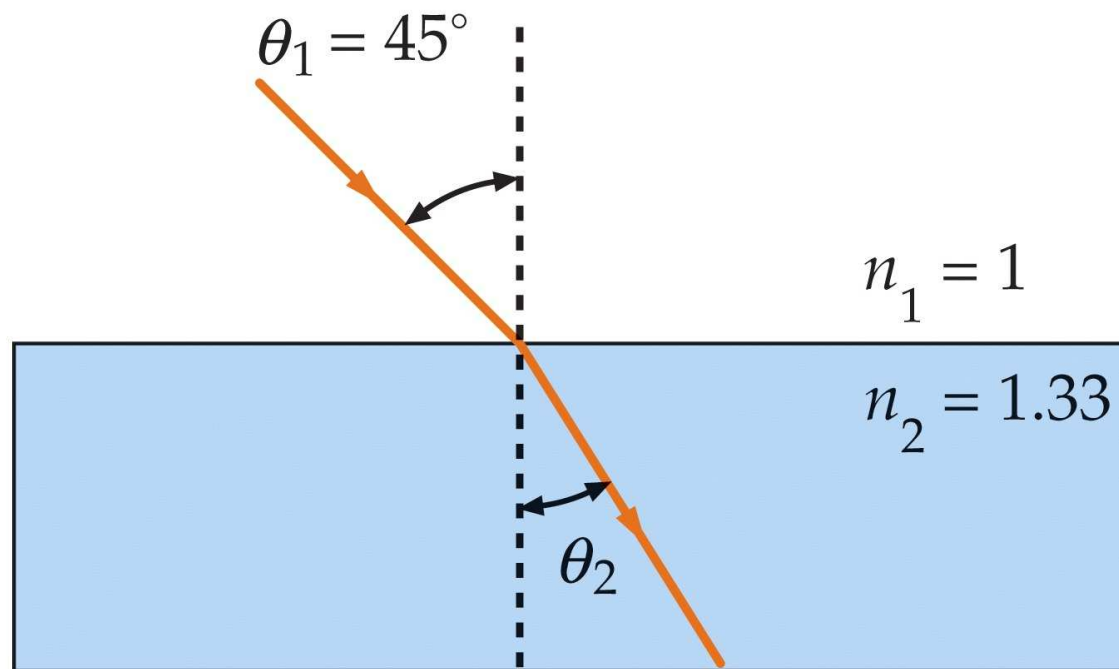
Si  $n_2 < n_1$  ( $v_2 > v_1$ )



- Les trajectòries de la llum per distins medis són reversibles



## Refracció d'aire a aigua



$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$\theta_2 = \arcsin \left( \frac{n_1}{n_2} \sin 45^\circ \right)$$
$$= 32.1^\circ$$

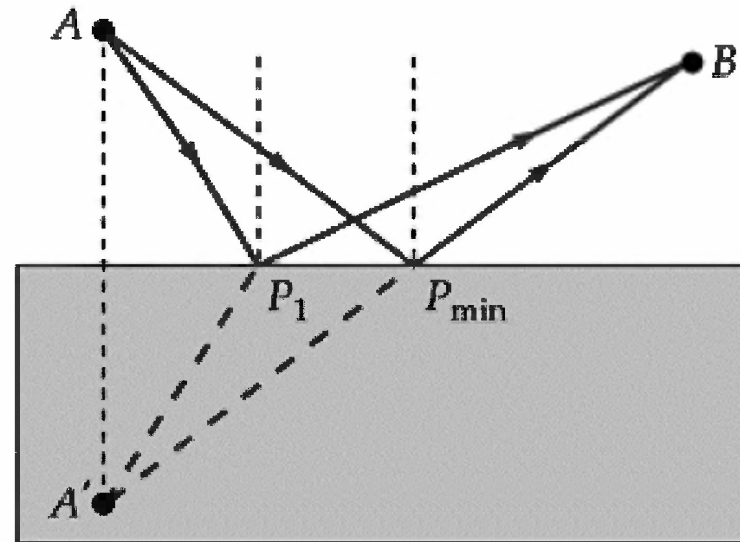
## El principi de Fermat del temps mínim

The path taken by light traveling from one point to another is such that the time of travel is a minimum.<sup>†</sup>

FERMAT'S PRINCIPLE

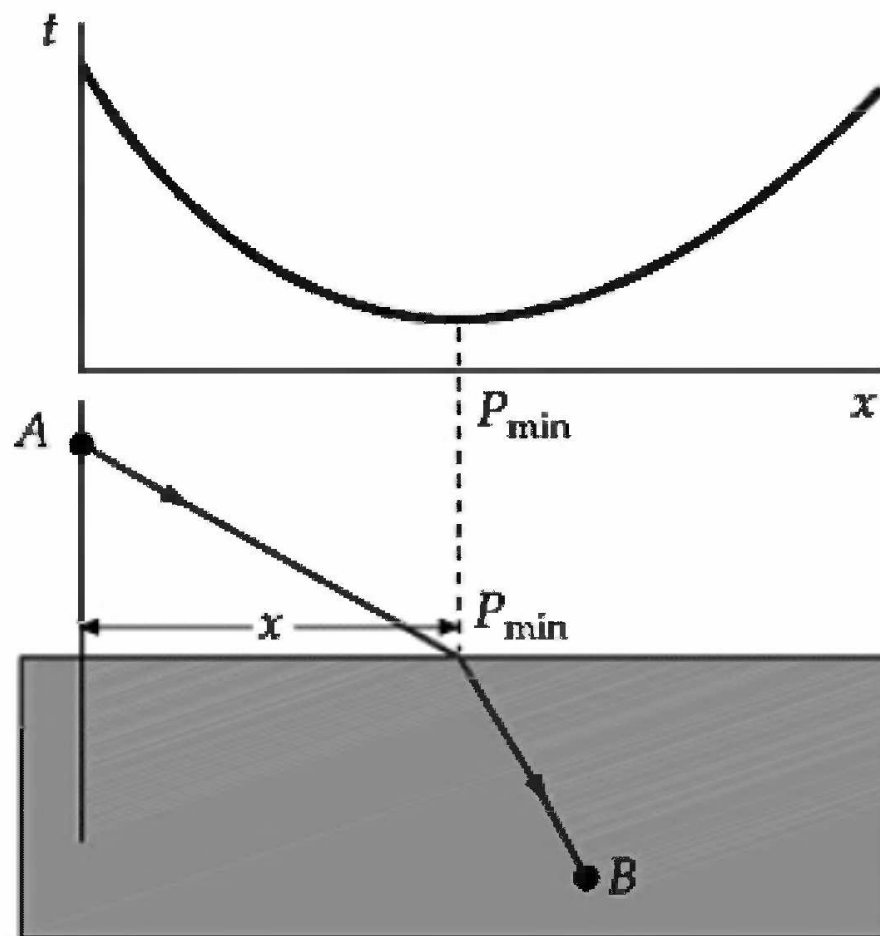
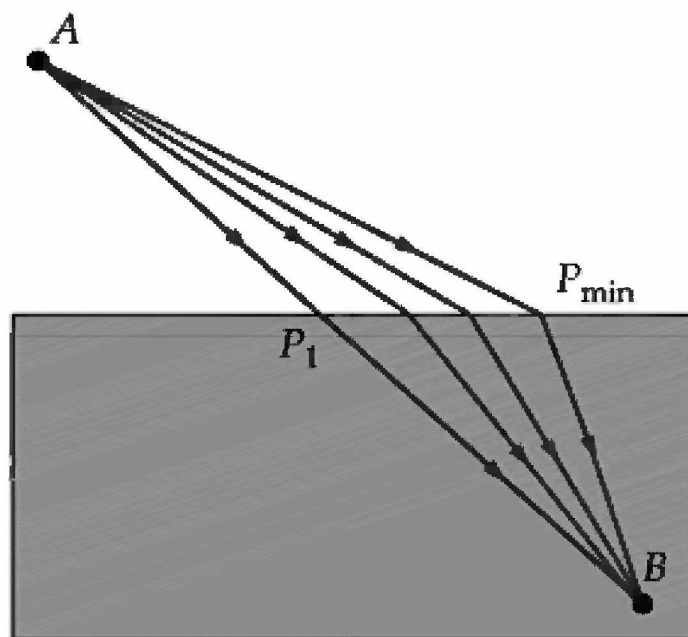
Trajectòries rectes dins un medi homogeni

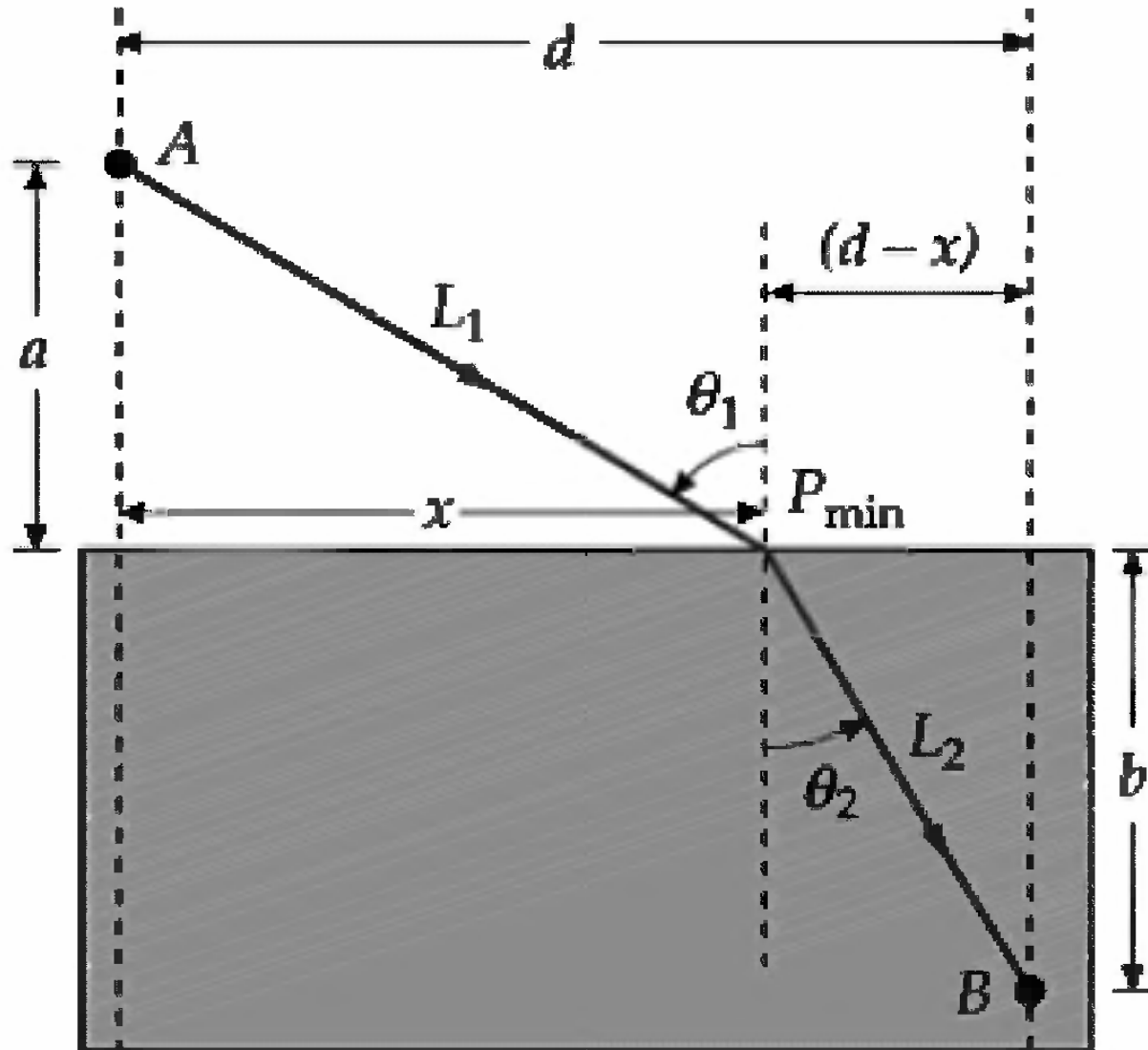
Reflexió



$$APB = A'PB$$

## Refracció





$$t = \frac{n_1 L_1}{c} + \frac{n_2 L_2}{c}$$

$$L_1 = \sqrt{a^2 + x^2}$$

$$L_2 = \sqrt{b^2 + (d-x)^2}$$

$$\frac{dt}{dx} = 0$$

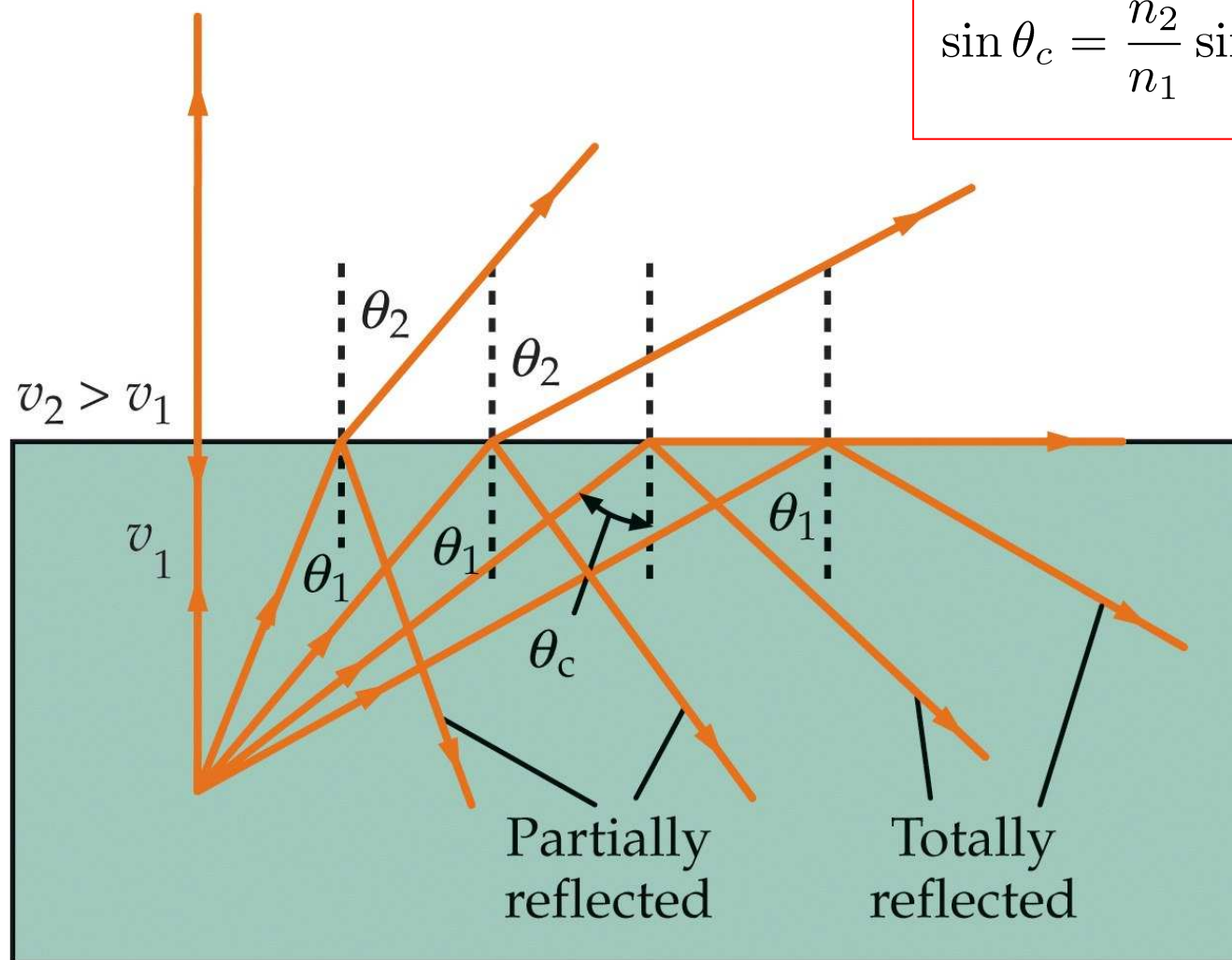
$$n_1 \frac{dL_1}{\underbrace{dx}} + n_2 \frac{dL_2}{\underbrace{dx}} = 0$$

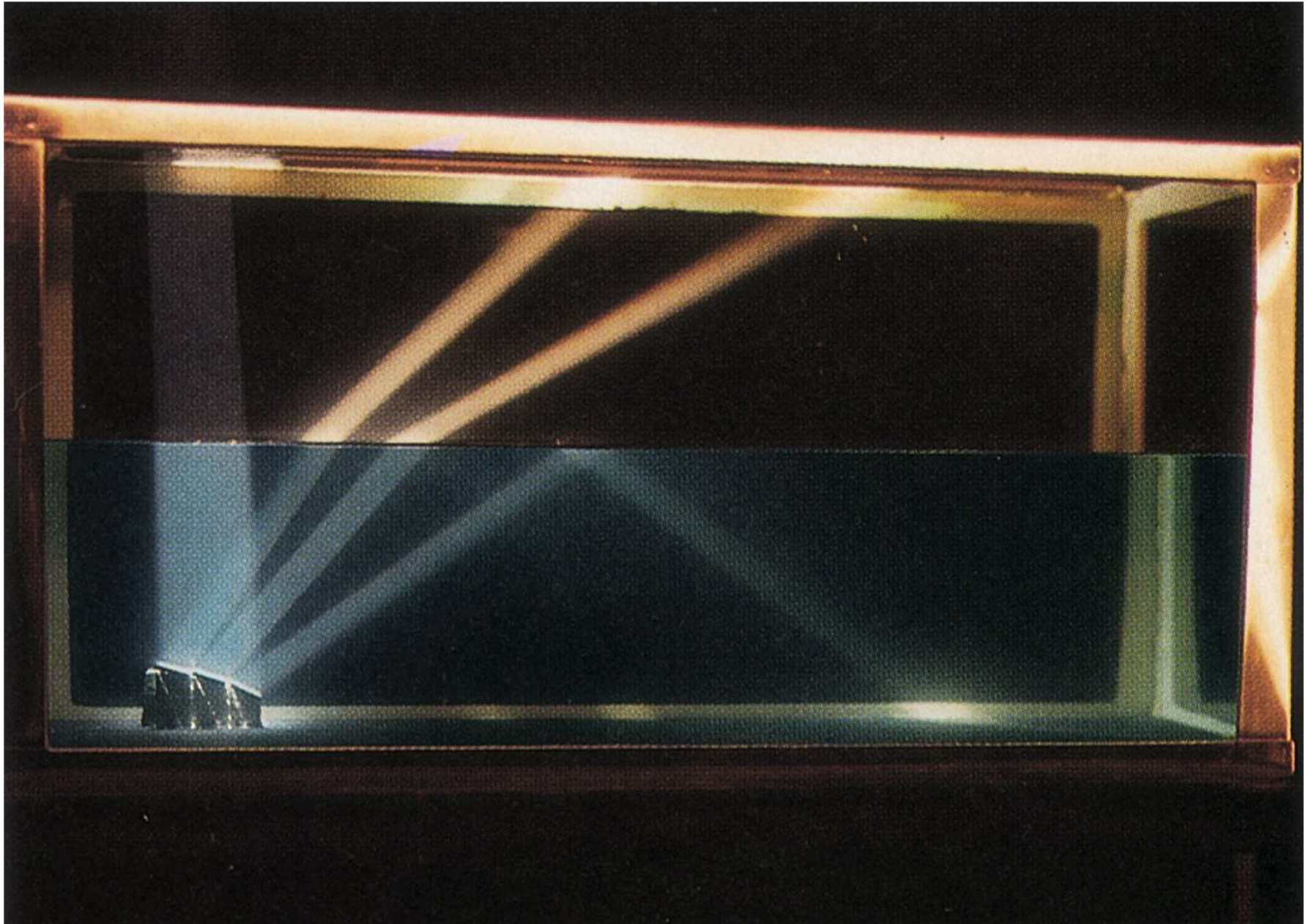
$$\frac{x}{L_1} - \frac{d-x}{L_2}$$

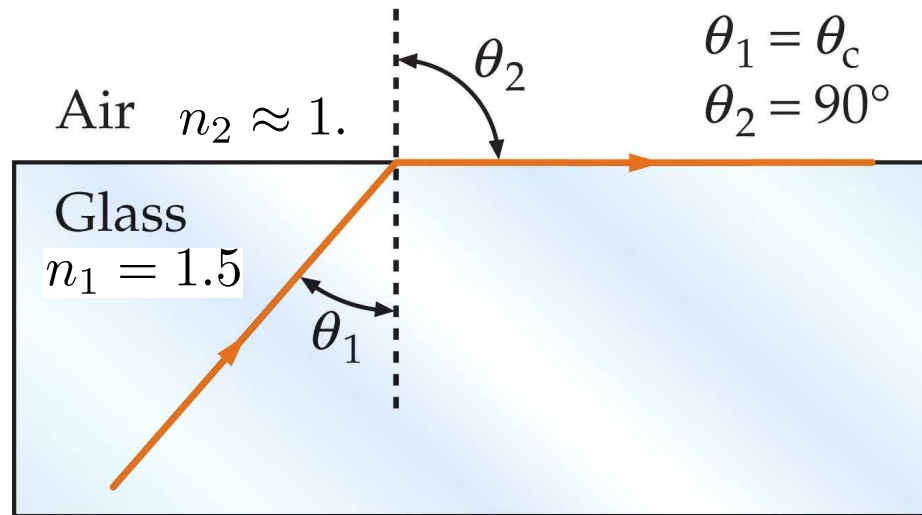
$$n_1 \sin \theta_1 - n_2 \sin \theta_2 = 0$$

## La reflexió interna total

$$\sin \theta_c = \frac{n_2}{n_1} \sin 90^\circ = \frac{n_2}{n_1}$$

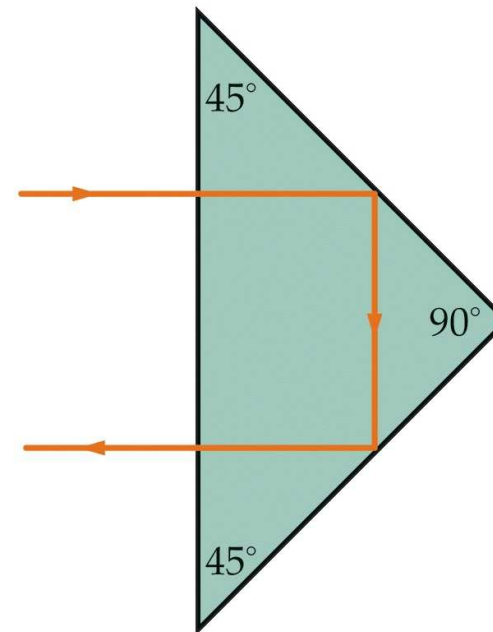
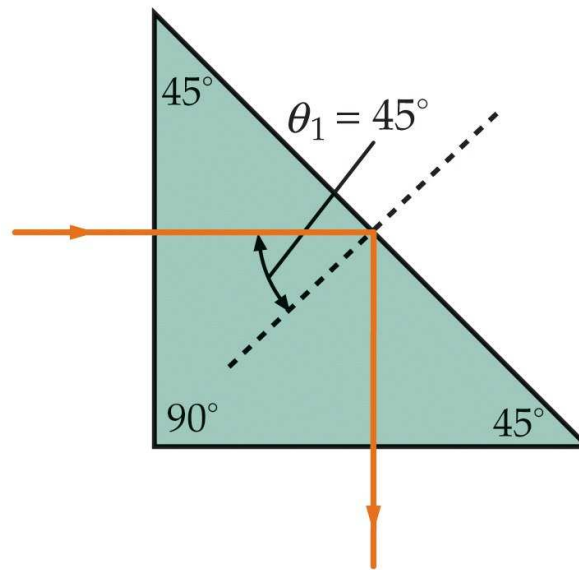


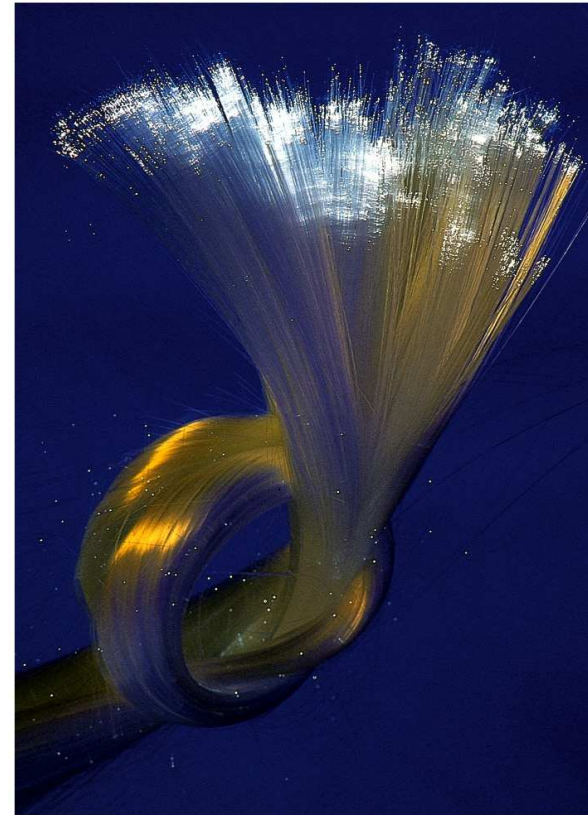
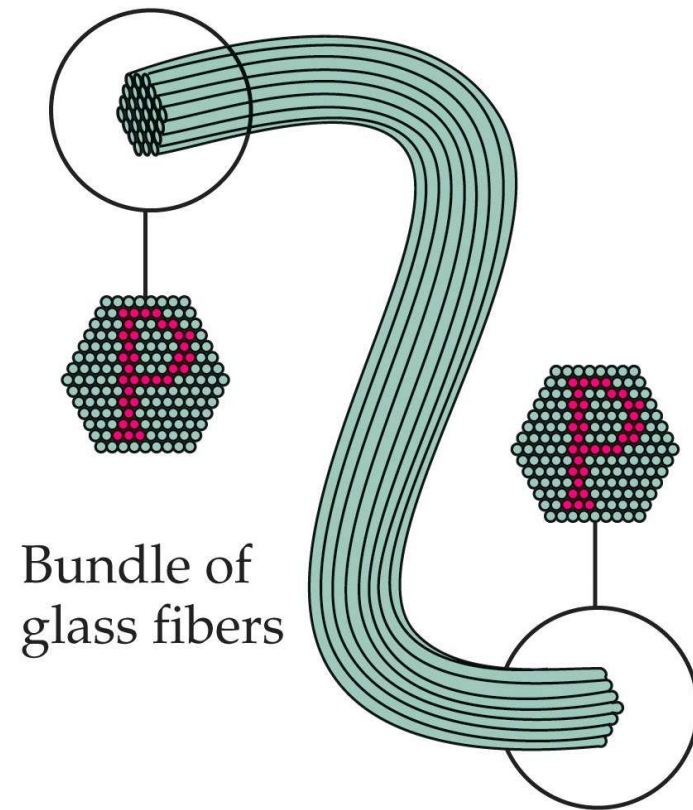




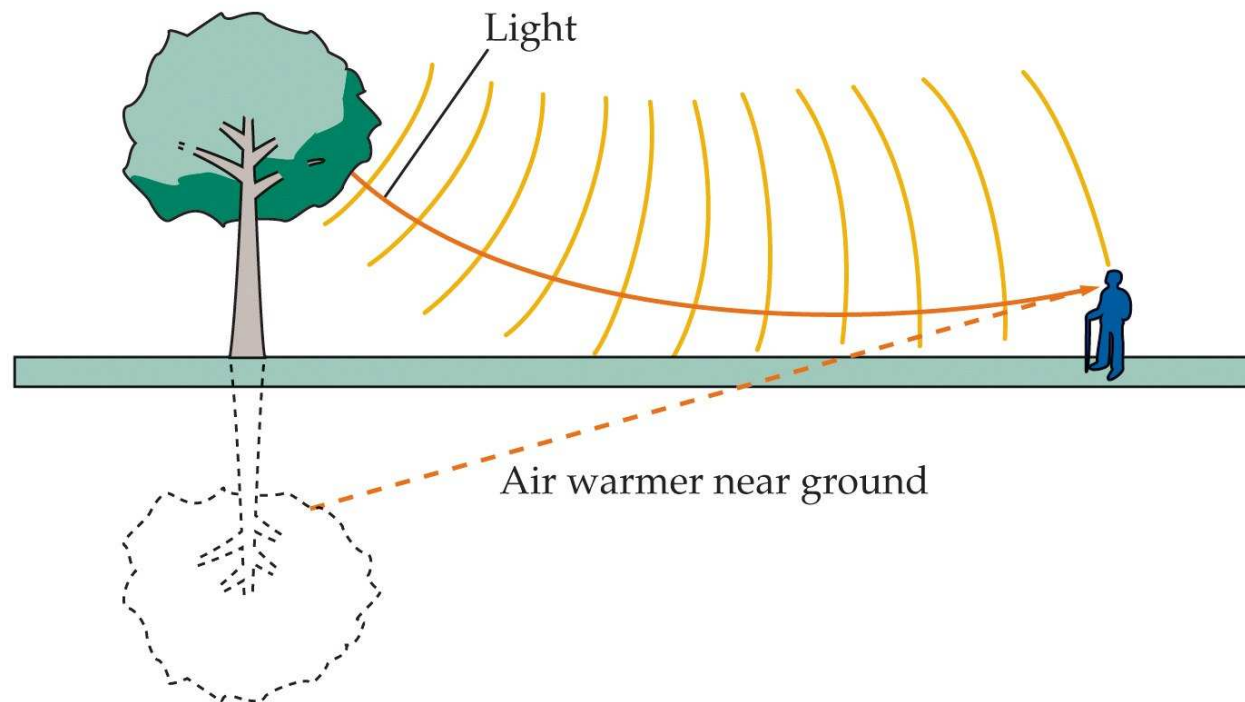
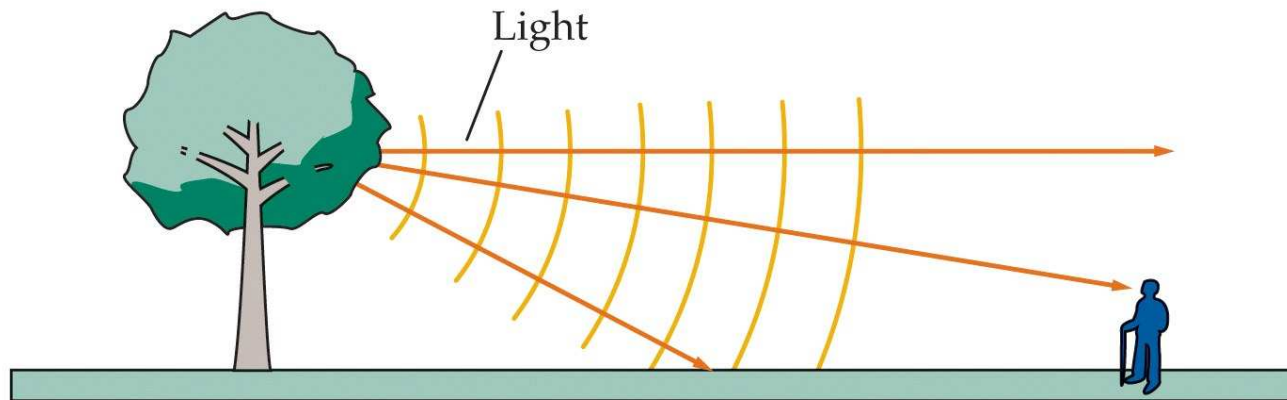
$$\sin \theta_c = \frac{n_2}{n_1} = \frac{1}{1.5}$$

$$\theta_c = 41.8^\circ$$





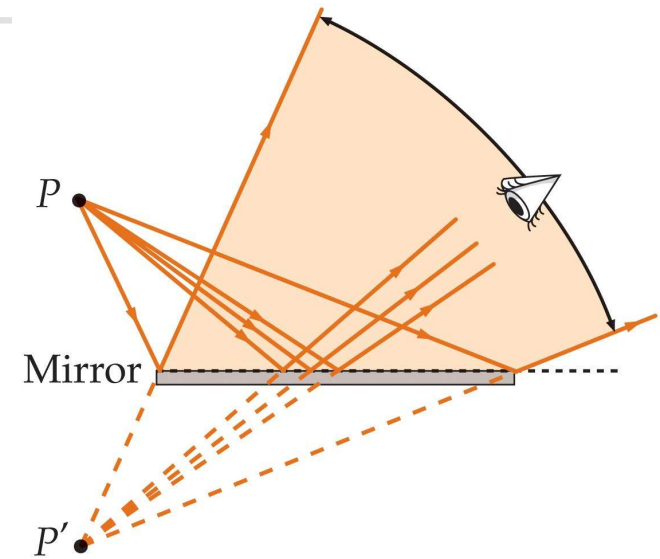
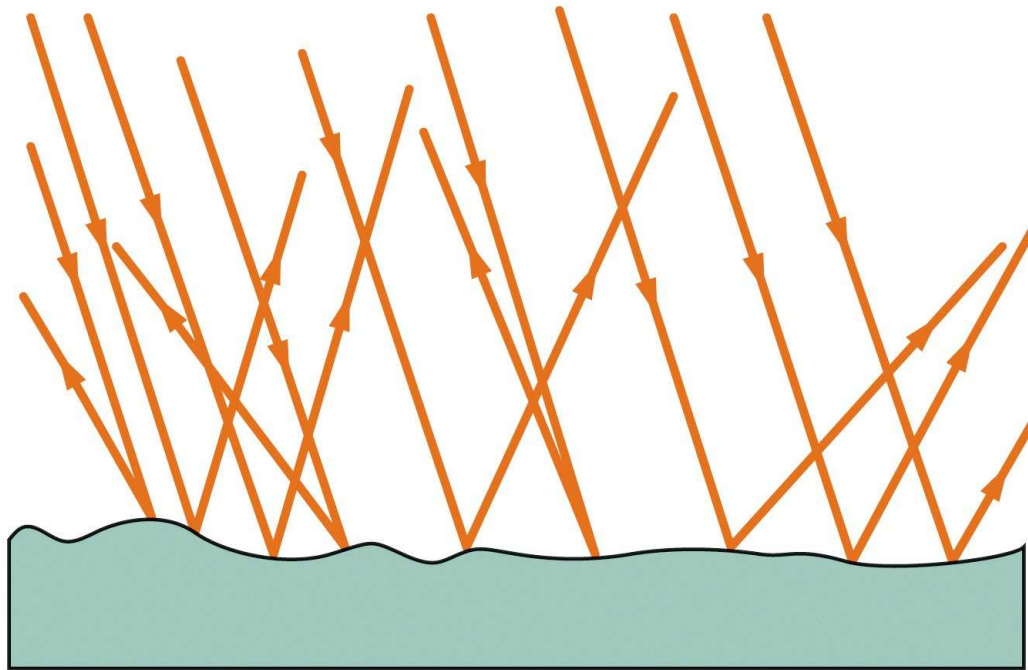
## Il.lusions optiques







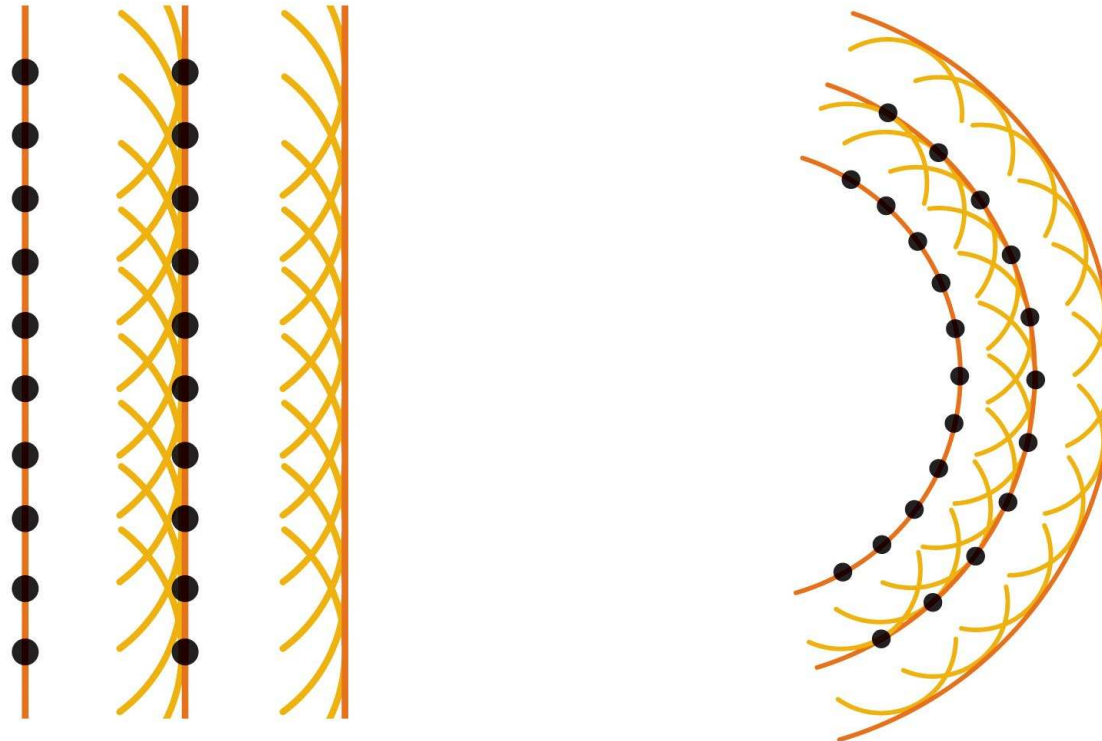
## Reflexió difosa



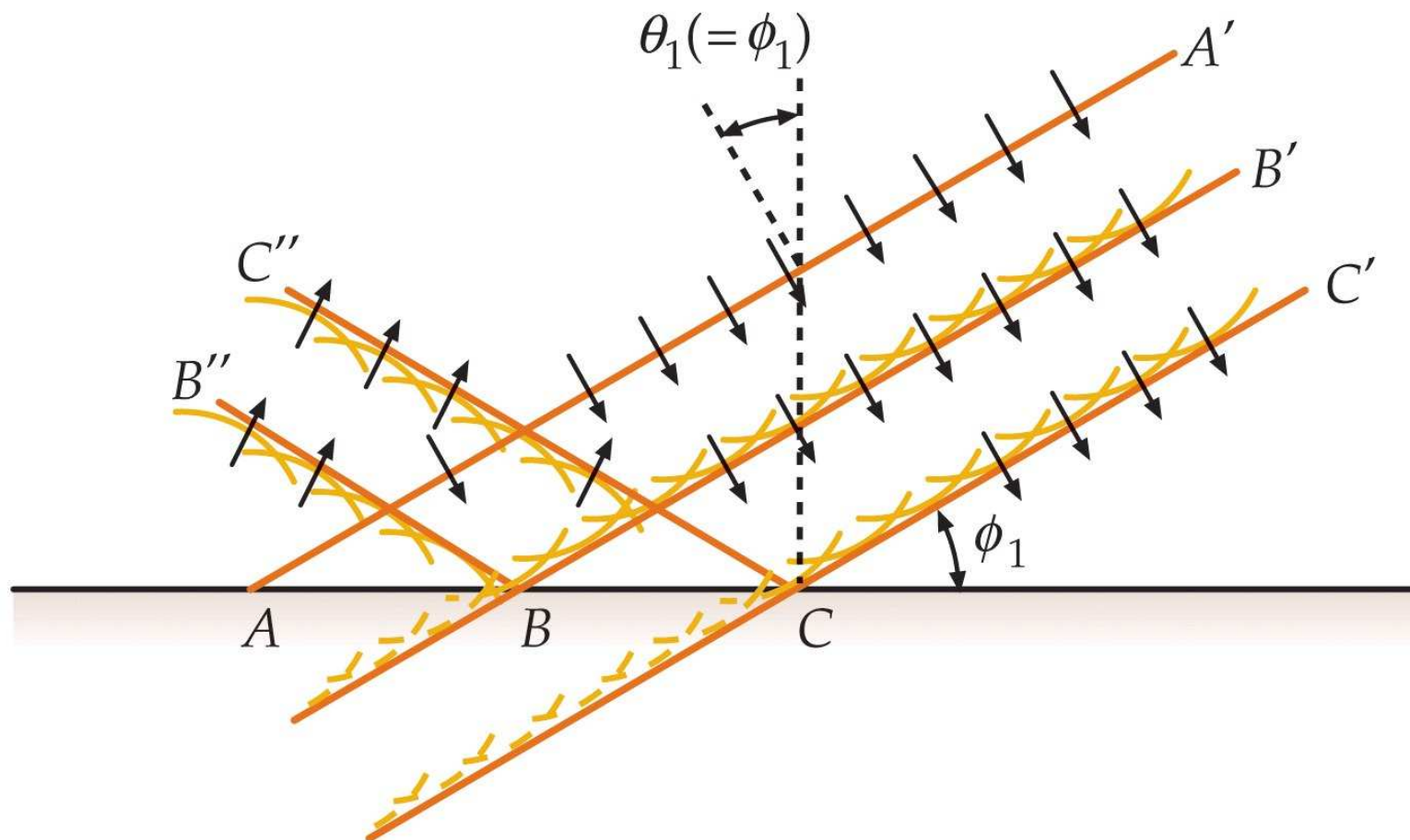
## El principi de Huygens

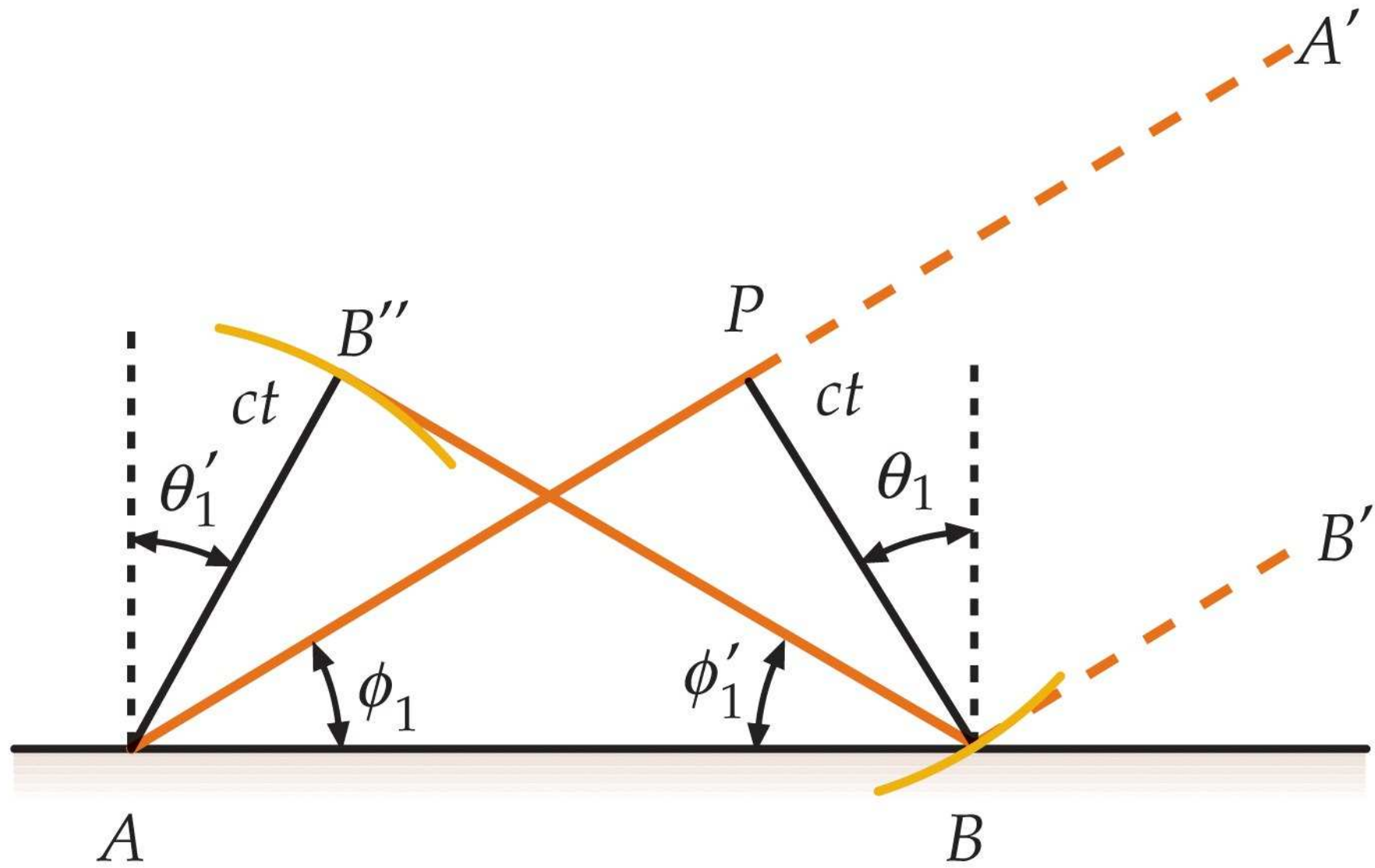
Each point on a primary wavefront serves as the source of spherical secondary wavelets that advance with a speed and frequency equal to those of the primary wave. The primary wavefront at some later time is the envelope of these wavelets.

HUYGENS'S PRINCIPLE

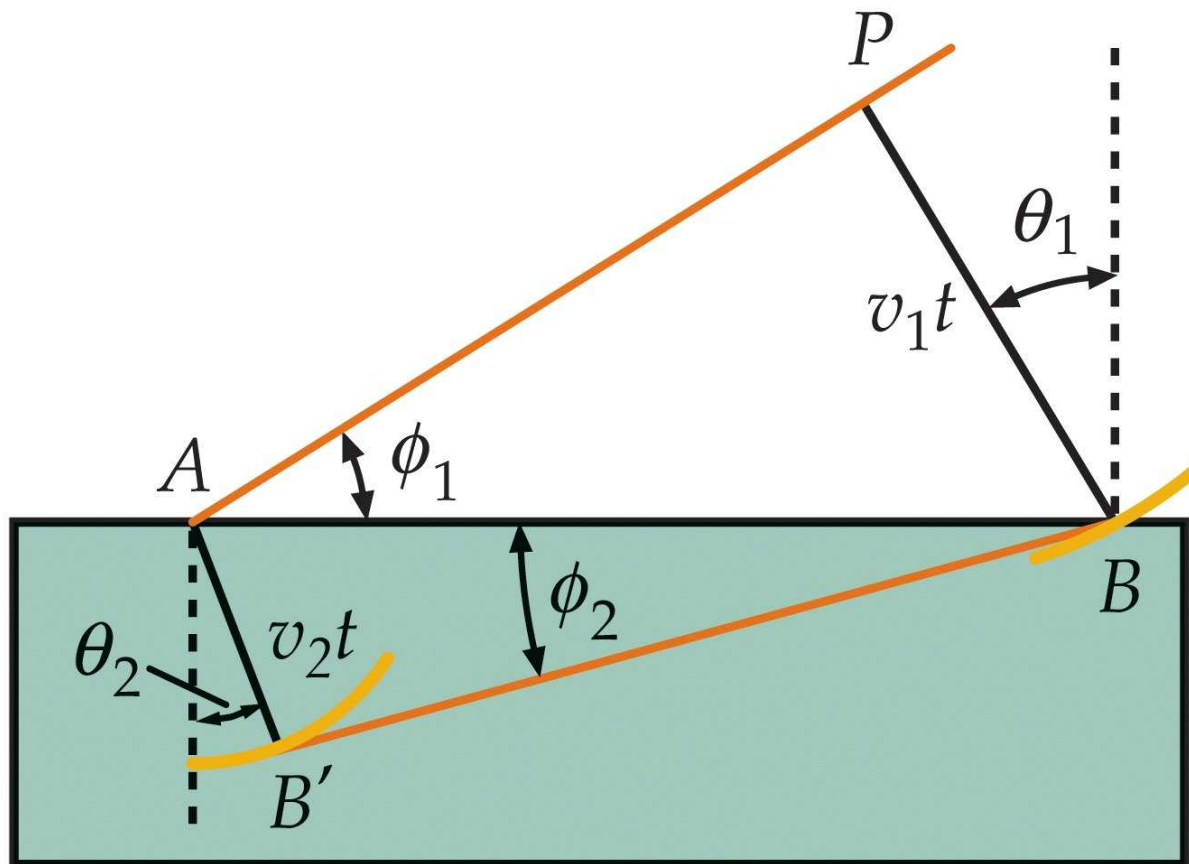


Llei de reflexió a partir del principi de Huygens





Llei de Snell a partir del principi de Huygens



$$\sin \phi_1 = \frac{v_1 t}{AB}$$

$$AB = \frac{v_1 t}{\sin \phi_1} = \frac{v_1 t}{\sin \theta_1}$$

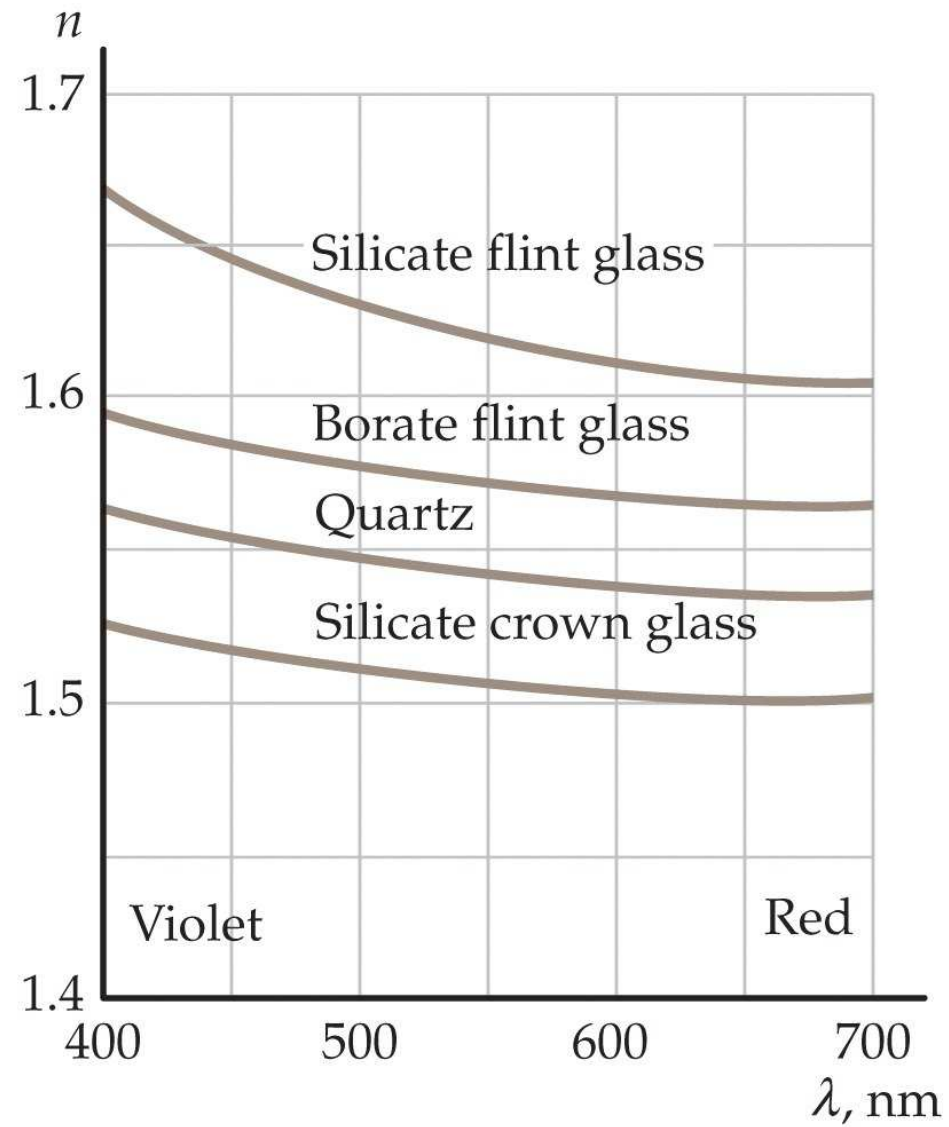
$$\sin \phi_2 = \frac{v_2 t}{AB}$$

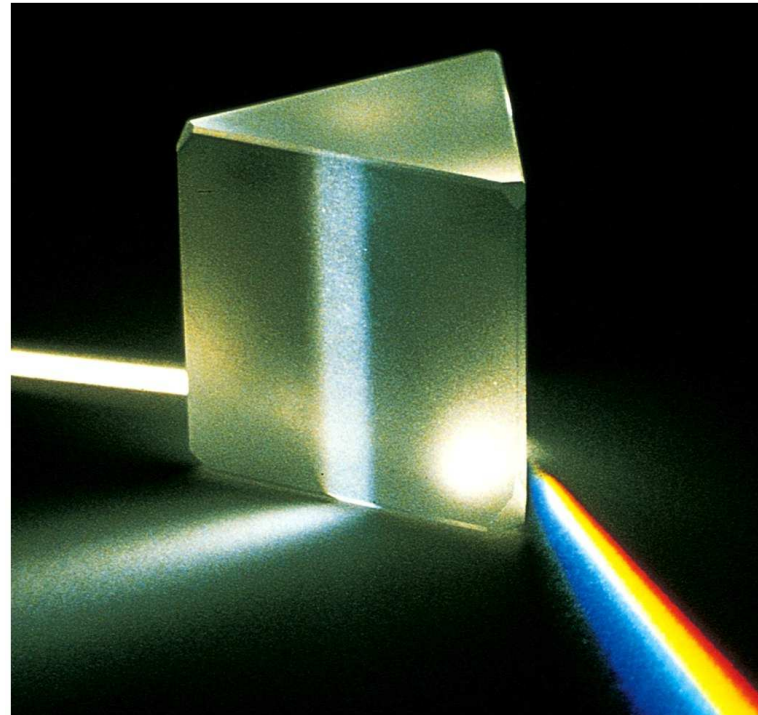
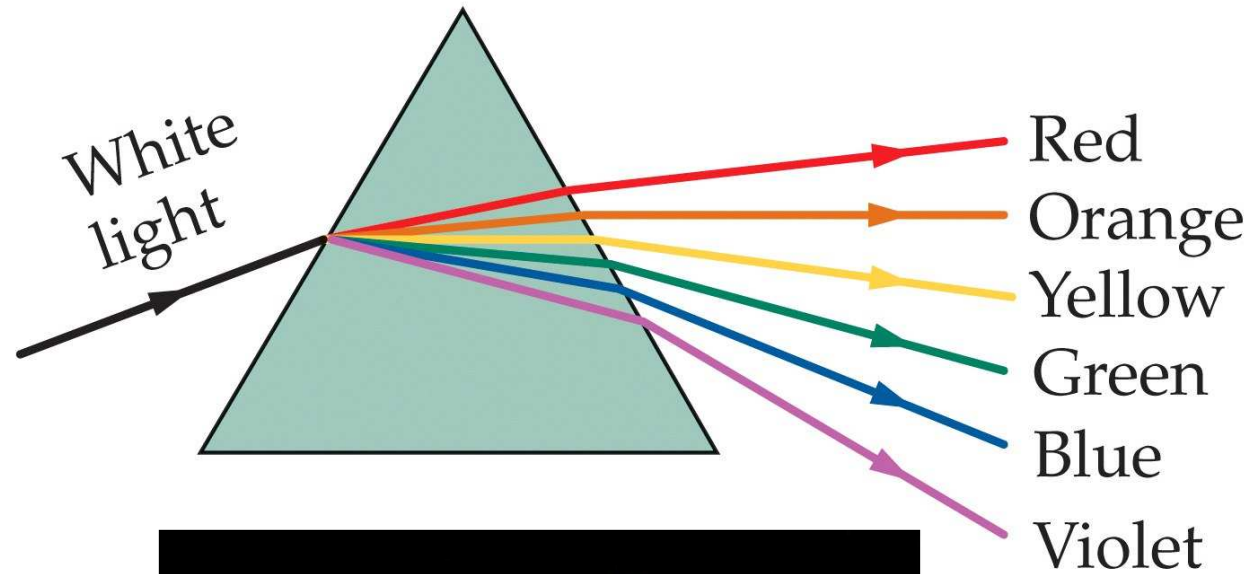
$$AB = \frac{v_2 t}{\sin \phi_2} = \frac{v_2 t}{\sin \theta_2}$$

$$\frac{v_1 t}{\sin \theta_1} = \frac{v_2 t}{\sin \theta_2}$$

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

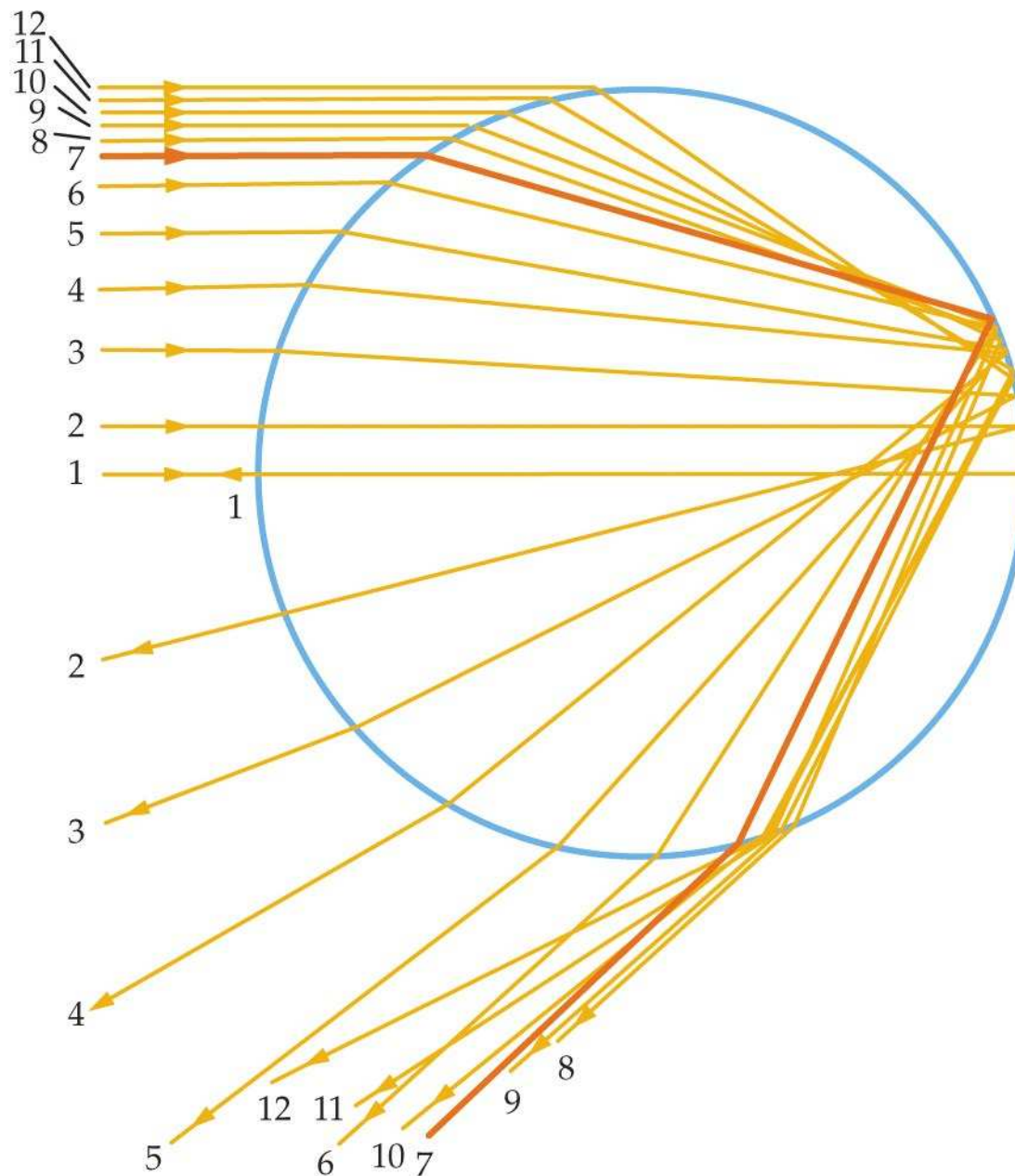
# Dispersió

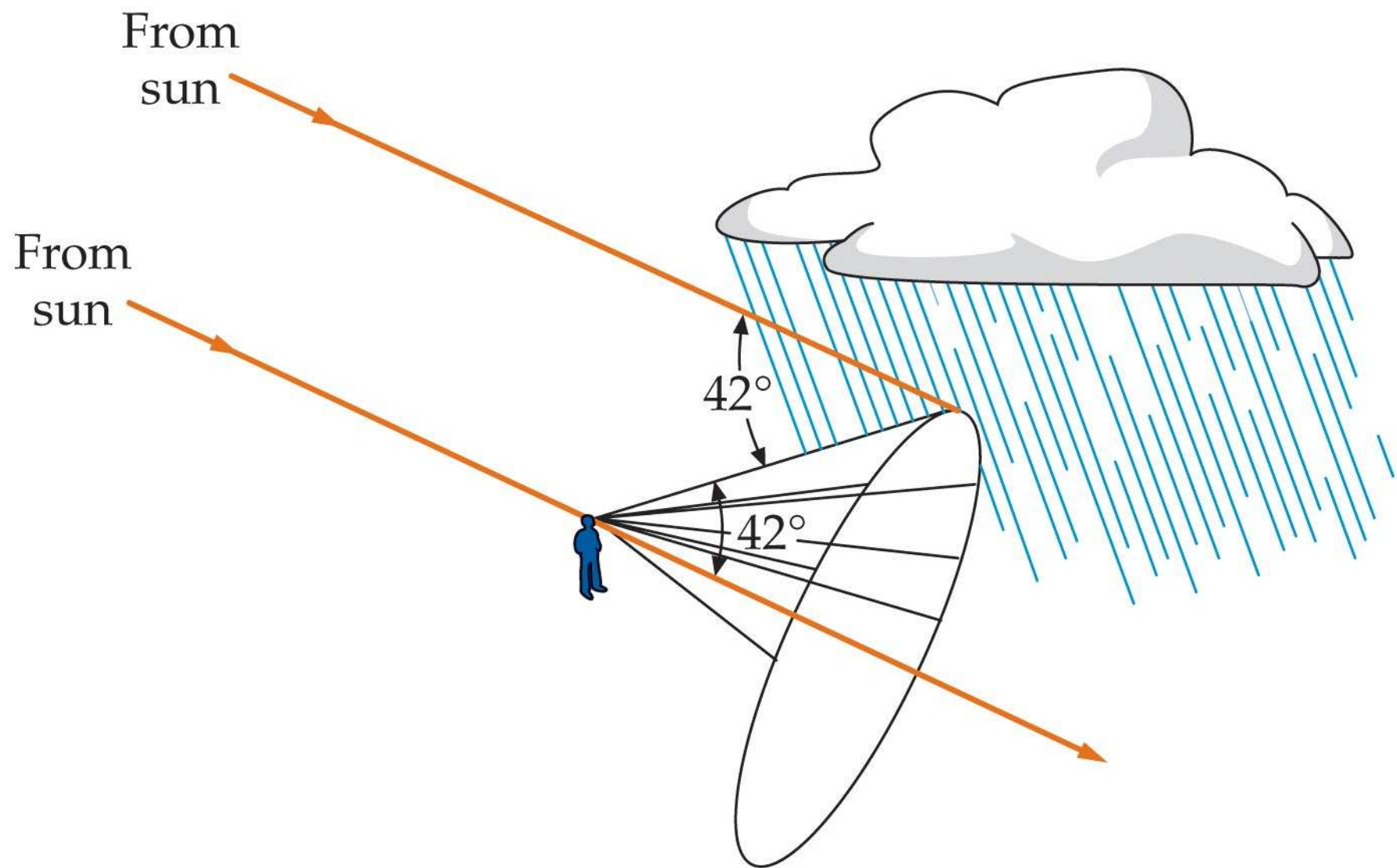


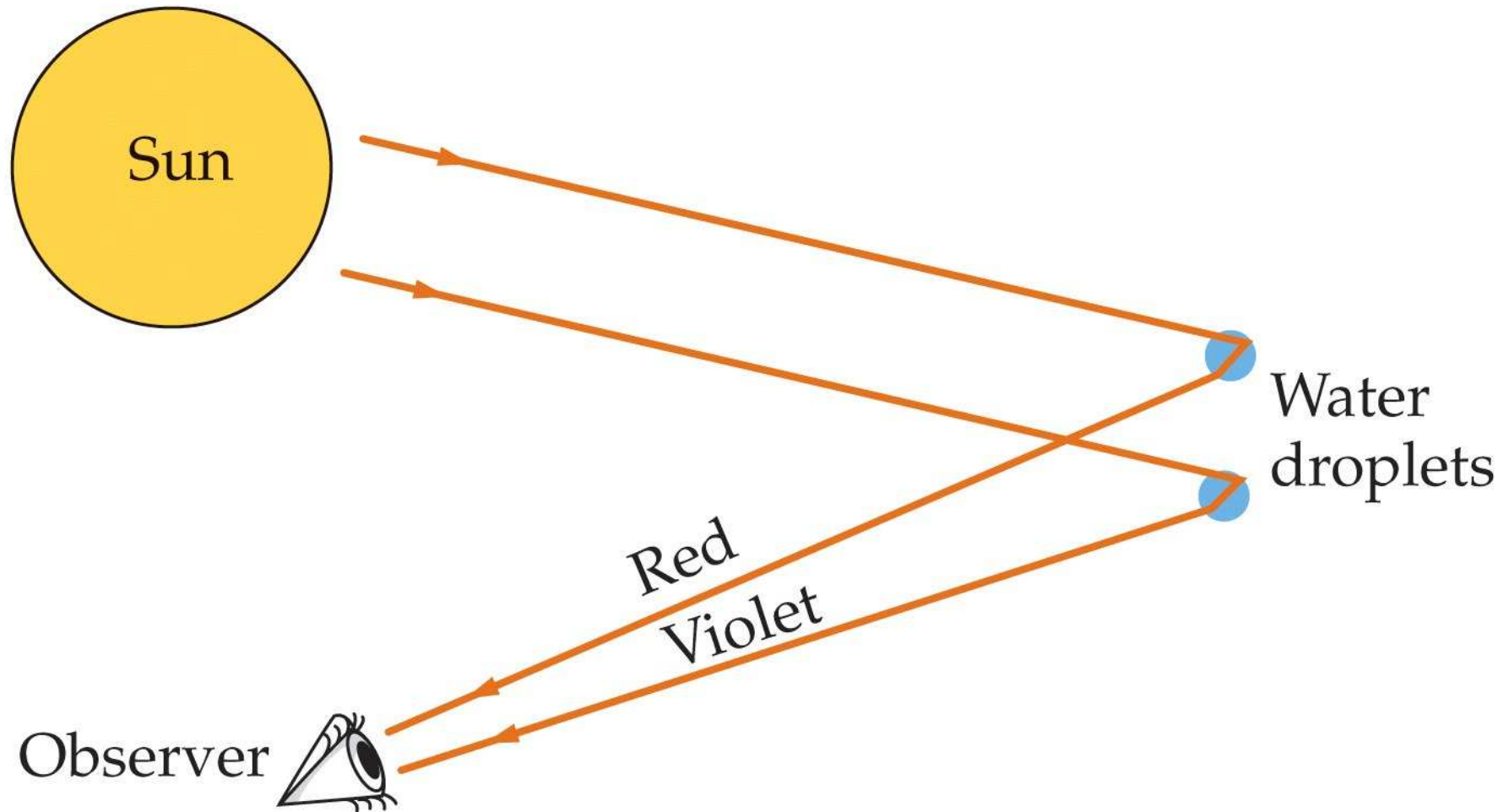


## Arc de Sant Martí (Arco Iris, Rainbow)

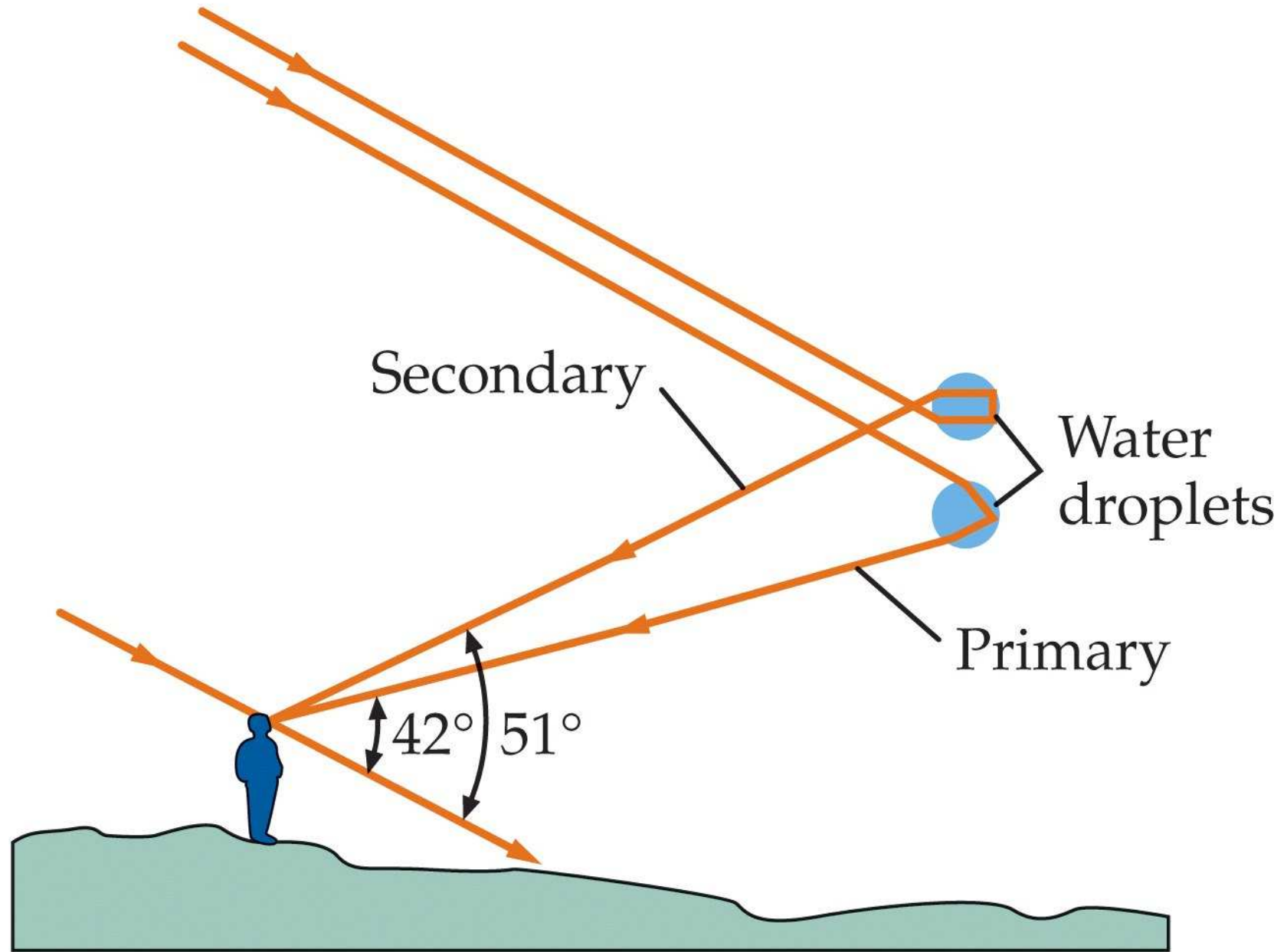
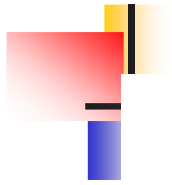
Concentració de rajos  
de Descartes

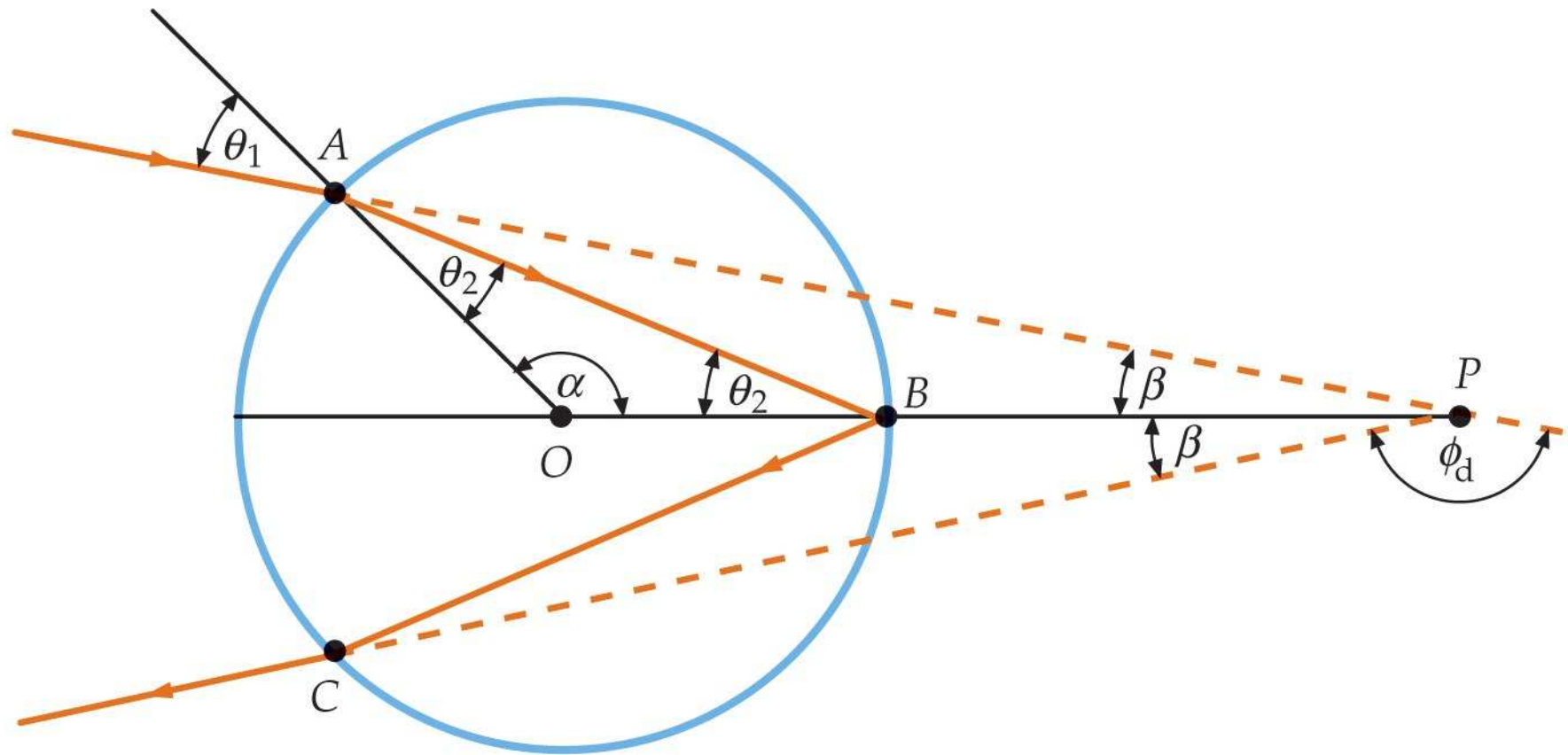


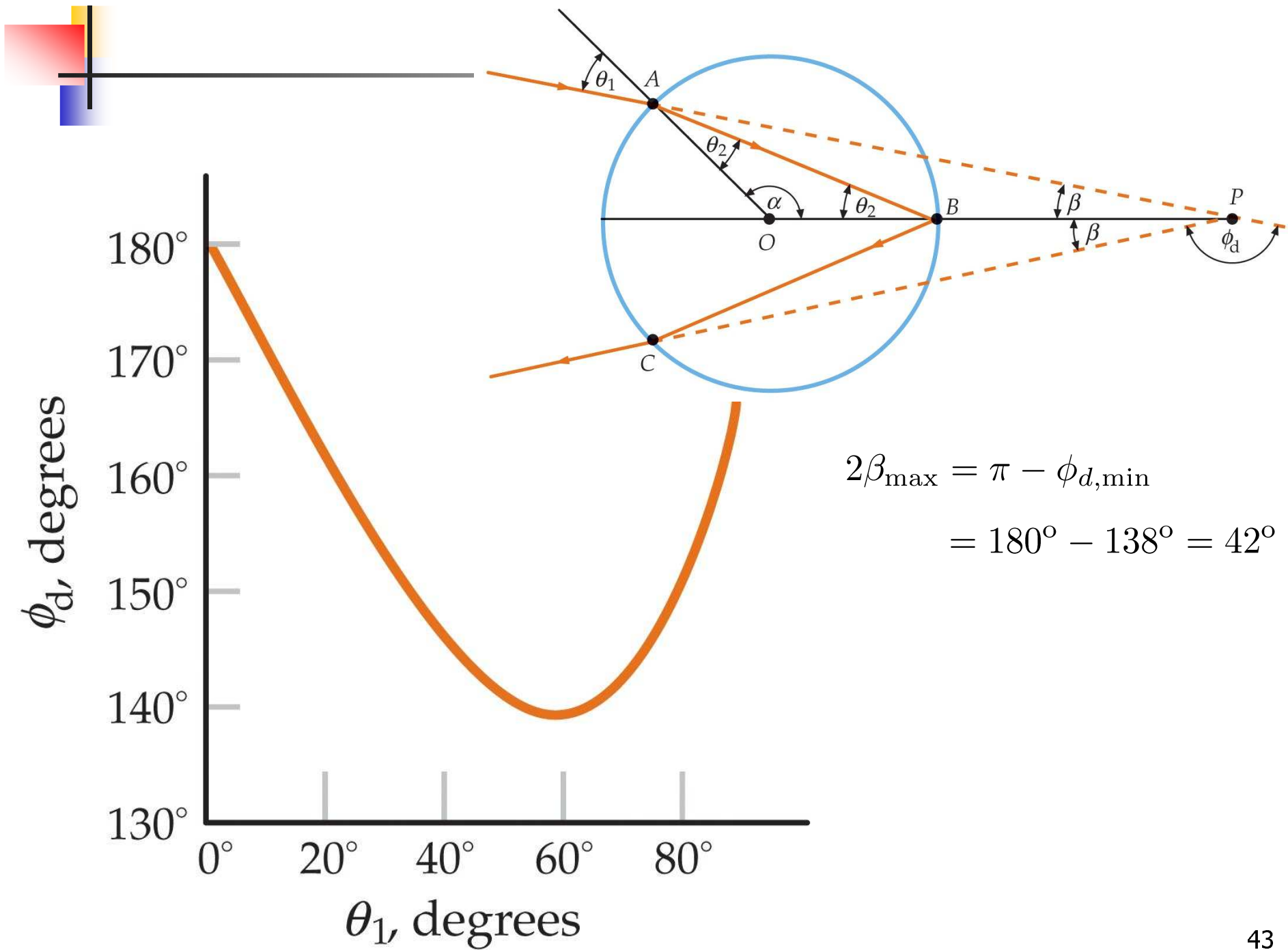








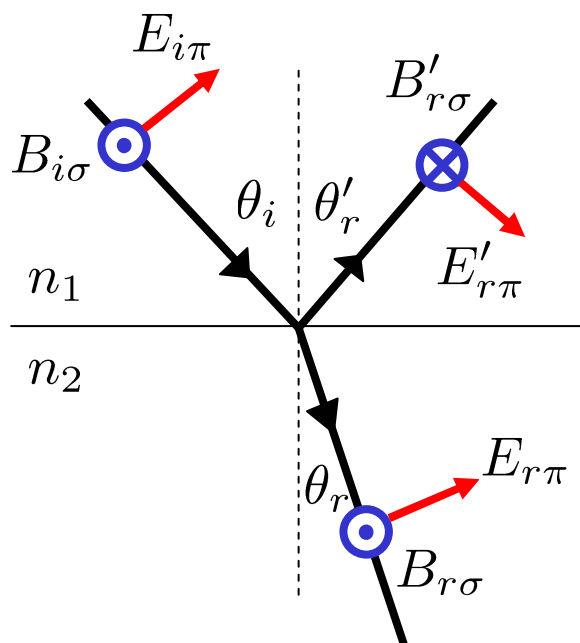




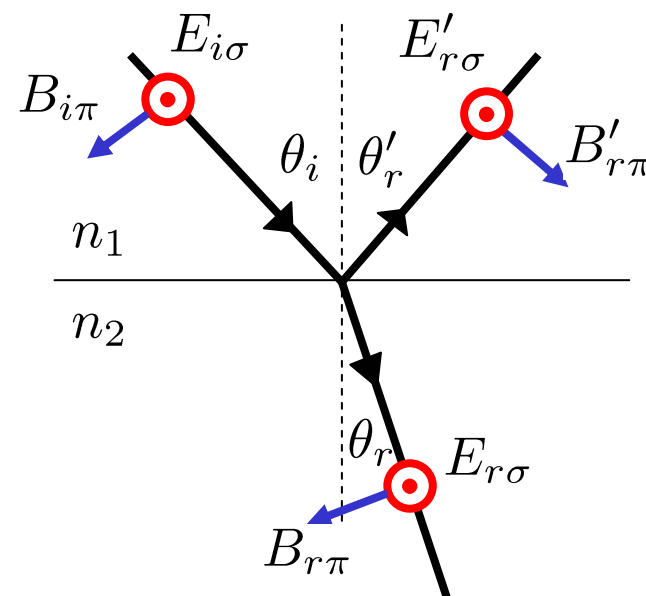
# Polarització

Components  $\left\{ \begin{array}{l} \text{paral.lela} \quad E_{\pi}, B_{\pi} \\ \text{perpendicular} \quad E_{\sigma}, B_{\sigma} \end{array} \right.$

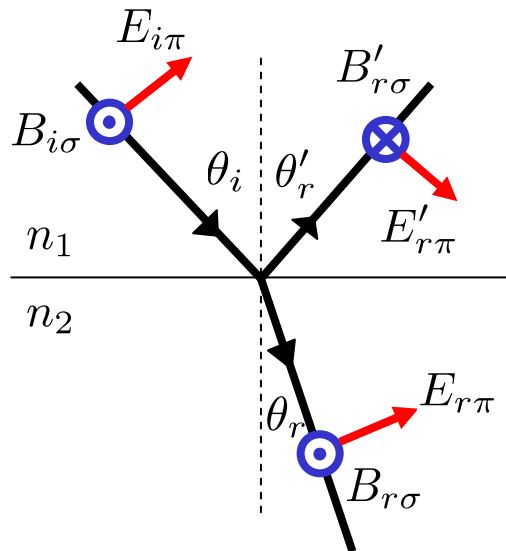
**(a) Polarització al pla d'incidència**



**(b) Polarització perpendicular al pla d'incidència**

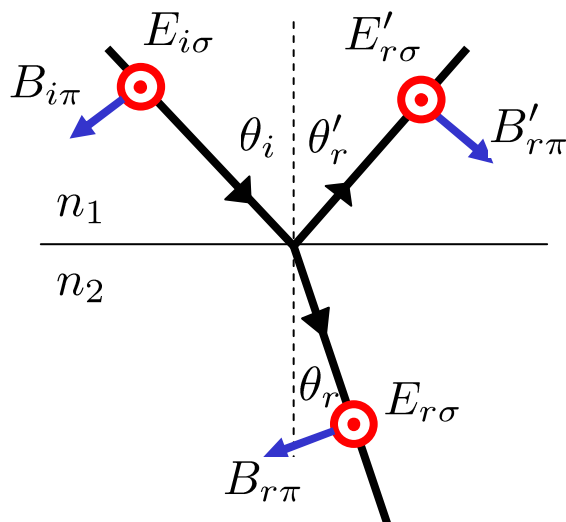


## Coeficients de reflexió i transmissió



$$R_\pi = \frac{E'_{r\pi}}{E_{i\pi}} = \frac{n_1 \cos \theta_r - n_2 \cos \theta_i}{n_1 \cos \theta_r + n_2 \cos \theta_i}$$

$$T_\pi = \frac{E_{r\pi}}{E_{i\pi}} = \frac{2n_1 \cos \theta_i}{n_1 \cos \theta_r + n_2 \cos \theta_i}$$



$$R_\sigma = \frac{E'_{r\sigma}}{E_{i\sigma}} = \frac{n_1 \cos \theta_i - n_2 \cos \theta_r}{n_1 \cos \theta_i + n_2 \cos \theta_r}$$

$$T_\sigma = \frac{E_{r\sigma}}{E_{i\sigma}} = \frac{2n_1 \cos \theta_i}{n_1 \cos \theta_i + n_2 \cos \theta_r}$$

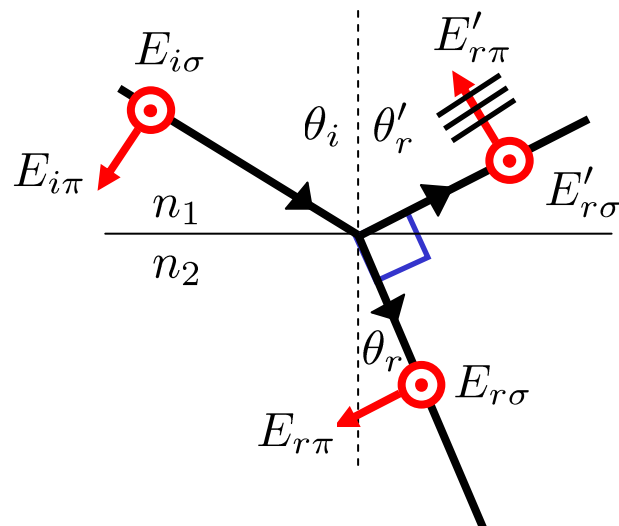
La reflexió paral·lela es pot anul·lar

$$R_{\pi} = 0 \quad \begin{cases} E'_{r\pi} = 0 \\ \text{Ona reflexada polaritzada } \sigma \end{cases}$$

$$R_{\pi} = \frac{E'_{r\pi}}{E_{i\pi}} = \frac{n_1 \cos \theta_r - n_2 \cos \theta_i}{n_1 \cos \theta_r + n_2 \cos \theta_i}$$

$$\text{(Snell)} \quad \left. \begin{array}{l} n_1 \cos \theta_r = n_2 \cos \theta_i \\ n_1 \sin \theta_i = n_2 \sin \theta_r \end{array} \right\} \Rightarrow \begin{array}{l} \sin \theta_i \cos \theta_i = \sin \theta_r \cos \theta_r \\ 2\theta_i = \pi - 2\theta_r \end{array}$$

$$\theta_i + \theta_r = \frac{\pi}{2}$$

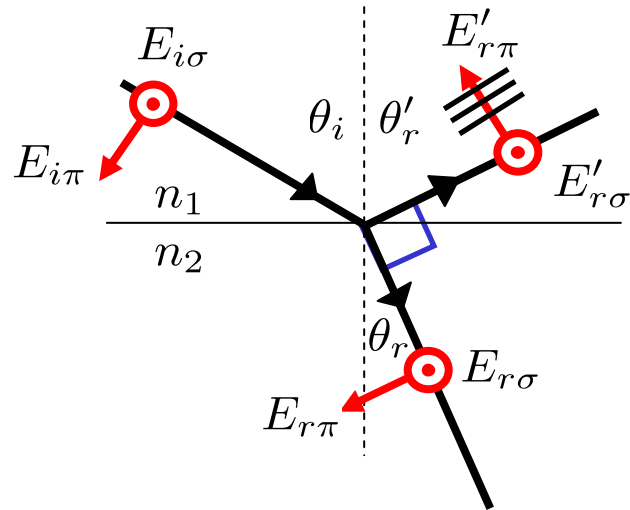


### Llei de Brewster

Quan el raig reflectit i refractat són perpendiculars aleshores el raig reflectit està polaritzat en direcció perpendicular al pla d'incidència.



## Angle de Brewster $\theta_i = \theta_B$



$$\theta_i + \theta_r = \frac{\pi}{2}$$

$$\tan \theta_i = \frac{\sin \theta_i}{\cos \theta_i} = \frac{\frac{n_2}{n_1} \sin \theta_r}{\cos \theta_i} = \frac{\frac{n_2}{n_1} \sin(\pi/2 - \theta_i)}{\cos \theta_i} = \frac{n_2}{n_1}$$

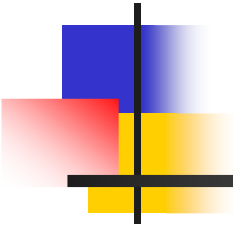
$$\tan \theta_B = \frac{n_2}{n_1}$$

**En general**       $R_\sigma \neq 0$        $T_\pi \neq 0$        $T_\sigma \neq 0$

$T > 0$       Incident i transmesa en fase

$R < > 0$

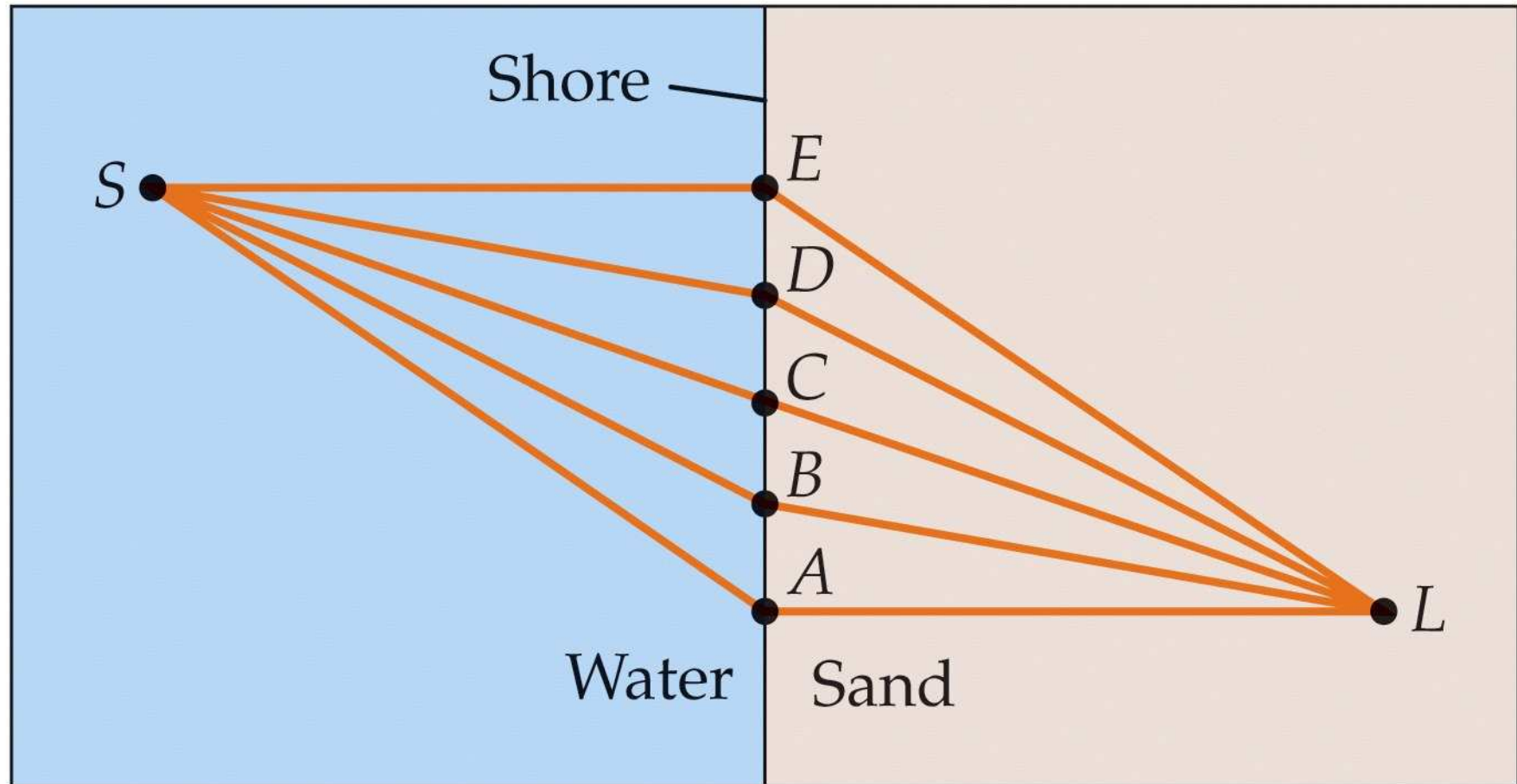




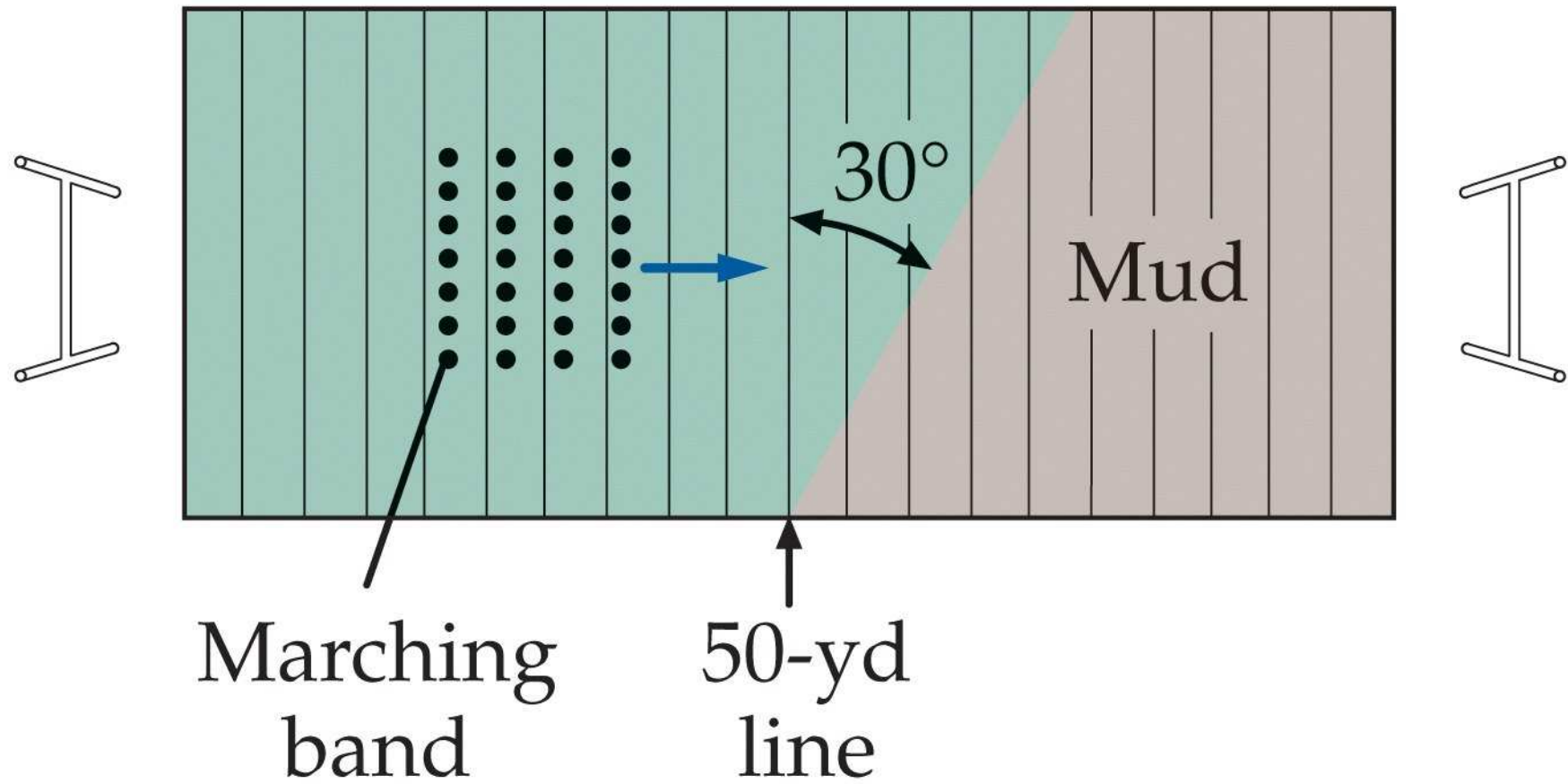
# Problems

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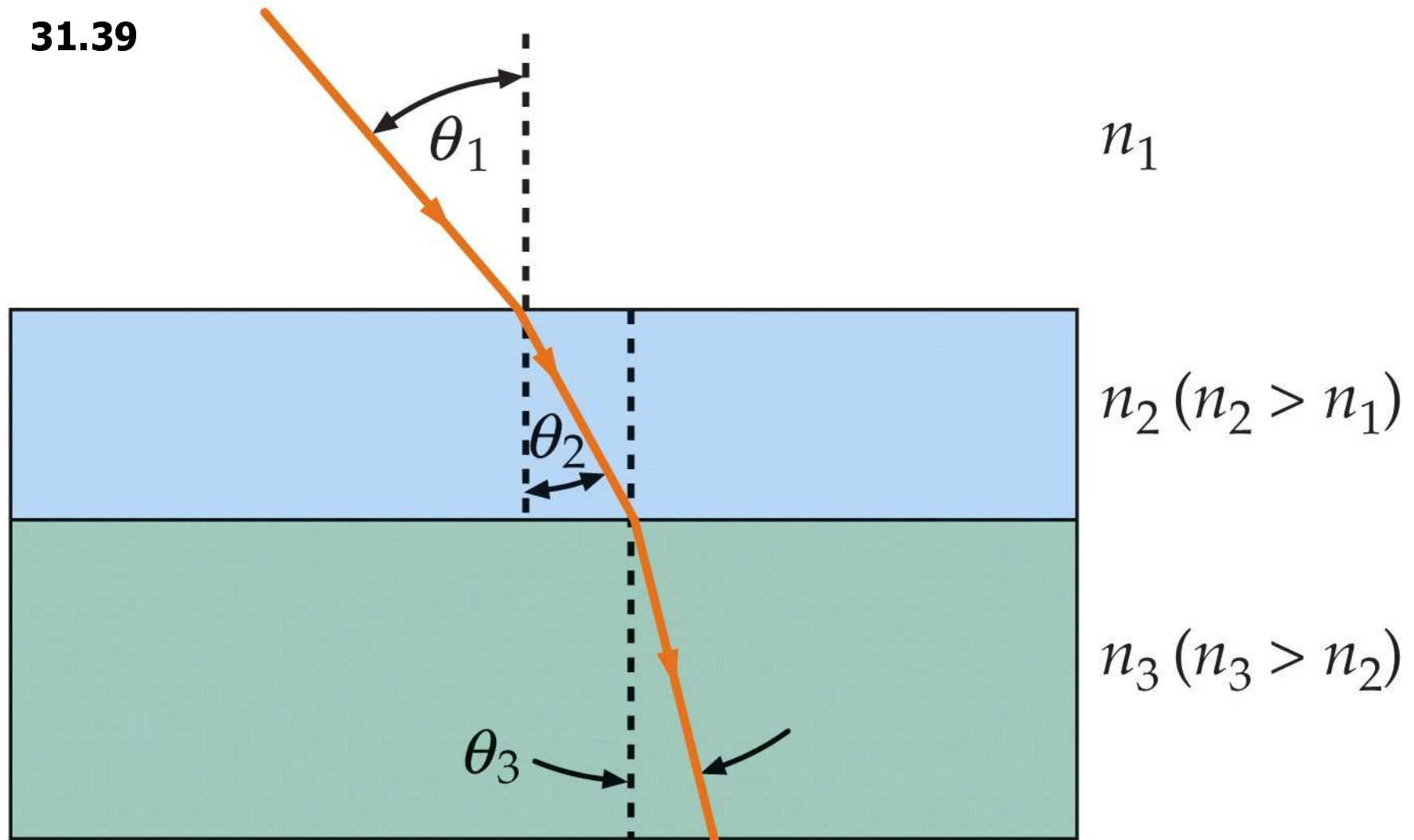
31.7

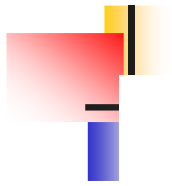


31.38

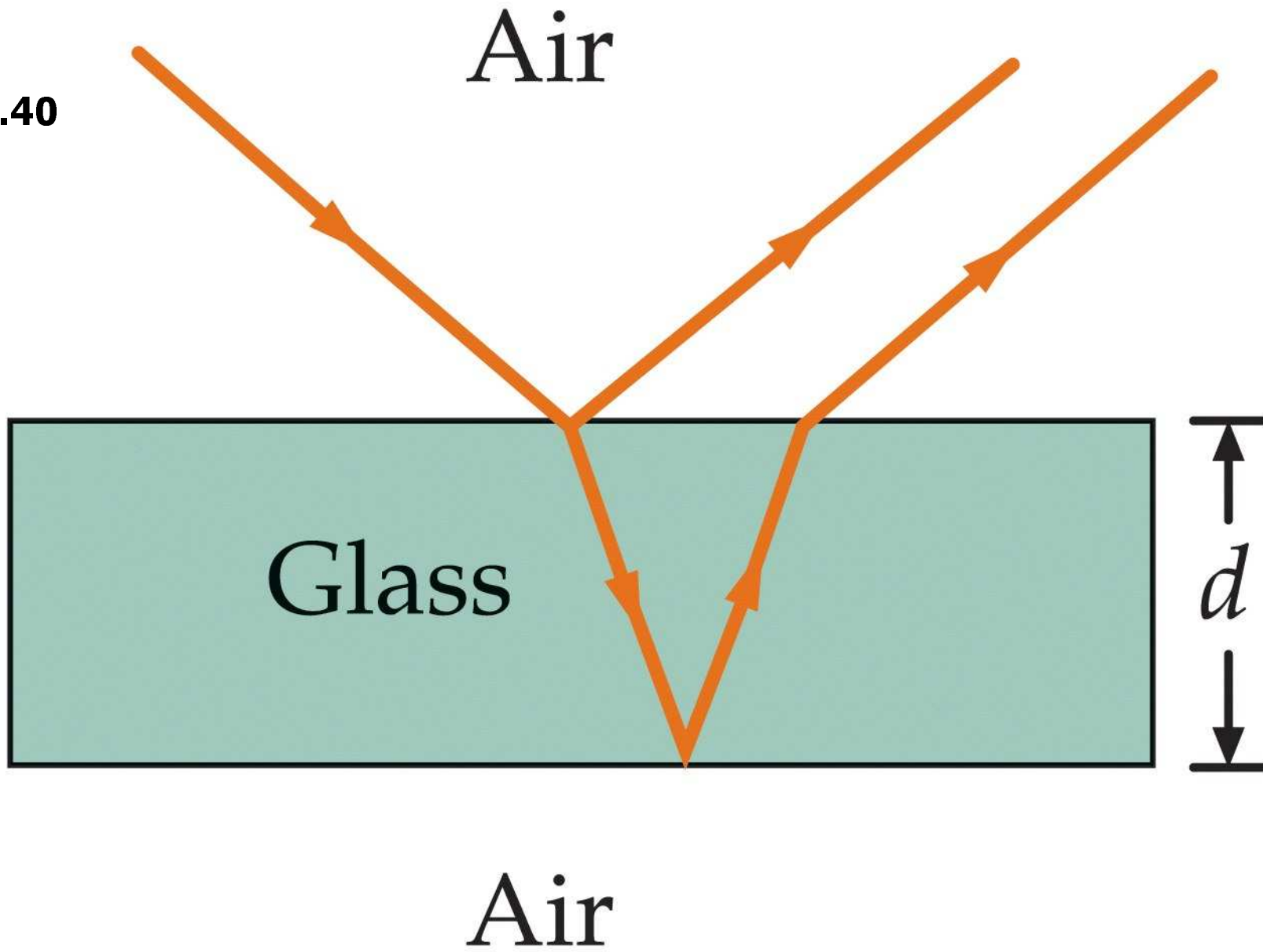


31.39

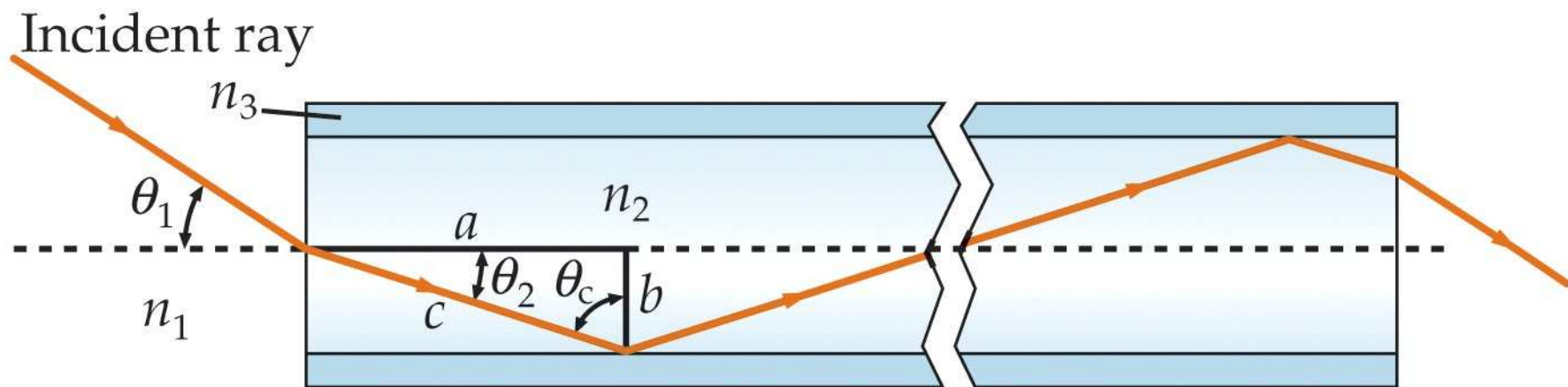




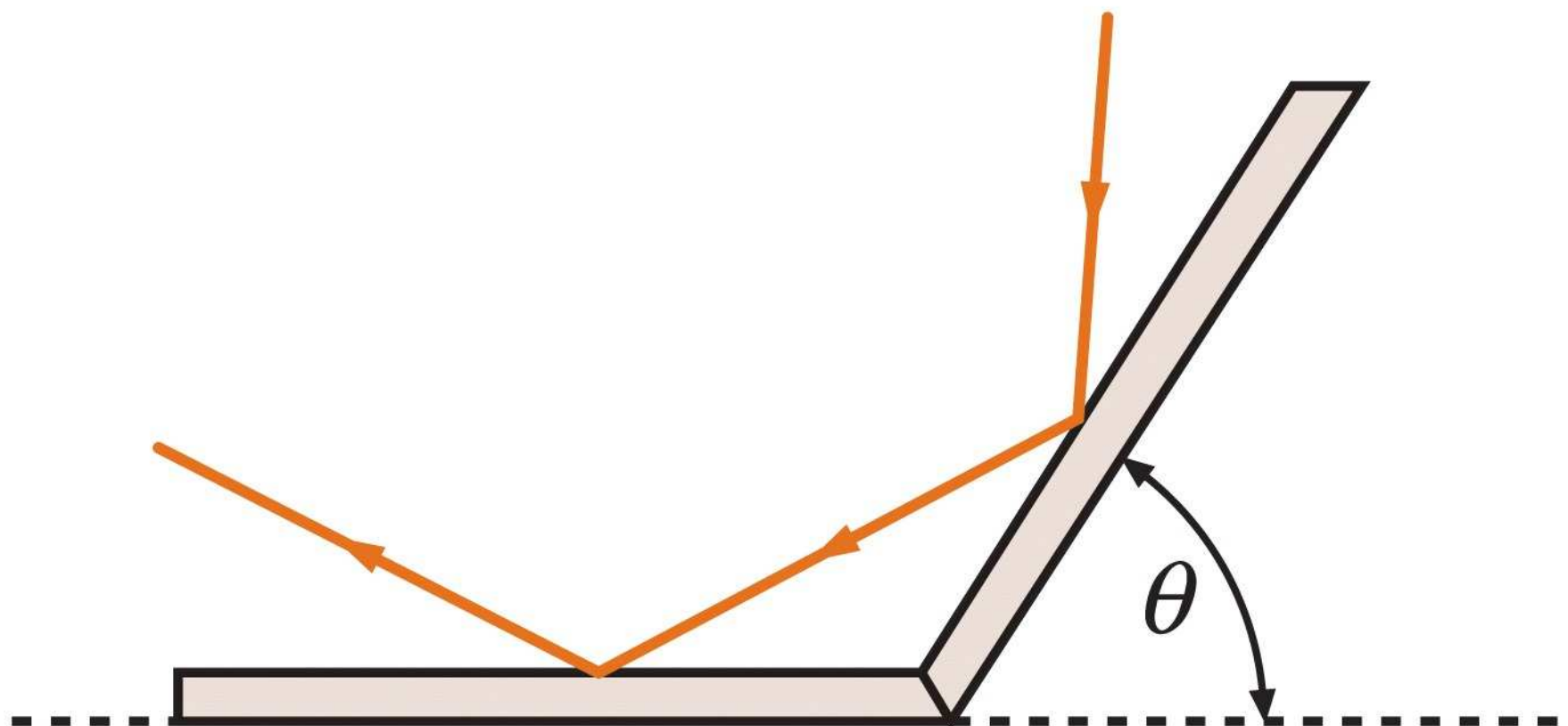
31.40



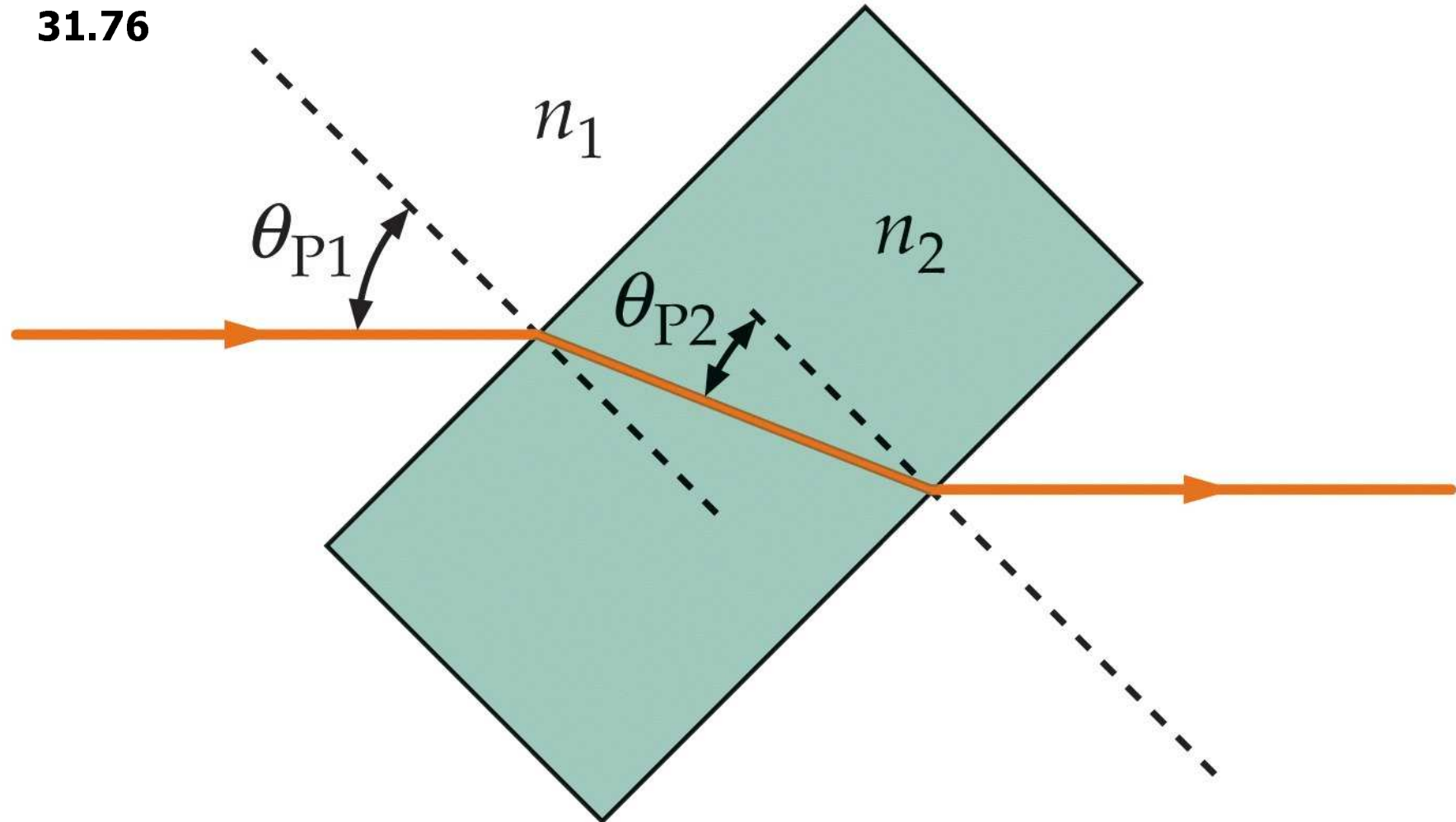
31.46

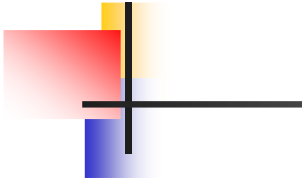


31.68



31.76





**31.78**

**31.79**

